STAT 341



SPECIAL EXAMINATION <u>THIRD YEAR EXAMINATION FOR THE AWARD OF DEGREE OF</u> <u>BACHELOR OF SCIENCE MATHEMATICS / BACHELOR OF SCIENCE APPLIED</u> <u>STATISTICS</u> <u>FIRST SEMESTER 2021/2022</u> (JULY, 2022)

STAT 341: SAMPLING METHODS 1

STREAM: Y3 S1

TIME: 2 HOURS

DAY: FRIDAY, 11.30 AM - 1.30 PM

DATE: 29/07/2022

INSTRUCTIONS:

1. Do not write anything on this question paper. 2. Answer Question ONE (Compulsory) and any other TWO Questions.

1 a)

- i) Give three major states of a survey design.
- ii) Give four data collection methods

b)Let \bar{x} be the mean of a simple random sample of size and drawn without replacement from a population of size *n*. Show that:

i)
$$V(\bar{x}) = \frac{N-n}{N} \frac{S^2}{n}$$
, Where
 $S^2 = \sum_{i=1}^{N} \frac{(X_i - \bar{X})^2}{N-1}$
ii) $E(S^2) = S^2$ where $S^2 = \sum_{i=1}^{n} \frac{(x_i - x)^2}{n-1}$ (15marks)

c) For a certain characteristics X for individuals in a population of size N=5, the values are 4,3,6,8 and 9

i) Calculate(\overline{X}), the population mean.

ii) Calculate S^2 , the population variance

iii) For all possible samples of sixe n=2 calculate \bar{x} (Hint: there are 10 such samples)

iv)Calculate the variance of the values obtained in (iii) and calculate the quantity

$$\frac{N-n}{N}\frac{S^2}{n}$$
 (8marks)

- 2. a) Give reasons why stratification may be suitable in surveys (4marks)
- b) Obtain n_h for Neyman allocation, where n_h is the size of the sample from the hth stratum. (5marks)
- c) A population has three strata with sizes means and variances as given below

	N _h	\bar{X}_h	S _h
Stratum 1	18000	5.2	2.8
Stratum 2	30000	4.8	3.0
Stratum 3	72000	6.9	2.5

- i) Obtain the population mean and variance
- ii) Obtain the proportional and Neyman allocation if a stratified sample of size 10000 was to be drawn in a survey. (11marks)

3.a) Give two advantages of systematic sampling over sample random sampling.

(2marks)

b) The data in the table below are for a small artificial population that exhibits a fairly steady rising trend. N=40, K=10 and N=4 each column represent a systematic sample and rows are the strata.

Strata	1	2	3	4	5	6	7	8	9	10
i	0	1	1	2	5	9	7	7	8	6
ii	6	8	9	10	13	12	15	16	16	17
iii	18	19	20	20	24	23	25	28	29	27
iv	26	30	31	31	33	32	35	37	38	38

Calculate

i) V_{ran}

ii) V_{st}

iii) Prepare ANOVA table

4a) In a population with N=6, the values of y are 8,3,1,11,4 and 7. If a random sample of size 2 are drawn with replacement from this population . Show by findings all possible samples that

$$V(\bar{y})$$
 satisfies the equation ; (11marks)
 $V(\bar{y}) = \frac{\delta^2}{n} = \frac{S^2}{n} \frac{(N-1)}{N}$

b) In a study of plant disease the plants were grown in 160 small plots containing nine plants each, A random sample of 40 plots was chosen and three random plants in each sampled plots were examined for the presence of diseases. It was found that 22 had no diseased plants (out of three),11 had one, 4 had two and 3 had three estimate;

i) The proportion of diseased plant

ii) Its standard error

5 a) Consider a population of size N in which the number of units possessing a certain characteristics is A, let the number of units possessing the characteristic in a simple random sample of size n be a.

i) Prove that
$$P=\underline{a}$$
 is an
N
Unbiased estimator of $P=A/N$
ii) Show that $V(P) = \underline{N-n} \underline{PQ}$
N-1 n
Where $Q = 1-P$

iii) Give an estimate of V(p)

b) In a simple random sample of size 65 units were found to possess a certain characteristic under investigation. Obtain the 99% confidence bounds for the population proportion possessing the characteristic. The population size is 7000

(9marks)

(18marks)