

# **UNIVERSITY EXAMINATIONS**

#### SPECIAL EXAMINATION

# THIRD YEAR EXAMINATION FOR THE AWARD OF THE DEGREEOF BACHELOR OF EDUCATION (SCIENCE) FIRST SEMESTER 2021/2022 (JULY, 2022)

## PHY 312: ELECTROMAGNETISM II

STREAM: Y3 S1 TIME: 2 HOURS

DAY: TUESDAY, 3:00 PM - 5:00 PM DATE: 26/07/2022

#### **INSTRUCTIONS:**

1. Do not write anything on this question paper.

2. Answer Question ONE (Compulsory) and any other TWO questions.

Permittivity of free space  $\varepsilon_0 = 8.85 \text{ x } 10^{-12} \text{F/m}$ , Permeability of free space  $\mu_0 = 4\pi \text{ x } 10^{-7} \text{ T- m/A}$ 

#### **QUESTION ONE (30 MARKS)**

- a) Define the term Gaussian Surface as used in relation to electric and magnetic fields (1 mark)
- b) State the Divergence theorem and cite an area in which this tool finds wide application (2 marks)
- c) One of the following electrostatic fields is impossible. Which one?

(i) 
$$E(r) = k [xy x^{-} + 2yz y^{-} + 3xz z^{-}]$$
  
(ii)  $E(r) = k [y^{2} x^{-} + (2xy+z^{2}) y^{-} + 2yz z^{-}]$  (6 marks)

- d) Obtain an equation for the magnetic field B if the wire in which current is flowing is long enough and B is tangential everywhere. (3 marks)
- e) A wire segment 3mm long carries current of 3A in the direction of x and lies in a magnetic field of 0.02T in the xy plane making an angle of 30° with the x-axis. What is the magnetic force exerted on the wire segment? (3 marks)

- f) Find the electric field a distance z above the midpoint of a straight line segment of length 2L which carries a uniform line charge  $\lambda$ . (6 marks)
- g) Given two infinite straight line chargesλ a distance d apart moving along at a constant speed v.
  - i. What would be the value of v that would have a magnetic attraction balance the electrical repulsion? (6 marks)
  - ii. Calculate the numerical value of v. (3 marks)

#### **QUESTION TWO**

- i) The magnitude of a position vector  $\mathbf{r} = \sqrt{(x^2 + y^2 + z^2)}$ .
  - a) Find the gradient of the quantity given.

(3 marks)

b) What is represented by the value obtained in i(a) above

(3 marks)

- ii) Two vectors  $A = 2i^{2} + 3j^{2} 4k^{2}$  and  $B = i^{2} 2j^{2} + k^{2}$ . Obtain
  - a) The dot product A.B

(3 marks)

b) The magnitude of the scalar product |A||B|

(3 marks)

c) The angle between the two vectors,  $\theta$ .

(3 marks)

d) The vector product A x B

(3 marks)

e) The magnitude of the vector product |A x B|

(3 marks)

#### **QUESTION THREE**

- i) One source of magnetic fields is a permanent magnet. List two other sources.(2 marks)
- ii) Explain one characteristic of magnetic fields.

(1 mark)

iii) State Lorentz Force Law

(1 mark)

iii) Two current carrying conductors are placed a distance d apart parallel to each other. Using Lorentz Force Law, show that force between the two conductors is given by:

$$f = \frac{\mu_0}{2\pi} \frac{I_1 I_2}{d}$$

(4 marks)

- iv) A long straight wire is carrying a steady current I.
  - (a) Find the magnetic field a distance z from the wire.

(6 marks)

(b) The wire was then made into a circular loop of radius R. Obtain the magnetic field a distance z above the centre of the circular loop. (6 marks)

### **QUESTION FOUR**

i) Define the following terms as used in electrostatics:

(2 marks)

- (a) Capacitor
- (b) Dielectric
- ii) Briefly explain how temperature affects the alignment of dipole moments of a dielectric. (2 marks)
- iii) The inner and outer cylinder conductors of a long coaxial cable used to transmit TV signal have a diameter a=0.5mm and b=1.5mm. What is the capacitance per unit length of this cable? (4 marks)
- iv) A parallel plate capacitor has square plates of sides 10cm separated by 1mm.
  - a) Calculate its capacitance

(3 marks)

- b) If this capacitor is charged to 12V, how much charge is transferred from one plate to the other? (3 marks)
- c) If the capacitor is filled with a dielectric of constant k = 2
  - (i) Find the new capacitance

(3 marks)

(ii) Find the charge on the capacitor with the dielectric if the capacitor is connected to a 12V battery. (3 marks)

#### **QUESTION FIVE**

i) State Biot-Savart's law

(1 mark)

ii) Show that the force due to a magnetic field B that results from a current carrying conductor is given by:

- iii) A point charge of magnitude q = 4.5 nC is moving with a velocity of 3.6 x  $10^7$ m/s parallel to the x-axis along the line y = 3m. Find the magnetic field produced by this charge when the charge is at point where x = -4m and y = 3m. (10 marks)
- iv) The magnetic field of any point in a region around a current has been found to depend on three factors. List the three factors. (3 marks)