AB-INITIO STUDY OF ELECTRONIC AND MECHANICAL STRUCTURE PROPERTIES OF THE SUPERCONDUCTING IRON PNICTIDE $EuFe_2As_2$

OMBOGA KERUBO NAOMY

B.ED SCIENCE (KISII UNIVERSITY)

A THESIS SUBMITTED TO THE BOARD OF POST-GRADUATE STUDIES IN PARTIAL FULLFILLMENT OF THE REQUIREMENTS OF THE DEGREE OF MASTER OF SCIENCE IN PHYSICS IN THE SCHOOL OF PURE AND APPLIED SCIENCES, DEPARTMENT OF PHYSICS, KISII UNIVERSITY

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| Dr. | Calford Oti | eno | | |
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| Depa | rtment of Phy | rsics | | |
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| Sign: | | | Date: | |
| | | | | |
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DEDICATION

This work is dedicated to my family and close friends for their tireless efforts and spiritual, financial and emotional support up to this level. God bless you all.

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ABSTRACT

Europium Diiron Diarsenide is one of the iron pnictide materials that exhibit superconductivity at high critical temperature. As a superconducting material it can be used in the manufacture of Magnetic Resonance Imaging (MRI) machines, design of cables that can be used to transmit electricity without energy losses hence lowering energy transmission costs. Although superconductivity has proven to be such a useful phenomenon, there is limited information available on the mechanical and electronic structure properties of Europium Diiron Diarsenide and most of the few available data is experimental, therefore constraining the use of this material in industry. Therefore, it is from this context that this research sought to investigate these properties, to provide complimentary information on the few available experimental data, so as to improve on the understanding of the materials properties and enhance its applicability in industry as a superconducting material. The aim of this study is to employ theoretical methods through the Density Functional Theory to investigate computationally the mechanical and electronic structure properties, the effect of pressure on these properties and on superconductivity sso as, in combination with the available experimental data, to be able to enhance its applicability in industry. The open source software Quantum Espresso which employs the plane wave and pseudo potentials of the ground state has been used in this study. A study on the mechanical structure property as obtained in the study indicates that the material is ductile and also anisotropic. The material is also mechanically stable. Electronic structure properties showed that the compound was a metal. The study of the effect of pressure on the Fermi energy also showed that the Fermi energy increases as the pressure increases. The Debye temperature also revealed that the compound has a high thermal conductivity. The phonon dispersion study revealed distinct acoustic modes and optical modes.

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LIST OF ABBREVIATION

| DFT | Density Functional Theory |
|-----------------------------------|---|
| PW | Plane Wave |
| ESPRESSO | opEn-Source Package for Research in Electronic Structure, Simulation, |
| | and Optimization |
| LDA | Local Density Approximation |
| LSDA | Local Spin Density Approximation |
| EuFe ₂ As ₂ | Europium Diiron Diarsenide |
| QE | Quantum ESPRESSO |
| E _{cut} | Plane wave cutoff energy |
| eV | Electron volt unit |
| Н | Hamiltonian |
| Fig | Figure |
| SDW | Spin Density Wave |
| SC | Superconductor |
| В | Bulk modulus |
| G | Shear modulus |
| E | Young's modulus |

| CMP | Condensed Matter Physics. |
|-------------|---------------------------------------|
| BME | Birch Munaghan Equation |
| GGA | Generalized Gradient Approximation |
| MRI | Magnetic Resonance Imaging |
| MBSE | Many-body Schrödinger Equation |
| SE | Schrödinger Equation |
| CHPC | Center for High Performance Computing |
| BCS | Bardeen, Cooper and Schrieffer |
| FeAs | Iron Arsenide |
| MP | Materials Project |
| MC | Materials Cloud |
| HF | Hartree Fock |
| K-S | Kohn-Sham |
| H-K | Hohenberg-Kohn |
| $V_{\rm H}$ | Hartree potential |
| Z | Atomic number |
| А | Atomic mass |
| Gpa | Giga Pascal |
| SCF | Self-Consistent Field |
| NSCF | Non Self Consistent Field |

| GRACE | Graphical Advanced Computing and Exploration of data |
|-----------------|---|
| E _{XC} | Exchange and Correlation energy of interacting system |
| PBE | Perdew Burke Ernzerhof |
| PBEGGA | Perdew Burke Ernzerhof Generalized Gradient Approximation |
| К | Kelvin |
| Vext | External potential |
| $ abla^n$ | Charge density variation |
| PDOS | Projected Density of States |
| BS | Band Structure |
| n(r) | Electron charge density |
| ∇ | Gradient operator/ Laplacian operator |
| PP | Pseudo Potential |
| PWSCF | Plane Wave Self Consistent Field |
| ICTP | International Center for Theoretical Physics |
| DFPT | Density Functional Perturbation Theory |
| LAPW | Linearized Augmented Plane Waves |
| FeSC | Iron based superconductors. |

CHAPTER ONE

INTRODUCTION

1.1 Background of the study

There has been increasing interest over the recent past and in the present amongst the science community especially Physicists over the phenomena of superconductivity due to its present and projected advantages and uses. H. Kamerlingh Onnes in 1911was the first to discover the concept of superconductivity, which was later illustrated by Bardeen, Cooper and Schrieffer in 1957 (Si, Yu, & Abrahams, 2016). Superconductivity refers to the total vanishing of electrical resistance to direct current in a material. Resistivity tends to zero while conductivity tends to infinity.

The iron Pnictides in particular have attracted special attention because they are relatively easier to synthesize and they exhibit superconductivity under conditions such as doping or application of external pressure (Miclea *et al.*, 2009). Superconductivity in the iron pnictide family was first discovered in 2008 (Si *et al.*, 2016).

Superconductivity arises when pairs of electrons which have opposite momentum move uniformly and transmit electricity without energy loss. Most power plants burn coal and fossil fuels to produce electricity (Ang & Su, 2016), which releases harmful toxics to the environment. Minimized energy losses due to use of superconducting cables decreases the quantity of electricity that power stations have to produce, hence reducing the quantity of fossil fuels that are burned everyday which benefits the environment by reducing the amount of toxic fumes released by power plants. Energy losses in form of heat are eradicated through the use of superconductors. High temperature superconductivity has been observed in iron Pnictides (Norman, 2008), EuFe₂As₂ being one of them.

Superconductors have other projected uses due to their advantages mentioned above and some of the projected areas of uses are: First, the Rapid Single Flux Quantum integrated circuit receiver that helps to achieve gigahertz frequencies. These high frequencies cannot be easily achieved by the current semiconductors that are used in cell phones due to energy loses so as to make the phones more efficient and reliable (Chen, Rylyakov, Patel, Lukens, & Likharev, 1999). This kind of integrated circuit can be achieved through use of superconducting materials. Secondly, in transport, magnetic trains (Ng, 1995) can be advanced since they are super quick as a result of the huge magnetic fields generated by a superconductor.

Superconducting magnets are already in use in areas such as in hospitals where Magnetic Resonance Imaging machine (MRI) (Green, 2001), which is used in patient diagnosis without performing unnecessary surgery. The Magnetic Resonance Imaging machine produces much better results than the x-ray technique, hence one important use of superconductors today. Magnetic Resonance Imaging machine can be improved as a result of development of cheaper superconducting materials, hence improved access to better health care. The Magnetic Resonance Imaging machine is used to perform 'knife less' surgery and diagnosis on patients suffering from various ailments. Currently, the Magnetic Resonance Imaging machine uses liquid helium for its superconducting properties which is quite expensive. Liquid Helium also undergoes easy evaporation causing losses. Superconductors have resistance being equal to zero and conduction is infinite. The use of superconducting grids to transmit electricity from one place to another would eliminate power loses and minimize extra costs being incurred as a result of resistance experienced in the cables used in transmission grids. The superconducting current is self-sustaining

2

and persists on a conductor for a very long time. Some other areas where superconducting materials are applied include in microwave sensors that employ infrared and in refrigeration where liquid helium is used although having the disadvantage of easy evaporation.

1.2 Superconductivity

Superconductivity is one of the most fascinating concepts of quantum mechanics. It refers to the state of no resistance below a given materials critical temperature. It can be achieved through doping or application of external pressure to a material. Below the critical temperature, the electrical resistivity of a material vanishes completely, therefore, electrons can move without energy dissipation. Actually, in the superconducting state, the resistance goes to zero (Bardeen, Cooper, & Schrieffer, 1957) and conduction to infinity. The onset of superconductivity in a material is as a result of interaction between conduction electrons and lattice vibration. Ginsburg and Landau considered the density of the material changing in space.

The Ginsburg Landau theory was restructured from the concept of London theory to include an effective wave function that can be normalized so that the local density can be obtained (Bardeen *et al.*, 1957). The phenomenon of high temperature superconductivity has been among the most challenging work in the science community, most especially amongst condensed matter physicists (Li, Zhu, Chen, & Ting, 2012).

The BCS theory of superconductivity is extended to the Migdal-Eliashberg theory, which relates the critical temperature to atomic scale properties of materials, in particular, the electronic band structures, phonon dispersions, which properties can be calculated using the Density Functional Theory. The electronic structure of a compound varies with temperature. This is because temperature leads to phonon excitations. The population of phonon would couple with electronic states and renormalize the energy of the electron energy. The zero Kelvin is the ground state of condensed matter. Electron to electron coulomb interaction gives rise to superconductivity in iron Pnictides.

Generally, superconductors are classified basing on the following criterion: the operational theory, the critical temperature, the nature of the material and how they react to a magnetic field. Basing on how they react to a magnetic field, they can be grouped into type one and type two superconductors. Basing on the theory of operation, they can be classified as conventional or unconventional superconductors, and basing on their critical temperature, they can be classified as high temperature superconductors and low temperature superconductors. Also, basing on the makeup material, they can be classified as ceramics, chemical superconductors, organic superconductors and superconducting Pnictides.

Superconductivity is unique in that not all materials that are conductors can exhibit superconductivity. It is not even related to atomic weight and number or electro-negativity. In some rare cases, a superconducting material can be formed from a combination of non-superconducting elements. The BCS theory predicts a correlation between critical temperature, lattice vibration, and average atomic mass. This theory is as a result of the theorem that Cooper put forward, that, the ground state of an electron gas is unstable and there exists a tiny attraction between its particles against the forming of pairs of electrons. In the BCS theory, superconductivity is illustrated at temperatures that are near 0K. Here, the cooper pairs are created which then occupy states but have the same but opposite momentum and opposite spin, basing on the Pauli Exclusion Principle that no two electrons with the same spin can occupy the same state simultaneously. In a scenario where the angular momentum due to orbiting of particles is zero, cooper pairs are generated. Cooper pairs are usually made up of particles that undergo spin $\frac{1}{2}$.

Superconductivity can be classified as conventional superconductivity and unconventional superconductivity. In conventional superconductivity, phonons lead to the generation of pairs of electrons in a process of attraction. This type of superconductors conforms to the BCS theory. Conventional superconductors can be type one or type two. Unconventional superconductors do not align with the BCS theory. The iron Pnictides are generally classified under the unconventional super conductors (Si et al., 2016). High temperature superconductivity is an example of unconventional superconductivity and the critical temperature is in the range of 7K to 100K. The resistant behavior in metals falls considerably in very low temperatures. Reduction in resistance implies much improved electrical conductivity. Initially, there were various speculations amongst scientists as to what would take place in the electrical resistance if the temperature of a material was lowered to 0K. Some of the scientists such as William Kelvin suggested that if the temperature was set to much lower levels, the electrons moving in the conducting material would stop moving completely (as the temperature is lowered to approach zero Kelvin.). Other scientists such as Onnes suggested that the resistance of a very cold wire would disappear. This prompted Onnes to begin searching for answers to this phenomenon. He performed an experiment which included passing direct current through a pure mercury wire while lowering the temperature, at the same time he noted down the resistance as he lowered the temperature. When he lowered the temperature and reached a temperature of 4.2K, the resistance disappeared all of a sudden and the direct current was now flowing freely through the mercury. The 4.2K is the transition temperature for superconductivity and he called this phenomenon superconductivity, hence bringing an end to the various speculations as to what happens to resistance when temperature is decreased. Take for instance, in a conducting material such as copper, electrons in the outer energy level move from one atom to another, hence conducting

electricity from one point to another. However, the behavior of electrons in superconductors is very much different; the electrons move in a much different way. The electrons do not collide or bump with anything as they move through the lattice; therefore they move freely, transmitting electricity at no resistance, as compared to normal conductors where the electrons collide with impurities in the lattice and fly off in different directions, which leads to energy loss as heat. In summary, a superconducting material can be termed as conventional if it can be described using the BCS theory and other theories derived from it, and it is unconventional if it cannot be illustrated by the BCS theory.

The London equations explain superconductivity in a simplified manner as the Ohm's equation explains conductivity. The London equations are as given in Eqs 1.1 and 1.2 below:

$$\nabla \times j = -\frac{n_s e^2}{m} B$$
.....

Where, j is the superconducting current density, E is the electric field, B is the magnetic field, e is the charge of an electron, m is the mass of an electron, n_s is the density of the superconducting carriers.

The basic terms and phenomena in superconductivity include:

- i. The Meissner Effect: Was put across by Walther Meissner and R. Ochsenfeld in 1933, who reported that superconductors have a special aspect of magnetism which includes the excluding of a magnetic field. The magnetic flux is excluded in a superconductor that has undergone cooling of up to below the temperature of transition in a magnetic field, and this concept is termed as the Meissner Effect. However, the Meissner Effect will take place when the field of magnetism is quite small. Superconductivity cannot exist in a large magnetic field. This is because the large field will enter into the material and expel superconductivity, therefore, superconductivity and magnetism cannot exist simultaneously in a material.
- ii. Critical magnetic field: The critical magnetic field is closely related to the concept of critical temperature T_c , the temperature at which the resistance of a material to flow of electrons completely vanishes. Superconductivity will not exist in a material if there exist a magnetic field that is larger than the critical value of magnetism.
- iii. The critical current density: this is the current density above which the superconducting state of a material disappears. The science community is still working hard to come up with a compound that can achieve superconductivity at room temperature, and this may be achieved by the use of the type two unconventional superconductors since they super conduct at fairly higher temperatures as compared to the conventional type one superconductors. Characteristics of materials are classified into two, and this classification depends on the ground state and the excited states. Some examples of ground state properties include the transition of crystals from one structure to another, the elastic constants, the density of charges, magnetic susceptibility and many others. Some

examples of electronic excited state properties include: susceptibility of the Pauli spin, optical properties and many more. The ground state energy dictates the structure and small energy movements of the nuclei. Generally, materials are grouped depending on their electronic ground state since it dictates their nuclei bonding. In physics, there are basically two types of excitations, one type of excitation being through the removal or addition of an electron to the structure and the other excitation being by maintaining the count of electrons. Excitation can be regarded as a perturbation.

Superconductivity in the iron pnictide family of compounds was first discovered in 2008 (Si *et al., 2016*). From the above, one can now come into the conclusion that the study on superconductors is quite important to the science community and the world at large.

1.3 Statement of the Research Problem

In the recent past, there has been growing interest in the science community on the study of the superconductivity phenomena due to its various present advantages and projected future uses in industrial design of various machines. The iron pnictide family of compounds has shown high temperature superconductivity on doping or application of external pressure. Although superconductivity has proven to be such a useful phenomenon, there is limited information available on the mechanical and electronic structure properties of Europium Diiron Diarsenide and most of the few available data is experimental, therefore constraining the use of this material in industry. Therefore, it is from this context that this research seeks to investigate these properties, to provide complimentary information on the few available experimental data, so as to improve on the understanding of the materials properties and enhance its applicability in industry as a superconducting material.

1.4 Objectives

1.4.1 Main Objective

To apply *ab-initio* methods to investigate the electronic properties and mechanical structure of the iron pnictide compound $EuFe_2As_2$

1.4.2 Specific Objectives

- i. To investigate computationally the mechanical structure properties including the Elastic constants, the Bulk modulus, Shear modulus, Young's modulus and the Poisson's ratio of the iron pnictide compound $EuFe_2As_2$.
- ii. To analyze computationally the electronic structure properties of the iron pnictide compound $EuFe_2As_2$.
- iii. To investigate the effect of external pressure on the mechanical and electronic structure properties of the iron pnictide compound $EuFe_2As_2$.
- iv. To study the thermodynamic properties of Phonon Dispersion modes and Debye temperature of the iron pnictide compound $EuFe_2As_2$ in relation to superconductivity.

1.5 Justification for the Study

Europium diiron diarsenide (EuFe₂As₂) is a material that can be important for use in the design of superconducting cables for electricity transmission and the design of motors for ships and turbines. Design of microchips for cheap energy usage is projected to benefit from superconducting materials such as EuFe₂As₂. Although research on this material has been done experimentally, not much has been explored especially on the mechanical properties. Experimental results are available on the electronic structure properties (Adhikary *et al.*, 2013)

but mechanical properties have not yet been explored, hence motivating the study. Computational methods are here used because of low cost and reliability. Computational methods can also be tested in regimes of high pressure and temperature that may not be achieved experimentally. The main aim of this research is to investigate the mechanical and electronic structure properties of Europium diiron diarsenide in relationship to its experimental applicability so as to be able to come up with additional data about the material to enhance and direct its effective use in industry. Since there is limited theoretical data on the iron pnictide EuFe₂As₂, the results obtained here will help future theoretical studies on the material.

CHAPTER TWO

LITERATURE REVIEW

2.0 Related Studies on the Iron Pnictide Compounds, A = (Ba, Ca, Eu, Sr)

By substitution of Europium with sodium or potassium superconductivity was obtained in the pressure was externally, the material material. Also. when applied or doped. superconductivity was achieved. There was a reduction of structural and magnetic phase transition temperature when the compound was doped or pressure applied externally to it, therefore superconductivity surfaces upon adequate suppression of the transition (Terashima et al., 2009) .The iron pnictide compounds are also unique because their phase transition to superconductivity, magnetic and structural properties are closely connected and conceal the key to comprehending the basic properties of the material (Colonna, Profeta, Continenza, & Massidda, 2011). According to (W. O. Uhoya, Tsoi, Vohra, McGuire, & Sefat, 2011), EuFe₂As₂ experiences a phase transition from the tetragonal phase to orthorhombic phase at a pressure of 4.3GPa. This phase was maintained up to a pressure of 11GPa where it transits to a collapsed tetragonal phase, which was maintained up to a pressure of around 35GPa. The conductivity of iron Pnictides shows a highly anisotropic characteristic (Ivanovskii, 2009). Phase transition at low temperature is common in the iron Pnictide family of compounds. Experiments performed at high pressure revealed characteristics which link the electronic and structural properties to the superconducting properties of the compound. (Colonna *et al.*, 2011)

Superconductivity and ferromagnetism co-exist in Europium diiron diarsenide that has been doped with phosphorous (Terashima *et al.*, 2009). The iron spin density and the Europium (

 Eu^{2+}) which orders anti-ferro magnetically makes Europium diiron diarsenide to be outstanding among the 122 iron Pnictide superconducting compounds. The FeAs layers in the compound of Europium diiron diarsenide are seen to be the source of the superconductivity (Miclea *et al.*, 2009).This compound is unique because of the additional magnetic moment of the localized Eu^{2+} given that other 122 compounds undergoes only the Spin Density Wave (SDW) transition. In the iron arsenide layer a square lattice is made by the ions of iron, while the ions or arsenic are situated overhead and underneath the middle of the above mentioned square.

Application of hydrostatic pressure on $EuFe_2As_2$ indicates that the SDW transition was continuously suppressed on pressure application. There is simultaneous occurrence of superconductivity, ferromagnetism and structural phase transition. Superconductivity is achieved on suppression of the magnetism. Application of chemical and physical pressure can be employed to change the properties of this material. Superconductivity transition temperature occurs at 30K at a pressure of 2.8 Giga Pascal (Ni *et al.*, 2008).

Other studies in similar iron Pnictides have been done, though mostly experimental. Barium diiron diarsenide exhibits superconductivity on distorting the structure through application of pressure (Kimber *et al.*, 2009). Superconductivity was achieved at a pressure of 5.5Gpa and temperature of 30.5K.The Iron Arsenide superconducting materials are resistant to disorder. Strontium diiron diarsenide also exhibits similar characteristics of superconductivity. Critical temperatures of up to 38 Kelvin have been previously discovered in the 122 family of iron Pnictides. The space group of EuFe₂As₂ transits from 14/mmm to Fmmm (Nandi *et al.*, 2014).

Studies on Calcium diiron diarsenide have also revealed that it exhibits superconductivity on application of pressure and up to temperatures of 40K (W. Uhoya *et al.*, 2010). Experimental

results on Europium Diiron Diarsenide have also indicated that superconductivity occurs below temperatures of 33 Kelvin (Paulose, Jeevan, Geibel, & Hossain, 2009).

The tetragonal space group of $EuFe_2As_2$ is 14/mmm. On application of pressure increasingly on the material, the length of the *a*-axis increases while the length of the *c*-axis decreases hence compression on the material is anomalous (W. Uhoya *et al.*, 2010). The anomalous compression reaches its highest point at 8GPa and the lattice shows a normal trend as from 10GPa.The compound undergoes a phase transition at $T_0 = 190$ K from the ambient tetragonal crystal structure to the orthorhombic phase (W. Uhoya *et al.*, 2010).

The compound $EuFe_2As_2$ can be grown experimentally using self-flux methods. The experimental values of the lattice parameters are about $a \sim 3.916$ Angstrom, b=a, and $c \sim 12.052$ Angstrom (W. Uhoya *et al.*, 2010). The ratio of the axes c/a exhibits a quick decrease below pressure of 8GPa and a slow decrease above the mentioned pressure of 8GPa (W. Uhoya *et al.*, 2010). This compound EuFe₂As₂ exists as a crystal at room temperature as the ThCr₂Si₂ structure (Tegel *et al.*, 2008). Doping of the iron arsenide superconductors subdues the spin density wave, which is linked to superconductivity (Tegel *et al.*, 2008).

In the ground state, Pnictides show spin density wave. The main differentiating factor between Cuprates (which were initially the major materials under the study of superconductivity), is the behavior of the conducting electrons (Maiti, 2015). In iron Pnictides, the Fe 3d prevails over the electrons near the Fermi level. The *p* character is largely contained in the states near the Fermi level (Maiti, 2015). Upon subduing magnetism in iron Pnictides, there arises superconductivity. The magnetism is subdued by doping with a suitable element or by exerting pressure externally EuFe₂As₂ has unique characteristics .since the Eu²⁺ ions have 4f electrons and the combined

spin of the electrons is $\frac{7}{2}$. The crystal structure of the Europium diiron diarsenide is as shown in Fig. 2.1:



Fig. 2.1: The crystal structure of the Europium diiron diarsenide. (Mahesh & Reddy,

2018)

The Europium atom is at the center, while the iron and arsenic atoms occupy other parts of the crystal structure. This gives it a body centered crystal structure.

The general crystal structure of the AFe₂As₂ iron pnictide compounds is as given in Fig. 2.2:



Fig. 2.2: The general crystal structure of the AFe₂As₂ iron pnictides. Source: (Alireza *et al.*, 2008)

The iron pnictides are usually body centered, as seen from Fig 2.2.

Calculating the band structure shows that Fe 3d orbitals brings about the states especially closeto the Fermi level of the iron pnictide (Li *et al.*, 2012). Superconducting and ferromagnetic

properties co-exist in the iron pnictide $EuFe_2As_2$. To come up with superconductivity at a high temperature; there are two conditions that must be met: First, at the Fermi level, the Density of States should be large. Secondly, the pairing interaction should be strong since this can be connected to fluctuations in magnetism.(Li *et al.*, 2012) A crystal is a repetitive and periodic ordered state of matter. Also, a crystal can be defined as the regular and periodic arrangement of atoms in a material.

Iron Pnictide Superconductors have a high critical temperature of up to 56 Kelvin. The 122 iron Pnictide family has numerous similarities with the cuprate family, similarities which include the structure of the crystal that is layered, and, to achieve superconductivity, carrier doping is carried out (Katase *et al.*, 2011). The difference is that iron Pnitides have the ability to exist in form of a metal or semi metal in the usual state, unlike the cuprates which are antiferromagnetic (Katase *et al.*, 2011).

The superconductivity in iron pnictides is associated with the layered structure. The layer of iron pnictide enhances the current that is superconducting (Deng *et al.*, 2009). Iron pnictide sand chalcogenides, Cooper pairs in superconductors that are iron based do not have any angular momentum and they are unconventional because they have different phases on different bands (Deng *et al.*, 2009). Iron Pnictides are also unique because they have a differentiated degree of correlation which is known as the differentiation of orbitals. This normal state that is correlated is the main source of superconductivity (Deng *et al.*, 2009). The iron based superconductors also experience a phase transition on application of pressure from the tetragonal crystal structure to the orthorhombic crystal structure. Furthermore, the number of electron and hole carriers is the same in the iron based superconductors (Deng *et al.*, 2009) . Compounds based on copper have been previously known to be the only ones with a high critical temperature of superconductivity, higher than 40 Kelvin (Si, Yu, & Abrahams, 2016). An interaction between electrons pairs generates superconductivity in iron based
superconductors (Si *et al.*, 2016). They also have a wide range of electronic structures (Si et al., 2016).

Superconductivity can be achieved through doping, pressure application and also chemical substitution (Deng et al., 2009). Iron pnictides below a temperature of 150 Kelvin are metals (Yin, Haule, & Kotliar, 2011). When magnetism arises, the electronic structure is highly impacted, also, the optical conductivity increases. This is as a result of the Spin Density Wave (SDW) being much more analytical than the Para magnetism state (Yin *et al.*, 2011). The paramagnetic state is solid like at a low temperature. Polarization of spin is large at points where the energy is high, while, polarization of orbitals is large at points in which the energy is low (Yin *et al.*, 2011). There is no Mott transition in iron pnictides (Qazilbash *et al.*, 2009). In the iron-pnictogen layers is where conduction of elecrons takes place. In the iron pnictide family, LaFePO (iron phosphide superconductor) is among the compounds which have high conductivity in the normal state (Qazilbash *et al.*, 2009).

CHAPTER THREE

METHODOLOGY

3.1 Introduction to Density Functional Theory (DFT)

Density Functional Theory (DFT) provides a useful means for computation of the quantum state of particles. The density of a material usually determines the properties of a material. The ground state energy and hence wave function is a functional of the density. The electron density is the expectation or mean of the wave function. The electron density only relies on the variable coordinates x, y and z. Density Functional Theory is a useful technique for the study of materials since it solves directly approximate versions of the Schrödinger equation. The electron density determines the external potential, which in turn determines the wave function. It should be noted that no two different external potentials can have a similar density, That is to say, two different external potentials lead to two different electron densities. The Density Functional Theory is a mathematical theorem and it is exact. The Density Functional Theory attempts to solve the problem of the many body wave functions that arises due to the numerous degrees of freedom as a result of the many electrons and nuclei involved. Material modeling from first principles uses various theoretical and computational techniques which are based on Density Functional Theory or have a relationship with Density Functional Theory. The Density Functional Theory was an idea initially put forward by Thomas and Fermi in 1927, shortly after the introduction of quantum mechanics. This theory was later on developed more by Hohenberg, Kohn and Sham in the mid- sixties, which also led to the introduction of the Local Density Approximation during this period. In Density Functional Theory functionals are used to determine the properties of many electron system and the functionals of electron density are mostly considered.

Density Functional Theory originates from the condensed matter Physics. One of the reasons as to why DFT is advantageous is because it provides a reasonable starting point for ground state energy. Apart from solid state physics, Density Functional Theory can also be used in other areas such as Molecular dynamics. There are several Density Functional Theory codes for simulation and they are able to calculate various properties of a material (Hasnip *et al.*, 2014). Density Functional Theory focuses on the electron density in place of the many-body wave function. Electron density refers to the number of electrons per unit volume at a specific point. The electron density is given in Eqs 3.1 below:

$$(r) = \sum \left(\left(\phi_i \right) r \right)^2 \qquad 3.1$$

Where ϕ_i are the Kohn Sham orbitals of electrons that do not interact (Giustino, 2014). Note: Summing up the electron density over all the space will yield the total electron number, that is to say: $\int (r) = n$, where n is the total number of electrons. Determining the electron density of a given system, just like the wave function, can enable us to determine the properties of the system. Density Functional Theory works on the principle that the total energy is a unique functional of the density of the electrons (Hasnip *et al.*, 2014). Density Functional Theory is a quantum mechanics modeling tool.Properties of crystal systems and structures can be obtained by the use of this theory. Over the years the science community has been adapting the use of Density Functional Theory is not variational and can describe correlation. The Density Functional Theory technique can be used to describe various materials and can be transferred to be used in the study of other classes of materials. The equations employed in theorems such as Kohn and Sham is simple and intuitive. It is easy to share the software: open source software with free download and use are available for the science community to access. Correct results are usually obtained from the computation and when compared with experimental data there is usually a minimal difference between them, making Density Functional Theory reliable. In Density Functional Theory, an assumption is made that there are no electron to electron interactions. Density Functional Theory has enabled computation on materials with very many electrons(up to thousands), which was difficult to achieve with wave function based methods due as a result of numerous number of interactions between electrons and nuclei. This has made computation of large compounds possible (Sholl & Steckel, 2011).

Density Functional Theory is implemented by three means which are: the pseudo potentials, exchange correlation and the plane wave. The basis sets for QUANTUM ESPRESSO are the plane wave basis sets. Plane waves are the set of functions which are put together so as to describe a wave function .They systematically improve basis sets to full or desired level of consistency. When using the plane wave basis, convergence in a system increases with an increase in the number of plane waves (Fiolhais, Nogueira, & Marques, 2003). Some advantages of the Plane wave basis are: It is simple to use, it is orthonormal, it is independent of the atomic positions, it is unbiased and it is easy to control convergence when using them. Plane waves take the form seen in Eqs 3.2 below:

$$(x,t) = A_0 \cos(kx - \omega t + \varphi) \dots 3.2$$

where A_0 - amplitude, k-wave number, ω -angular frequency, φ - phase shift of the wave.

x- point along the x-axis, and A(x, t) –magnitude of disturbance or displacement of the wave.

Plane waves help in calculating the total energy of a system by using the periodicity of the lattice of a given crystal. However, it should be noted that, the higher the number of plane waves, the more difficult it becomes to calculate the total energy of a system (Fiolhais et al., 2003). Plane waves are exact Eigen states and are not biased to any specific atom (Togo & Tanaka, 2015). The advantages of plane wave basis sets include the following: they are not difficult to implement, that is to say, they are simple and easy to use. They also allow convergence to be achieved systematically, and are independent of the positions of the atoms. The disadvantages of the plane wave basis include: it requires very many plane waves to attain a high level of accuracy and it is difficult to achieve convergence for the orbitals that are tight. Pseudo potential is the effective potential which is used as an approximation for the simplified description of complex systems such as the Many Body Schrödinger Equation, MBSE. The valence electrons in an atom influence the properties of the material and are used to classify the material. The pseudo potential replaces the potential and the core electrons which barely determine the properties of the material. Pseudo wave functions take the place of true valence wave functions hence enabling the use of lesser number of plane waves since they are node less. This is because the electron wave functions near the nucleus oscillate rapidly as a result of interaction with the positively charged nucleus, therefore need to be replaced by plane waves of short wavelength which results into large cut-off energy, an issue addressed by the pseudo potential.



 r_c -cut off atomic radius, V-potential, ψ -wave function

Fig. 3.1: General representation of pseudo potential. The real and pseudo wave function at a given cut-off atomic radius are in good agreement, (Togo & Tanaka, 2015) justifying the use of pseud potentials.

Therefore the pseudo potentials represent the real potentials of the system with a high level of accuracy at a certain cut off atomic radius.

Pseudo potentials cater for the core electrons, cover the strong potential of the core electrons and allow correct self-consistent field calculations (Hamann, Schlüter, & Chiang, 1979). As seen from the above diagram, the real and pseudo wave function at a given cut-off atomic radius are in good agreement, (Togo & Tanaka, 2015) justifying the use of pseudo potentials. The cut off radius is used to determine the quality of a given pseudo potential. Pseudo potentials with small cut off radius are realistic and strong, while those with a big cut off radius are unrealistic (Fiolhais *et al.*, 2003).

A good pseudo potential should illustrate correctly the characteristics of valence electrons in numerous different chemical surrounding or it should be transferrable(Fiolhais *et al.*, 2003) When using the pseudo potential approximation, the external potential is the sum of the individual pseudo potential of each atom that is present in the crystal.

The Projector Augmented Wave (PAW) Non Linear pseudo potentials were used in this research (Kresse & Joubert, 1999; Troullier & Martins, 1991). QUANTUM ESPRESSO supports the use of Projector Augmented Wave (PAW), Ultra Soft Pseudo Potentials (USSP), which are Norm Conserving (NC). Norm Conserving pseudo potentials are hard but they maintain the accuracy. Norm Conserving means that the integral of the square of the real all electron wave function should be equal to the integral of the square of the pseudo wave function. Norm Conservation improves on transferability. USSP tremendously decreases the cut off energy, especially for difficult elements. The Ultra Soft Pseudo Potentials can make the pseudo wave functions very soft and also select multiple references of energy. Projector Augmented Wave allows the user to reconstruct the wave function.

The factors one should consider in the selection of pseudo potentials include: the level of accuracy that can be achieved by using it, the transferability of the pseudo potential, relativistic and the semi core inclusions. Over the years, the Density Functional Theory methodology has become more popular in use amongst various scientists in the Physics and Chemistry fields; and lots of Density Functional Theory -based academic papers have been published. Apart from the numerous publications, there also exist several books printed to discuss the fundamentals of Density Functional Theory and related topics (Fiolhais *et al.*, 2003), hence proving its increasing use as seen in the Fig. 3.2 below:



Fig. 3.2: DFT publications over the years up to 2009. The number of publications keeps increasing each year, implying that more scientists are employing this method to perform their research.

The use of DFT over the years has increased over the years as shown in the above figure, this is because it is much cheaper to use in research and provides results which are similar to those produced by experimentalists.

Density Functional Theory is based on two basic theorems which are:

- i. Kohn and Hohenberg theorem
- ii. Kohn and Sham theorem

The Kohn and Hohenberg theorem states that the energy of the ground state of a system is a unique functional of the density of the electron, which in turn relates the ground state energy to the wave function of the ground state (Giustino, 2014). The Kohn and Hohenberg theorem did not define exactly what the functional is, therefore, the Kohn and Sham theorem goes ahead to describe a useful characteristic of the functional: The density of the electron that makes the energy of the overall function minimum is the true density of the electron that corresponds to the solution of the Schrödinger equation; This means that, the electron density that takes the energy of the system to a minimum is the density that provides the solution to the Schrödinger equation, hence the electron density is a unique functional of the total energy of a given system. In the Kohn and Sham theorem, both the kinetic energy and density of electrons are known exactly from the orbitals (Togo & Tanaka, 2015). The Kohn and Sham equations are non-linear therefore they are solved through iterations to achieve self-consistency.

Kohn and Sham came up with a set of valid equations, which, to solve them, the Hartree potential must be defined, and, to do so, the density of electrons should be known. To obtain the density of electrons, the single-electron wave functions should be known; also to obtain the wave functions, the Kohn Sham equations should be solved. This appears like we are moving in a circle!

To solve the above problem, an iterative technique is used whereby:

- i. The starting density of electron on trial is defined (A trial electron density selected.)
- ii. The Kohn Sham equations are solved using the above trial electron density.
- iii. The electron density is calculated as obtained from the Kohn-Sham single particle wave functions.
- iv. The computed density of electron is compared with the density of electrons employed in solving the Kohn-Sham equations. If the above densities are similar, then this is the density of electrons in the ground state, if they are not similar, the trial density of electron should be changed and the procedure repeated from step two.

The iterative technique here leads to a self-consistent solution of the Kohn-Sham equations.

But, to obtain a solution of the Kohn-Sham equation, the exchange correlation functional should be defined, which is a bit complicated to define. However, in the uniform electron gas, this functional has been obtained exactly and it gives a means of using K-S equations.

3.2 The Many-Body Schrödinger equation

Matter consists of electrons and nuclei, hence understanding the properties of materials entail a proper comprehension of the characteristics and behavior of nuclei and electrons. Quantum mechanics is therefore of the most important branches of Physics, since it deals with the study of the characteristics of sub-atomic particles (Fiolhais et al., 2003). Nuclei and electrons interact with each other and there exist two fundamental interactions: one, electrostatic interaction and two, Coulomb interaction. Electrons, especially the valence electrons move at velocities which are much lower as compared to the speed of light and therefore they are non-relativistic (Fiolhais et al., 2003). In quantum mechanics, the nature of atoms, their electrons and nuclei particles is illustrated in details. Understanding the electron and the electronic structure opens up a path to comprehending many more useful properties of materials; hence electrons are of importance in quantum mechanics. Quantization of energy is also studied, the Schrödinger equation forming a basis for these solutions. The Schrödinger equation , $H\psi = E\psi$, where H is the Hamiltonian and E is the energy, is one of the most important equations in quantum mechanics, since its solution yields the ground state energy and ground state wave function which contain useful information about any given crystal structure. The Hamiltonian term consists of both the kinetic and potential energy terms of the electrons and nuclei present in the material. The Schrödinger equation can be time dependent or time independent. In Condensed Matter Physics, the major concern is to obtain a solution to the non-relativistic time independent Schrödinger equation (Togo & Tanaka, 2015).

The Schrödinger equation can also be re-written as in Eqs 3.3 below:

$$H = T_{e} + T_{n} + V_{ee} + V_{en} + V_{nn} - \dots$$

Where, T_e and T_n are the kinetic energies of the electrons and nuclei respectively, V_{ee} describes the electron-electron interaction V_{en} describes the electron-nucleus interaction and V_{nn} describes the nucleus-nucleus interaction.

Solutions to the Schrödinger equation for simple atoms like the hydrogen atom can be obtained since it has a single electron. However, when the electrons increase in number, the Schrödinger equation becomes more complex and a bit complicated to obtain the exact solution, and it's now referred to as the Many-Body Schrödinger Equation. By solving the Many Body Schrödinger Equation, we obtain the ground state wave function hence the ground state energy. The wave function contains important information about the state of particles therefore we can obtain the properties of a material from it. The time independent many body Schrödinger equation is mainly considered in Density Functional Theory. Eqs 3.4 is the time-independent Many Body Schrödinger equation:

The first term on the left hand side of the above equation is the kinetic energy of the nuclei, the second term kinetic energy of electrons, the third and fourth terms are potentials due to nucleinuclei interaction and nuclei to electron interaction respectively. The fifth term is the potential due to electron-electron interaction. In summary, the left hand side represents the Hamiltonian of the system. Due to many electrons and nuclei in the system, it's difficult to get exactly the solution to the system. Though difficult, there are valid approximations that are employed in solving the equation above. To solve the above equation, the scientific community came up with valid approximations. The approximations are as discussed below:

3.3 The Born Oppenheimer Approximation

The electron motion and the nuclei motion in molecules can be made into separate mathematical problems. This approximation focuses on the fact that the nucleus is much more heavier compared to the electron. Therefore, in terms of motion, the nucleus moves at a very slow speed compared to the electron hence it can be considered to be stationary or fixed. This therefore implies that the kinetic energy term of the nucleus in the many-body Schrödinger equation vanishes. This is the Born Oppenheimer approximation. On this approximation, The Many Body Schrödinger Equation is asshown below in Eq 3.5

$$-\sum_{i}^{n} \frac{\hbar^{2}}{2m_{i}} \nabla_{i}^{2} - \sum_{i=1}^{n} \sum_{j=1}^{N} \frac{Z_{j}e}{r_{i}-r_{j}} + \sum_{i=1}^{n} \sum_{q>1}^{n} \frac{e^{2}}{r_{i}-r_{q}} + \sum_{j}^{N} \sum_{p>j}^{N} \frac{z_{j}z_{p}}{R_{j}-R_{p}}) \psi(r_{1}, r_{2} \dots r_{n}) = E\psi(r_{1}, r_{2} \dots r_{n}).$$

$$(3.5)$$

The Born Oppenheimer Approximation is considered to be an adiabatic approximation (Pisana *et al.*, 2007) because there exist no coupling between various electronic surfaces.

3.4 Thomas-Fermi Approximations

This approximation was developed by Thomas and Fermi. To obtain the total energy of a system, the potential energy and kinetic energy are summed as in Eq. 3.6 and below. The kinetic energy of electrons is obtained through the partial varying electron density $\eta(r)$.

| $E = T + U_{e-z} + U_{e-e}$ | |
|-----------------------------|--|
| | |

3.5 Hohenberg-Kohn Approximation

The electron density contains important details about the particle, and the ground state energy is a functional of the density of the electron. The external potential is a functional of the electron density. The theorems address the energy function that Thomas and Fermi were not aware about in their previous discovery.

The theorems are as follows; The external potential (), and hence the total energy is a unique functional of the electron density [(r)], and, a universal function for energy $[E(\eta(r))]$ can be defined in terms of density as in Eq 3.7 :

$$E(\eta(r)) = \int n(r)_{\mathcal{V}_{ext}} dr + F(\eta(r)) \dots 3.7$$

Therefore, according to the theorems, studying the electron density in the DFT can enable one to obtain the energy of a system hence the compound's properties can also be determined.

3.6 Kohn-Sham formulation

A fictitious non-interacting system is constructed such that its density is the same as that of the interacting electrons. The solutions of the Kohn–Sham are single electron wave functions that depend on only three spatial variables. The Kohn-Sham is taken to be exact because it gives a ground state density as that of the actual system. The exact ground state density can be written as the ground state density of a fictitious system of non-interacting particles, expressed as follows in Eq. 3.8:

$$E\eta(r) = E_{k}[\eta(r)] + E_{e-e}[\eta(r)] + U_{ei}\eta(r) + E_{xc}\eta(r) - 3.8$$

Where: $E_k[\eta(r)]$ -Kinetic energy of the electrons, $E_{e-e}[\eta(r)]$ - Electron-electron energy $U_{e-i}[n(r)]$ - Electron-ion interaction potential and $E_{XC}(\eta(r)$ - Exchange correlation energy resulting from Pauli Exclusion Principle (Kohn, 1999)

To solve the Kohn Sham equations, self-consistency must be achieved in the iterative process. The equations are said to be 'simple', because the computational effort required to solve them is much less as compared to the one required to solve the Hartree Fock (Fiolhais *et al.*, 2003). Beingeasy therefore does not imply that they are not difficult or fast to write. Computer codes have been written to solve the Kohn Sham equations for any given system. It should be noted that the Kohn Sham potential depends on the electron density (Fiolhais *et al.*, 2003).

The Kohn Sham technique is the most extensively used technique of calculating the electronic structure in Condensed matter Physics (Fiolhais *et al.*, 2003). The KS method gives the total energy of a system exactly, and leaves the exchange correlation energy to be estimated. This is quite trivial because of the following reasons: First, the total energy of a system takes a huge portion while the exchange correlation energy is just a small portion. Secondly, the total energy dictates the shell structure density oscillations and Friedel types. Lastly, the exchange correlation energy is more suitable for the local and half local estimation (Fiolhais *et al.*, 2003).

3.7 Hartree-Fock (HF) method

DFT and wave function methods are strongly connected. HF is one of the wave function techniques related to the electron density in its working. This approximation method determines the wave function and energy of a given system in a stationary state. The many-electron problem is reduced to single electron problem and hence the single electron problem is solved to obtain the solution for the many electron problems. In this approximation, N-electrons wave function ψ is expressed as a single determinant of N-single particle wave function (*x_i*).

Where (x_i) is the product of (r_i) spatial orbital function and (s) electron spin function expressed in Eq. 3.9 below:

The Hartree-Fock method did not take into account the energy of correlation, which is now the energy accounted for through approximations in Density Functional Theory as the exchange correlation energy through the use of Local Density Approximation and Generalized Gradient Approximation.

The Hartree-Fock method caters for the Pauli Exclusion Principle by writing the wave function as a Slater determinant of single electron wave function and is applicable to the non-degenerate ground states. Non-degenerate in this case means a state with different energy and quantum states. If any two electrons are in the same position at the same time, their determinant goes to zero. However, the Slater determinant above actually exists to cater for this by the using of Pauli Exclusion Principle which states that no two or more electrons can exist in the same quantum state at the same time. There exist two main limitations of Hatree-Fock approximation which includes; one, the nature of the function is not known and secondly, the necessary conditions to be met for a function n(r) to be seen as the most accurate ground state solution are not well characterized. Other approximations such as the LDA+U are also present, the choice of the correlation function depending on the type of material you are working on and what exactly you need to achieve.

3.8 Exchange Correlation

The exchange correlation energy contains all the quantum effects in a given system and is given as in Eq. 3.10 below:

Where, E_X is the exchange energy between similar spin electrons and E_C is the correlation energy between electrons with different spin. The Exchange correlation also refers to the difference between the real kinetic energy and the Kohn Sham kinetic energy. The exchange correlation energy E_{XC} is usually a small fraction of the total energy of a given atom or system, but it greatly dictates the chemical bonding and other useful aspects such as the energy of atomization; therefore correct approximation of this term is essential in the DFT scheme (Fiolhais *et al.*, 2003). The exchange correlation functional is independent of external potential and is universal. In cases where the density of charges is slowly changing/ where the charge density is variable, GGA is much better than LDA although not for all systems (Togo & Tanaka, 2015). To obtain the exchange correlation energy, the Local Density Approximation and Generalized Gradient Approximation, Meta Generalized Gradient Approximation, and Hybrid functionals can be used. But, before addressing the exchange correlation functionals, it is important to hint about the uniform electron gas due to its various advantages to the generation of functionals as will be mentioned below:

The uniform electron gas.

The uniform electron gas is also known as the Jellium. It postulates that the electron density is constant over all space. Near the surfaces of materials, the electron density varies in an oscillatory way (Lang, 1969; Lang & Kohn, 1971, 1973). The most simplified systems play an important role in science. For instance, the study of the hydrogen atom is very important in quantum and atomic Physics, and the uniform electron gas is quite important in solid state Physics and Density Functional Theory. Since the electron density is constant over all space in the uniform electron gas, it implies that the number of electrons is infinite. In the Density Functional Theory scheme, the uniform electron gas is applied in the construction of the Local Density Approximation, which is the 'mother' of all the other approximations of exchange correlation energy. Using the quantum Monte Carlo computations of the uniform electron gas, correct values of the density of correlation energy have been acquired for numerous values of electron density, and these values have been employed in the construction of the half empirical correlation function (Ceperley & Alder, 1980; Perdew, McMullen, & Zunger, 1981).

3.8.1 The Local Density Approximation

This is one of the easiest approximations and all the other approximations are based on it. It has given reliable predictions of the frequency of vibration, stability of phases and moduli of numerous compounds hence its use in some cases. The Local Density Approximation uses the density of the electrons to determine the exchange correlation energy (Becke, 1988) and is expressed in Eq. 3.11

below:

The Local Density Approximation over binds, that is it over compresses the system, therefore when one uses it they obtain results that are of lower figure when compared to experimental values.

The Local Density Approximation is quite economical computationally in the estimation of the exchange correlation energy but however, it overestimates the binding energy, hence the use of the Generalized Gradient Approximation (Neyman, Pacchioni, & Rösch, 1996).

3.8.2 The Generalized Gradient Approximation

The Generalized Gradient Approximation originates from the Local Density Approximation and uses the spatial variation of the electrons to determine the exchange correlation energy and it is expressed in Eq 3.12:

The Generalized Gradient Approximation uses both the density of electron and gradient of the electron density. The Generalized Gradient Approximation is a Perdew, Burke and Ernzerhof (PBE) functional.

It is advisable that when you are working with the GGA, use a pseudo potential that has been generated by the Generalized Gradient Approximation, that is to say, the pseudo potential and the functional should be the same (Fiolhais et al., 2003). The Generalized Gradient Approximation functional is size consistent (Fiolhais et al., 2003). Note: for two separate sub systems of energies E_1 and E_2 , and densities $n(r_1)$ and $n(r_2)$, the total energy E of the system is the sum of the two individual energies, that is to say, $E = E_1 + E_2$ and the density of the system is the sum of the two individual densities i.e., $n(r) = n(r_1) + n(r_2)$ (Fiolhais *et al.*, 2003). Approximations that satisfy the above condition are said to be size consistent. The Generalized Gradient Approximation, unlike the LDA, under binds, that is, when one uses it, the results obtained are of a higher figure when compared to experimental figures. For example, when comparing the Generalized Gradient Approximation optimized values of the lattice parameters with experimental lattice parameter values, the Generalized Gradient Approximation values are seen to be a bit higher than experimental values, simply because the Generalized Gradient Approximation under binds. The Generalized Gradient Approximation generates bigger bond lengths, the LDA does an underestimation of the equilibrium lattice parameter and the Generalized Gradient Approximation over estimates the equilibrium lattice parameter (Fiolhais et al., 2003). One of the most famous Generalized Gradient Approximation is the PBE and BLYP. In this study, the PBE (Perdew, Burke and Ernzerhof) functional of the Generalized Gradient Approximation was used because of the nature of the compound. The Generalized Gradient Approximation may look as the grand solution for the exchange correlation energy, though this is not the case. The density of the core in an atom is quite important since it dictates the overall density of the material except for the very light atoms.

This therefore implies that in large gradients, the Generalized Gradient Approximation gives a better description of the density of the core. The functional one chooses depends on what the individual intends to achieve.

The Generalized Gradient Approximation cannot work for non-single Slater determinants and when the non-interacting energies are nearly degenerate. It also does not capture a diffusing long range tail in a system that is extended (Fiolhais *et al.*, 2003). The Generalized Gradient Approximation has the disadvantage of under estimating the band gap when its results are compared to results from experiments. In summary, the Generalized Gradient Approximation is a better exchange correlation approximation for numerous systems than the LDA and gives a one to three percent range of error. It also gives a correction of the over binding element of the Local Density Approximation.

In this research the open source software Quantum Espresso which is a full *ab-initio* package for performing the electronic structure properties, energy, and mechanical property calculations was used. Take for instance the concept of the Jacob's ladder. At the bottom is the LDA, then the GGA above it and other hybrid functionals as you go up. The ladder leads us to the 'heaven' of chemical accuracy, therefore implying that the Generalized Gradient Approximation is more advanced than the LDA, though more painful and more expensive to work with in terms of computation resources and time. The Generalized Gradient Approximation corrects the Local Density Approximation to obtain results that are much more similar to experimental findings (Fiolhais *et al.*, 2003).

The constant 'a' can be obtained through a theoretical estimation as $a\sim 1/4$ for the case of molecules (Fiolhais *et al.*, 2003). Hybrid functionals are considered to be the most correct functionals of the density that are used in quantum computations.

The Jacob's ladder (Fiolhais *etal.*, 2003) of approximation of the functionals of density stretches from the 'Hartree world' to the 'heaven' of chemical accuracy (Janesko, 2013). The ladder has got five steps as explained below, starting from the bottom (Janesko, 2013).

- i. Local spin density approximation (LSDA), is the 'parent' of the other approximations. It uses the spin up density of electrons and spin down density of electrons as its ingredients.
- ii. The Generalized Gradient Approximation (GGA), it includes the gradient of the electron density in its operations.
- The Meta Generalized Gradient Approximation, it includes the derivatives of the gradient of electron density
- iv. The hyper Generalized Gradient Approximation, it includes the exact exchange energy density. The hybrid functionals are actually classified under the hyper GGA.
- v. Exx with partial exact correlation (Fiolhais *et al.*, 2003)

Inbuilt in Quantum Espresso is the Plane-Wave Self-Consistent Field (PWSCF) code which is employed to do the calculation of the total energy in a system. PWSCF employs norm conserving Pseudo Potential (PP) and Ultra-Soft Pseudo Potential (USPP). Norm conserving pseudo potentials enable elimination of core electrons from *ab*- initio calculations, which makes the computation quicker. USSP solve the problem of strongly fluctuating pseudo potentials near the nucleus, hence making the study of elements in the row and transition elements easier to study. However, this leads to loss of details on the wave functions of the electrons in the nuclei vicinity, an issue overcome with the use of Projector Augmented Wave (PAW) method. Quantum Espresso is also inbuilt in the supercomputer at the CHPC South Africa where the calculations were done. One can run self- consistent calculations in QE to obtain the total energy of the system, the Fermi energy and much more valuable theoretically computed data. Self-consistent calculations are performed and once convergence is achieved, more calculations such as the Density of States, mechanical properties and band structure are done on the system. The flow diagram for the total energy calculation in the Density Functional Theory is as shown in Fig. 3.3. Upon the initial guess on our system, it indicated convergence hence other calculations followed after.



Fig. 3.3: The Density Functional Theory flow chart as adapted from (Hao, Moran, Liu, & Olson, 2003).

After the electron density and total energy have been evaluated, if convergence is achieved, calculation proceeds to provide output quantities such as forces and energies, if convergence is not achieved, the initial guess is reset and the steps repeated until the system converges.

The above procedures are followed systematically, if the system converges after a given limit of iterations then we proceed to further calculations, if the system does not converge, the process is repeated to achieve convergence. Convergence is a state in which the system has the lowest energy, hence at this point it is considered to be at its most stable state. It is achieved through the system performing several iterations on the compound, to attain the lowest energy of the system. This prevents unnecessary errors in the results obtained in the study. There is a great correlation between the critical temperature of a compound and the electronic band structure; hence, studying the electronic structure properties of the compound will generate useful data, since at a given critical temperature; there will be an onset of superconductivity in the material (Adhikary et al., 2013). The study of Density of States (DOS) and Partial Density of State (PDOS) will also provide additional valuable information on the electronic structure of the compound. The band structure diagram can reveal the states and energy levels available for occupation. The two dimensional diagram of the band structure can greatly assist in classifying a compound as a metal, semi-metal or insulator. It can also help to determine whether a material has a direct or indirect bad gap, basing on the position of the maximum band line in the valence band and minimum position of band line in the conduction band. Also, studying theoretically the mechanical properties of the material and establishing the Young's modulus, shear modulus, bulk modulus and Poisson's ratio and application of varying pressure on the material will help us establish and analyze how the material responds to mechanical stresses, and come up with a critical temperature at which indicates the onset of superconductivity of the material. For instance, studying the Poisson's ratio of the compound as one of the mechanical properties will

help us determine whether the compound is ductile or brittle, using the Frantserich (Frantsevich, Voronov, & Bokuta, 1983) technique. For a Poisson ratio less than 0.26 the material is brittle and for that greater than 0.26 the material is ductile.

The two main theorems on which DFT is based are applicable only to the ground state; this proves to be a limitation in the study of excited states. Though predictions of the excited states may be made from the ground state, they may not be very accurate. Also, in the case of weak vander Waal forces, DFT computations may provide results that are incorrect (Sholl & Steckel, 2011). Finally, when dealing with a system that has a large number of atoms, such as hundreds or thousands of atoms, it becomes computationally expensive in terms of time and resources required to perform computation (Sholl & Steckel, 2011). In summary, the basic model of solid state consists of Plane Waves, Pseudo Potentials and the Kohn Sham equations (Fiolhais *et al.*, 2003).

Crystal Structure

A crystal structure is composed of a Bravais lattice and a basis. A Bravais lattice is a set of points which are ordered in such a way that they look exactly alike when one views them from whatever position. Bravais lattice is the most sophisticated variety of lattice, in which case, a lattice refers to an array of points in which a similar pattern is repeated; such that if one viewed the points from any direction, they would look exactly the same therefore it would be difficult to differentiate them. Since lattices are formed through repetition of small units, structures can therefore be studied through studying just a small unit or region instead of the whole structure. The small unit or region is known as a primitive cell.

The inverse of the volume of the primitive cell gives the density of the material. The study of the structure of a crystal is quite important since in-depth computation of mechanical and electronic structure properties relies on knowledge of the positions of the individual atoms. Lattice can either be monoatomic lattices which are made up of atoms of one element or diatomic lattices. Compounds consist of two or more elements therefore cannot be classified as Bravais lattices, but as lattices with a basis. Lattices can be categorized depending on their symmetries and for the seven crystal systems; there are 14 Bravais lattices Crystal structures that are also made up of a unit cell.

The Bulk modulus is obtained using the Eqs 3.14, 3.15 and 3.16 below

$$B_{R} = \frac{C}{M}$$

$$c^{2} = (c_{11} + c_{12})_{33} - 2c_{13}^{2}$$

$$(3.15)$$

$$M = C_{11} + C_{12} + C_{33} + 4C_{13}$$

The Shear modulus is obtained using Eqs 3.17, 3.18 and 3.19 below:

$$G = \frac{G_V + G_R}{2} \qquad3.19$$

The Young's modulus E and Poisson's ratio V were obtained respectively using the Eqs 3.20 and 3.21:

The word phonon originates from the Greek language and it means sound, since phonons generate sound. The idea of phonons was introduced by a physicist from Soviet, known as Igor Tamm. The study of phonons assists in understanding properties of materials such as thermal and electrical conductivity. It helps us to quantize the energy of vibration. A phonon refers to a kind of lattice vibration in a crystal, where the particles vibrate at the same single frequency (Simon, 2013). Phonons quantize the energy of vibration. From the phonon dispersion calculation, one can be able to calculate the critical temperature of the material in question. A dispersion relation refers to the relationship between the frequency of vibration and the wave vector and this relationship is given as in Eq 3.22 below:

| $\omega = v(k)$ | | 2 7 | 2 |
|-----------------|---|-------|----|
| | • | 1. /. | 1. |

Where, k - wave vector, - frequency of vibration and v - velocity of sound. (Simon, 2013) (Yu & Cardona, 1996). Phonons are assumed to have momentum (Meyers & Myers, 1997). Past studies have predicted that phonons may have some mass, and since they exhibit some movement, they therefore have momentum (Nicolis & Penco, 2018). There are two branches in phonon dispersion relation: the acoustic mode which is the lower mode and the optical mode, which is the upper mode (Misra, 2011). The acoustic mode refers to the in phase vibration mode while the optical mode refers to the out of phase vibration. The optical phonons get their name from the fact that they get excited by the radiation of infra-red in crystals that are ionic (Mahan, 2011). There are two types of phonon calculation methods: the frozen phonon method and the Density Functional Perturbation. Theory as implemented in PWSCF using ph.x. QE uses the DFPT to do the phonon calculation. DFPT is fast and reliable but has got some limitations such as it does not work for hybrid functionals.

The finite differences method cannot calculate the dielectric tensor or effective charges. The frozen phonons are computed for atoms at known positions. It is the computation of total energy as a function of the position where the atoms are located. For the case of Density Functional Theory phonons, big super cells are required and it takes a lot of time to do the calculation. However, this method can accurately do the calculation of the matrix of the force constant through displacement of the atoms.

The frozen phonon method is much faster and cheap in terms of computation as compared to the linear response technique that uses the Density Functional Perturbation Theory to perform calculation of the forces. This method however has the following setbacks: big super cells are required to correctly do the calculation of the matrix of the force constant. Also, the displacement of a single atom in the unit cell generates forces not only on all the atoms in the unit cell but also on the repeated image of atoms. Valence electrons, unlike the core electrons, are quite useful in the formation of bonds. The valence electrons are the ones that undergo ionization and are the electrons that conduct electricity in materials since they are not strongly attracted to the nucleus as the core electrons. As a result of this, the frozen core approximation method does away with the nucleus and core electrons and works with the valence electrons since they are the most active. This results to reduced number of wave functions.

Other advantages of frozen core approximation method include: there is a reduction in the number of plane waves required, therefore the computation is a lot quicker, and the researcher can work with many more electrons. The effect of relativity is removed from the system since this problem is brought about by the core electrons. The pseudo potentials produce a very little percentage of errors in their working.

CHAPTER FOUR

RESULTS AND DISCUSSION

4.1 Optimization

In this section, we report the various results obtained from the theoretical computation. The open source computer code Quantum Espresso, which incorporates the Density Functional Theory (DFT), Pseudo Potentials (PP) and the Plane Wave (PW) was used to perform calculations from first principles. Projector-Augmented Wave (PAW) Pseudo Potentials were used in these calculations. There are three types of atoms in the crystal, namely: Europium, Iron and Arsenide. The number of atoms in unit cell considered in these calculations is five; one Europium, two iron, and two arsenic atoms. Optimization of the k-points, lattice parameters and cut-off kinetic energy were carried out and the system was run to convergence. Optimization details and graphs are reported in details. The first step of the computation was to make an input file for the calculations. In our study, we used the Plane Wave method to investigate the electronic and mechanical structure properties of the compound from first principles, using the open source computer code Quantum-Espresso (Giannozzi et al., 2009). Self -Consistent Calculations were run to obtain the total and Fermi energy of the system, which are useful parameters in describing the electronic structure properties of the compound (West, Sun, & Zhang, 2012). The input files were designed such that the mechanical properties including the Bulk, Shear and Young moduli, and Poisson ratio were obtained. Quantum Espresso supports the use of Projector-Augmented Wave (PAW), Ultra Soft Pseudo Potentials (USPP), which are Norm Conserving. Norm Conserving Pseudo Potentials are well normalized, a feature useful for an accurate description of bonding in the compound (Hamann, 1989; Hamann et al., 1979).

PAW Non Linear Correction Pseudo Potentials were used in these calculations (Dalgarno, Bottcher, & Victor, 1970; Garrity, Bennett, Rabe, & Vanderbilt, 2014; Troullier & Martins, 1991). Before running the Self-Consistent Calculations, the Variable Cell relax (VC-relax)calculation was performed to obtain relaxed atomic positions and then optimization of cell dimensions, K-points, and the kinetic energy cut off(which was set at 45 Ry) was also done so as to obtain a relaxed crystal structure, to ensure that the ground state crystal structure is obtained and that the results are free from stress (Lund, Orendt, Pagola, Ferraro, & Facelli, 2013; Wales & Scheraga, 1999; Yang *et al.*, 2009). The initial k-point sampling was done using $2\pi/a$ where a is the lattice parameter (W. Uhoya et al., 2010). Optimization of the k-points yielded the converged K-points, convergence ensuring a stress and strain free system. Sampling on the Brillouin zone was done using the Monkhost scheme and the mesh used was 8x8x6. Exchange correlation was computed by employing the Generalized Gradient Approximation as put forward by Perdew, Burke and Ernzerhof. Plane wave basis were used as a basis set for optimization of the lattice parameters, k-points and cut off kinetic energy so as to obtain converged total energy. Calculations were performed in the quenched paramagnetic state, implying that the polarization of the spin is not permitted on the Fe ions in the computation (Li et al., 2012). The Density Functional Theory which focuses on the electron density to study the properties of a many electron body system was employed. Experimental cell dimensions were used in the input file before optimization. Before optimization was carried out, the variable cell relax calculation was done to obtain relaxed atomic positions, which were then used to perform optimization on the compound. The optimization curves for the iron pnictide EuFe₂As₂ are as shown in Fig. 4.1:



Fig. 4.1: Optimization curves for the kinetic energy cutoff (Fig4.1(a)) and k-points(Fig 4.1(b)). Both parameters exhibit convergence at ~ 45 Ry and ~4 Bohr respectively. K- Point sampling done using $\frac{2\pi}{a}$, *a* being the lattice parameter.. The converged k-point values are in good agreement with the experimental values (W. Uhoya *et al.*, 2010)

So as to obtain accurate results, one must select the values above the obtained cut-off energy. However, cut-off energies that are very high are not good because they increase the cost of computation yet the results obtained from the computation are not of improved accuracy. Therefore, the energy should be as low as possible. Plane waves are a basis set: a set of functions that you join to describe a wave function. The more the plane waves, the better the description of the wave function therefore the cut off energy tells us about the cut off on the number of plane waves that are to be used to represent a wave function. K-points describe the different energy levels in the compound. They are the sampling points in the region nearest to the origin, in the first Brillouin zone. Optimization of cell dimensions was done and below in Fig. 4.2 a and b is the converged graphs for the lattice parameters.



Fig. 4.2: The optimization curves for cell dimensions; Fig 4.2a converges at approximately 8 Bohr while Fig 4.2b convergence at approximately 4.5 Bohr. These values correlate with the experimental values of 7.4 Bohr and 5 Bohr respectively (W. Uhoya *et al.*,2010).

After variable cell relax calculation (to obtain relaxed atomic positions of the crystal and optimization of cut-off energy and cell dimensions one and three, the crystal structure of the compound is as in figure 4.3:

4.2 Structural properties

The structure of a crystal dictates its mechanical properties and the electron structure dictates the optical and electrical properties (Fiolhais *et al.*, 2003).

Fig. 4.3 is the crystal structure of EuFe₂As_{2:}



Fig. 4.3: The optimized crystal structure of EuFe₂As₂ as visualized using a Quantum Espresso package Xcrysden.

A body centered structure is portrayed as seen in Fig. 4.3 above. The Europium atom is located at the center, giving it the mentioned structure of Body Centered Tetragonal, with space group 14/mmm. We were more interested in the tetragonal crystal system since the compound we were researching on was of a tetragonal structure. For the case of tetragonal structures, the base of the compound is of a cubic shape, that is why the lattice parameter a is equal to lattice parameter b as seen in the above figure. The tetragonal system is made by stretching a cube's four sides into a rectangular shape.

The structural properties as obtained from computation and their comparison with experimental properties are as shown in the table 4.1.

Table 4.1

Comparison of the experimental and calculated structural values

| Parameter | This work | Experimental | Reference |
|---------------------|-----------|--------------|--------------------------------|
| $a_0=b_0$ (ang) | 3.991 | 3.989 | (W. Uhoya <i>et al.,</i> 2010) |
| $c_0(\mathrm{ang})$ | 10.846 | 10.738 | (W. Uhoya <i>et al.,</i> 2010) |

From table 4.1 above, it is realized that optimized and experimental lattice parameters are in good agreement, which shows that Density Functional Theory reliable (Ali, Rahman, & Rahaman, 2019). However, there is a slight deviation in the lattice parameters since optimized lattice parameters are temperature dependent and also due to the GGA rule.

4.3 Mechanical Properties

Mechanical properties such as elastic properties guide in understanding more about the nature of the force in the crystal. The elastic constants c_{ij} of the compound were computed at T=0K and P=0GPa. There exist six elastic constants in the body centered tetragonal structures (Ali et al., 2019), and they are as recorded in table two.

Table 4.2

| C _{ij} | Value (GPa) |
|-----------------|-------------|
| C ₁₁ | 531.61 |
| C ₁₂ | 284.81 |
| C ₁₃ | 253.34 |
| C ₃₃ | 505.73 |
| C44 | 141.31 |
| C ₆₆ | 225.69 |
| | |

Given the Born-Huang criteria (Piskunov, Heifets, Eglitis, & Borstel, 2004) shown below, a stable tetragonal structure should satisfy the criteria in Eqs 4.1, 4.2, 4.3, and 4.4:

| • <i>C</i> _{<i>ii</i>} | 0(i = 1,3,4,6)4. | 1 |
|---------------------------------|------------------|---|
|---------------------------------|------------------|---|

The values reported in the above table are all positive and satisfy all the above four criteria, hence proving that this tetragonal compound is stable. The above values of elastic constants have been reported for the first time and there are no experimental data to compare with. It is therefore left for experimental work to compute these values. The Bulk, Shear and Young's modulus are

obtained using the Voigt-Reuss Hill Approximation method. Table 4.3 below shows the obtained Bulk, Shear and Young's modulus, and the Poisson's ratio

Table 4.3

Bulk, Shear and Young's moduli, and the Poisson's ratio of Europium diiron diarsenide at zero pressure.

| | Voigt | Reuss | Voigt-Reuss-hill |
|------------------|---------------|---------------|------------------|
| Property | Approximation | Approximation | Average |
| Bulk modulus (B) | 346.939Gpa | 346.352Gpa | 346.646GPa |
| Young modulus(E) | 375.378Gpa | 350.224Gpa | 362.801GPa |
| Shear modulus(G) | 142.224Gpa | 131.518Gpa | 136.871GPa |
| Poisson ratio(n) | 0.31967 | 0.33147 | 0.3254 |

A large bulk modulus indicates that the material is relatively hard, but less hard than diamond whose bulk modulus is ~440Gpa. Pugh's ratio $-\frac{B}{G}$ (Pugh, 1954) indicates that: $\frac{B}{G} > 1.75$ for ductile materials

 $\frac{B}{C}$ < 1.75 for brittle materials

Calculating the $\frac{B}{G}$ value from the above table gives a value of 2.53, implying that the compound under study is ductile.

Using the Frantserich method, ductile and brittle materials are classified on the basis of their Poisson's ratio. The value v~0.26, indicates the border of ductility and brittleness.
If v > 0.26, the material is ductile

If v<0.26, the material is brittle. Since v>0.26, as seen from the Table 4.3 above, this further proves that the compound is indeed ductile.

When the Poisson's ratio is in the range 0.25-0.5, implying that the forces present in the compound are central. The anisotropic character was also calculated using Eq 4.5 below.

$$A^{u} = \frac{5G^{v}}{G_{R}} + \frac{B_{v}}{B_{R}} - 6$$

Where, if $A^{U} = 0$, compound is totally isotropic.

Also, considering the lattice parameters x, y and z, x is equal to y but they are both not equal to

z, hence the compound is anisotropic. In this case, the material is anisotropic with anisotropic value of 0.408. The Bulk, Shear and Young's moduli values increased upon application of increasing pressure on the compound. For instance the Poisson's ratio, Bulk modulus, Shear modulus and Young's modulus at a pressure of 1GPa were 0.36100, 1196.9GPa, 326.6GPa and 889.0GPa respectively, showing a progressive increase up to 1GPa. Temperature and pressure are related by the equation of state, which is one of the most basic equations in condensed matter physics. At a particular temperature and pressure, the stable structure of the compound dictates other characteristics of the material. The energy at a temperature of zero is an important value in ab initio calculations. In theoretical studies, the volume of the system can be varied, and this is quite helpful because the results can be compared directly with experimental values. For a crystal structure to be considered stable at an unchanging pressure and temperature of zero temperature, our result compared well to a value of 0.302 for other families of Pnictides(Parvin & Naqib,

2019), the difference may be as a result of varying atoms present in the two compounds and a slight difference in the crystal structure. This value further confirmed that EuFe₂As₂ is a stable and metallic (Gercek, 2007; Park, 1987). Other Pnictides such as SrFe₂As₂ have a Poisson's ratio of ~0.48 upon application of pressure (Shein & Ivanovskii, 2008), which causes the lattice parameters to change. The Bulk modulus, Shear modulus, and Young's modulus were found to be ~346Gpa, ~136Gpa and ~362Gpa respectively, implying that the material is hard since the moduli are greater than 200GPa (Shein & Ivanovskii, 2008). The Voigt and Reuss values for the Bulk, Shear and Young moduli values are similar to each other hence they are averagely valid. However, there are scanty report on the structural properties (Ceder & Persson, 2010) of the The study of elasticity dates back to Galileo and other 17th iron Pnictide EuFe2As2. century scientists. The fundamental physics of elastic constants was introduced in 1660 by Hooke (Rychlewski, 1984). Elastic constants are derivatives of free energy (Parrinello & Rahman, 1982) and they are highly linked to the thermodynamic characteristics of the system such as Debye temperature and specific heat. Elastic constants are important in the determination of phase, superconducting and structural transitions (Parrinello & Rahman, 1982). Solids that are amorphous contain isotropic elastic characteristics and crystals that are unit and have anisotropic elastic characteristics (Rychlewski, 1984) as proved above by the elastic constants of this iron pnictide. Solids that are isotropic can be elastically compressed and sheared. The coordination number is highly linked to the elastic properties of a given structure. There is decreased elasticityin group VI elements that are tetrahedral.

4.4 Electronic structure properties

In this section, we report on the calculations of the electronic structure properties which included the band structure calculation, Density of States and Partial Density of States. Europium Diiron Diarsenide in this case belongs to the 14/mmm space group, therefore the following high symmetry points in the Brillion zone were used $\Gamma(0,0,0)$, Z(0,1/2,0) B(0,0,1/2), Y(1/2,0,0), C(1/2,1/2,0), D(0,1/2,1/2), A(-1/2,0,1/2), E(-1/2,1/2,1/2). There is a band gap of 0.0eV, which is in agreement with other theoretical studies on the compound (Jain *et al.*, 2013)

The density of states curve for the compound was obtained as shown in Fig. 4.4 below.



Fig. 4.4: The Density of States at zero pressure. There are two curves, separated by a superconducting gap of ~4.5eV, which is in close agreement with the results of other iron Pnictides such as BaFe₂As₂ (Ivanovskii, 2009) which yield coulomb parameters of ~4eV (Maier, Graser, Scalapino, & Hirschfeld, 2009); (Yang *et al.*, 2009). It is within this gap that there exists the superconducting state of the compound (Ashcroft & Mermin, 2005).

The Density of State of this study is in good agreement with previous experimental studies on the material as done by (Nandi et al., 2014). Also, around the Fermi energy of the material, (8.5eV), the density of states is large hence proving that the material can exhibit superconductivity properties (Li *et al.*, 2012). High Density of States at a given level of energy implies that there are numerous states available for occupation. The DOS above is continuous meaning this is not an isolated system. As seen in Fig. 4.4 above, there is a high Density of States around 10, given that the Fermi energy is also around this region. Usually, around the Fermi energy, there are many states available for occupation. Near the Fermi level, the states originate from the 3d Fe orbitals (Fiolhais et al., 2003). The Partial Density of States shows Europium and Iron atoms to be the major contributors to the projecting states. Other minor curves are left out in the illustration since their contribution to the Partial Density of States is minimal. The density of states of other Pnictides shows similar gaps (Parvin & Naqib, 2019). The Density Of States with the long and sharp peaks are between energies of $\sim 7.8 \text{eV}$ and $\sim 10.2 \text{eV}$, and they represent the core electrons that have a minimal contribution to determining the properties of the electrons since they are considered to be chemically inert (Kahn, Baybutt, & Truhlar, 1976). The Density of States between the peaks is zero since states do not exist there as seen above in figure 4.4. A Kondo-like peak is as shown above, in agreement with results from similar iron Pnictides which show similar peaks (Yang et al., 2009). Similar pnictide such as BaCa2As2 also exhibits a sizeable gap far from the Gamma-X high symmetry line(Yi et al., 2009), similar to the one present in the band structure and Density of States. The band structure is as shown in Fig. 4.5:



Fig. 4.5: The band structure of Europium diiron diarsenide at zero pressure(fig 4.5(a)), and the combination of band structure and density of states(fig 4.5(b)): The high symmetry points include GM, Z, B, Y, C, D, A, E.

From Fig. 4.5 there exists no band gap in the material as seen from the graph above, similar to previous results from studies on the pnictide (Ceder & Persson, 2010), hence the material is a conductor. The Density of States and Band structure of the compound show very close similarity as seen above. The zero binding energy and Fermi level correspond, in agreement with previous studies on the material (Paramanik, Das, Prasad, & Hossain, 2013). There is no band gap so the compound is metallic, suggesting that it might be a superconductor, which is actually the proven fact from previous studies. The Fermi energy is above the highest occupied energy level, hence the compound is metallic. There also exists a clear distinction between the valence bands and conduction bands.

The Density of States and band structure were then calculated at various pressures, ranging from 0.2Gpa to 1Gpa. We plotted the results and the graphs are as seen in Fig. 4.6 below:





Fig. 4.6: The Density of States at 0.2Gpa and 1GPa

The range 0.2-1GPa was selected because past studies on the material indicate that the onset of superconductivity is from around 1-2.5GPa(Alireza *et al.*, 2008; Miclea *et al.*, 2009; Terashima *et al.*, 2009; W. Uhoya *et al.*, 2010), and the study sought to understand the properties of the material before it attained its superconducting state. The other range of 5GPa-35GPa was selected as a result of past experimental high pressure studies that went up to high pressures such as one reported by Uhoya (W. O. Uhoya *et al.*, 2011). The band structure calculations show similar structure to that of the density of states. The Fermi energy versus pressure was also plotted at both low and high pressure. The low and high pressure plots are as shown in Fig. 4.7 below:



Fig. 4.7: Graphs of Fermi energy against pressure from 0.2-0.8Gpa and from 5-35GPa. The Fermi energy increases with an increase in pressure up to 0.8GPa. This indicates that the population of charge carries with respect to density of states increases hence more electrons are made available for electrical conductivity, hence enhancing electrical conductivity in the compound

A graph of total energy of the system against pressure was plotted and it took the shape shown in Fig. 4.8 below





The final enthalpy of the system against pressure is also plotted: first, from a pressure of 0.2-1GPa and second from 5-30GPa. The graphs are as shown in Fig. 4.9.



Fig. 4.9: Graphs of Enthalpy against pressure from 0.2-0.8Gpa and from 5-35GPa. At both pressures ranges, the enthalpy increases with a pressure increase, results which are in good agreement with previous studies on the material as seen from (Mahesh & Reddy, 2018) Enthalpy is given as:

$$H = U + PV$$
,

Where, H is-Enthalpy, U is -Sum of internal energy, P is-Pressure on the system and V is-Volume of the system. Enthalpy is useful because it informs us on how much energy is in a given system.

As pressure increases, the enthalpy of this crystal system increases since as seen from the above equation, the two quantities are directly proportional. Graphs of volume against pressure were plotted and they are as shown in Fig. 4.10 :



Fig. 4.10: Graphs of volume against pressure applied on the crystal system. Up to a pressure of 1GPa, application of pressure on the system leads to a decrease in the volume as expected from past experimental studies on the pnictide.(W. Uhoya *et al.*, 2010)

4.5 Phonon dispersion

Below in Figure 4.11 is the phonon dispersion curve of the band structure (phonon bands)



Fig. 4.11: The phonon dispersion curve. The optical (upper) mode and the acoustic (lower) mode are clearly differentiated.

Given that Europium diiron diarsenide has got five atoms; there are 15 modes of vibration. The acoustic modes converge at the gamma high symmetry point.

In the study of phonons, there exist three modes that are associated with each mode number n. For a primitive cell that has N atoms, there exist 3N degrees of freedom (Simon, 2013), taking into account the x, y, and z axes(Birman, 1984). The number of acoustic modes is usually three for crystals whose number of atoms is equal to or greater than two, and the optical modes are given by 3N-3(Mahan, 2011). Therefore, given that Europium diiron diarsenide has got five atoms; there are 15 modes of vibration expected. As seen in the Fig. 4.11 above, there are 15 vibration modes with twelve being optical modes and three being acoustic modes. The acoustic modes converge at the gamma high symmetry point. Acoustic modes vibrate at a slower frequency and are in the same phase with the unit cell. Optical modes of vibration have a higher frequency compared to acoustic modes and two neighboring atoms vibrate in a direction opposite to each other, that is to say, if one atom vibrates in the left direction, the adjacent atom will vibrate to the right. In the acoustic mode, the two adjacent atoms will vibrate together in the same direction. Phonon dispersions are computed along a given line of high symmetry points. The above information therefore confirms that the compound is dynamically stable.





Fig. 4.12: The plotted phonon Density of States. The phonon Density of States is similar to the Density Functional Theory Density of States. As the wavelength becomes longer, the frequency of the acoustic modes of vibration goes to zero, while for longer wave lengths in optical phonons, the frequency does not go to zero as seen from the figure above.

A system is considered to be dynamically stable at equilibrium if the potential energy is always increasing for any combination of displacement of atoms, therefore, phonons should have non negative and real frequencies for stability (Togo & Tanaka, 2015). Negative frequencies imply that the potential energy reduces hence the system is unstable. Phonon frequencies arise as a result of the displacement of atoms in a given crystal from the rest position, which in turn makes the forces to rise (Togo & Tanaka, 2015). The phonon calculation of finite differences was done using Phonopy. A smearing of 0.2eV of the Methfessel-Paxton scheme was used. The finite displacement and super cell technique was used with a 2x2x2 super cell of the conventional unit cell. We used an energy cut off of 30Ry, which dictated the number of plane waves to be employed. It is important to establish the number of normal modes that are neighboring a certain phonon energy, these details are necessary when studying thermal and electrical conductivity and

also establishing the critical temperature of superconducting materials(Giustino, 2014). The Debye temperature is a constant that is associated with the highest allowed mode of vibration (Hill, 1986). The Debye temperature in this study was 436.454K and the average Debye sound velocity was 3330.336 m/s. A Debye temperature of above 400K implies that the crystal's thermal conductivity is high (Low, 2012), and since the compound we were studying had a Debye temperature of above 400K, we concluded that the thermal conductivity is high. Note that, for temperatures that are below the Debye temperature, the heat capacity of the compound rises with the temperature cube and for temperatures above the Debye temperature, the heat capacity of the crystal remains constant, that is to say, it no longer depends on temperature. The Debye temperature and the heat capacity are directly proportional(Debye, 1912) A high Debye temperature implies that the material is hard for example, Diamond, while a low Debye temperature implies that the material is soft, for example, Lead has a low Debye temperature. The Debye temperature is the approximate limit below which the quantum effects in a system can be seen. It is defined by:

 $k\theta = hv$,

Where, k –Boltzmann constant, v-Debye frequency, h- Planck's constant and θ is the Debye temperature. (Hill, 1986) The highest frequency of phonons and the Debye temperature are coupled with each other(Low, 2012).

CHAPTER FIVE

CONCLUSIONS AND RECCOMENDATIONS

The aim of this computational study was to provide additional information on the structural, mechanical and electronic structure properties of the iron pnictide compound Europium diiron diarsenide, and also provide more details on the behavior of the compound on subjection to external pressure. The thermodynamic property of Phonon vibration modes was also studied. There were guiding objectives in this study, which were achieved. The optimized lattice parameters in this computational study were in close agreement with available experimental values and values from other Density Functional Theory studies. The DFT technique mostly is suitable for ground state studies; hence the results obtained in this study were at the ground state of the compound.

The milestones below have been achieved in the study of the above mentioned iron pnictide compound:

1).The mechanical structure properties of Bulk, Shear and Young's modulus, and Poisson's ratio have also been studied. These have guided in classifying of the compound as a ductile material Poisson's ratio is in the range 0.25-0.5, implying that the forces present in the compound are central forces and that the compound is also hard due to its large bulk modulus and highly anisotropic.

The elastic constants have also been studied for the first time, which went on to further prove that the material is actually ductile. The elastic constants also show that the compound is of a stable tetragonal structure. 2). The electronic structure properties including the Density of States and Band Structure have been studied. It has been noted from the properties that there exists no band gap hence the compound is metallic, and the DOS graphs show properties similar to other compounds in the iron pnictide family.

3). The electronic and mechanical structure properties under application of increasing pressure of up to 35Gpa were also studied. The study of the effect of pressure on volume of the material indicated that the volume decreases as the pressure increases, implying that the material shows normal compressional behavior. The study of the effect of pressure on the Fermi energy also showed that the Fermi energy increases with pressure, which implies that the population of charge carriers with respect to Density of States increases, hence more electrons are made available for electrical conductivity in the compound. The compound was quite expensive in terms of computational time and a bit challenging but we managed to make the above mentioned milestones.

4). The thermodynamic property of Phonon dispersion was also studied and the nature of optical and acoustic vibration modes confirmed that the compound is dynamically stable. There were no negative frequencies. The Debye temperature was also studied and it revealed that the compound is a good thermal conductor

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The findings in this study provided more information on the mechanical and electronic structure properties of the iron pnictide Europium diiron diarsenide. It also provided additional information on how the iron pnictide responds to pressure changes. This information can enhance future use of the iron pnictide as a superconductor in industry.

The challenges that were faced in this study included: Early on in the research, determination of the type of pseudo potentials to be used, whether hard or soft, PAW or USSP. Also, optimization of the crystal structure presented a challenge since it was a quite 'heavy' compound in terms of the number of electrons and the number of atoms. This increased the number of hours that were required to perform optimization of the energy, cell dimensions and k-points. Sometimes it made the computer to 'Hang', rendering it useless for the time period of the calculation. However, this challenge was later solved with the usage of the super computer in South Africa. Having a little background in usage of computers also presented a big challenge at the beginning, since the research was basically theoretical and needed us to use computer operating systems such as Ubuntu which was very new to me, also, installation and learning of the commands also presented a challenge at the beginning but with time, all that became a thing of the past.

The current research leaves gaps and questions which need to be addressed in future research, and include the following;

More study should be done on application of pressure on the material to explain more on the phase transition on the material. A phase transition study from one crystal structure to another and its effects on the structure and functioning of the iron pnictide should be done. In some crystals, pressure application leads to a change in the crystal structure. Also, more pressure

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should be applied on the compound so as to establish at what pressure the crystal structure get distorted, that is, to establish how much pressure the material can with stand. The partial density of states at various pressures should also be looked into so as to gain more understanding into the states available in the system. The phonon dispersion should also be closely looked into to understand more on the critical temperature of superconductivity of this particular iron Pnictide. Since the compound also shows some magnetism, more studies on the magnetic structure properties should be done to complement the available studies, and relate the magnetism to superconductivity. Optical properties should also be looked into. All the above properties studied, it will give scientists an in-depth understanding of the compound.

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APPENDICES

APPENDIX I:Input files

The input file of the iron pnictide Europium diiron diarsenide.

&control

```
calculation
                 =
                         'scf',
 restart_mode='from_scratch',
 prefix='EuFe2As2',
                        './',
 pseudo_dir
                  =
 outdir='./tempdir/',
/
&system
 ibrav=7,
 celldm(1) = 7.5419,
 celldm(3) = 5.1355,
 nat=5,
 ntyp=3,
 ecutwfc = 30,
 ecutrho
                     240,
              =
 occupations = 'smearing'
 smearing = 'gaussian'
 degauss = 0.01
/
```

&electrons

```
mixing_beta = 0.2,
```

```
conv_thr = 1.0d-8,
```

```
/
```

ATOMIC_SPECIES

Eu 151.964 Eu.pbe-spdn-kjpaw_psl.1.0.0.UPF

Fe 55.845 Fe.pbe-spn-kjpaw_psl.0.2.1.UPF

As 74.922 As.pbe-n-kjpaw_psl.1.0.0.UPF

ATOMIC_POSITIONS (crystal)

- $Eu \quad 0.00000000 \qquad 0.00000000 \quad 0.000000000$
- Fe 0.817210010 0.272541202 0.455331192
- Fe 0.182789990 0.727458798 0.544668808
- As 0.633980657 0.649443121 0.015462464
- As 0.366019343 0.350556879 0.015462464

K_POINTS (automatic)

664111

The nscf file

&control

calculation = 'nscf'

restart_mode='from_scratch',

prefix='EuFe2As2',

```
pseudo_dir = './',
```

outdir='./tempdir/'

/

&system ibrav= 7, celldm(1) = 7.5419, celldm(3) = 5.1355, nat= 5, ntyp= 3, ecutwfc = 45, ecutrho = 360,

/

&electrons

mixing_beta = 0.2 conv_thr = 1.0d-8

/

ATOMIC_SPECIES

Eu 151.964 Eu.pbe-spdn-kjpaw_psl.1.0.0.UPF

Fe 55.845 Fe.pbe-spn-kjpaw_psl.1.0.0.UPF

As 74.922 As.pbe-n-kjpaw_psl.1.0.0.UPF

ATOMIC_POSITIONS (crystal)

Eu -0.00000000 0.00000000 0.00000000

Fe 0.977790038 0.242572369 0.264782331

Fe 0.022209962 0.757427631 0.735217669

As 0.713485486 0.632926667 -0.080558819

As 0.286514514 0.367073333 0.080558819

K_POINTS tpiba_b

10

0.000000000 0.00000000 0.00000000 30

0.000000000 0.00000000 0.500000000 30

 $0.250000000 \quad 0.250000000 \quad 0.250000000 \quad 30$

 $0.000000000 \quad 0.500000000 \quad 0.000000000 \quad 30$

0.000000000 0.00000000 0.00000000 30

0.500000000 0.500000000 -0.500000000 30

 $-1.00000000 \quad 2.5202352114 \quad 1.000000000 \quad 30$

0.000000000 0.00000000 0.00000000 30

 $-0.1362877078 \quad 0.1362877078 \quad 7.3374188776 \ 30$

0.500000000 0.500000000 -0.500000000 30

Variable cell relax calculation

&control

calculation = 'scf',

restart_mode='from_scratch',

prefix='EuFe2As2',

pseudo_dir = './',

outdir='./tempdir/',

/

&system

ibrav=7,

celldm(1) = 7.5419,

celldm(3) = 5.1355,

nat= 5,

ntyp=3,

ecutwfc = 30,

ecutrho = 240,

occupations = 'smearing'

smearing = 'gaussian'

degauss = 0.01

/

&electrons

mixing_beta = 0.2,

 $conv_thr = 1.0d-8$,

/

&ion

Ion_dynamics = 'bfgs'

&cell

Press=0

/

ATOMIC_SPECIES

Eu 151.964 Eu.pbe-spdn-kjpaw_psl.1.0.0.UPF

Fe 55.845 Fe.pbe-spn-kjpaw_psl.0.2.1.UPF

As 74.922 As.pbe-n-kjpaw_psl.1.0.0.UPF

ATOMIC_POSITIONS (crystal)

- Eu 0.00000000 0.0000000 0.00000000
- Fe 0.817210010 0.272541202 0.455331192
- Fe 0.182789990 0.727458798 0.544668808
- As 0.633980657 0.649443121 0.015462464
- As 0.366019343 0.350556879 0.015462464
- K_POINTS (automatic)

664111

Phonon Calculation

To compute phonons in Quantum Espresso, the following steps are followed:

- 1) A self-consistent field calculation
- 2) A non-self-consistent field calculation
- 3) Pseudo potential ph.x calculation
- 4) Pseudo potential q2r.x calculation
- 5) Pseudo potential matdyn.x calculation.

The scf computes the total energy of a crystal from its equilibrium position. Pseudo potential ph.x calculation computes the normal modes of a specific q-vector, beginning with files obtained from the pw.x calculation in the scf. Dynamical matrices are calculated at this level. The Pseudo

potential q2r .x calculation code reads the dynamical matrices from the previous step and does a Fourier transform on them. The Pseudo potential matdyn.x calculation generates the modes of the phonons and their frequencies. The above procedure did not however yield results therefore a second method was used to calculate the phonons. This second method involves the creating of a super cell using a package known as Phonopy(Togo & Tanaka, 2015) and then generating force sets using Quantum ESSPRESSO for post processing. This second method proved to be successful. There were 9 super cells and a sample of the super cell information is as shown below:

Super cell 001

! ibrav = 0, nat = 40, ntyp = 3

CELL_PARAMETERS bohr

19.7213357861786740 -0.1907791352002044 0.0000000000000000

11.1164888651131673 16.2905715232244397 0.00000000000000000

 $-15.4189123256459197 \quad -8.0498961940121188 \quad 9.2968100231471915$

ATOMIC_SPECIES

Eu 151.96400 Eu.pbe-spdn-kjpaw_psl.1.0.0.UPF

Fe 55.84500 Fe.pbe-spn-kjpaw_psl.1.0.0.UPF

As 74.92160 As.pbe-n-kjpaw_psl.1.0.0.UPF

ATOMIC_POSITIONS crystal

Eu 0.00000000000000 0.0000000000000 0.0010140736703417

Eu 0.00000000000001 0.499999999999999 0.500000000000000 Eu 0.5000000000000 0.499999999999999 0.500000000000000 Eu 0.3749994735000000 0.1249994735000000 0.2499989475000000 Fe 0.8749994735000000 0.1249994735000000 0.2499989475000000 Fe 0.3749994735000001 0.6249994735000000 0.2499989475000000 Fe 0.8749994734999997 0.6249994735000000 0.2499989475000000 Fe Fe 0.3749994735000001 0.1249994735000000 0.7499989475000001 0.8749994735000002 0.1249994735000001 0.7499989475000001 Fe 0.3749994735000002 0.6249994735000000 0.7499989475000001 Fe Fe 0.8749994735000000 0.6249994735000000 0.7499989475000001 0.1250005265000000 0.3750005265000000 0.2500010525000000Fe 0.6250005265000002 0.3750005265000000 0.2500010525000000 Fe Fe 0.1250005265000000 0.8750005265000000 0.2500010525000000Fe 0.6250005265000000 0.8750005264999999 0.2500010525000000 Fe 0.1250005265000000 0.3750005264999999 0.75000105250000000.6250005265000000 0.3750005265000000 0.7500010525000000Fe Fe 0.1250005265000000 0.8750005264999999 0.7500010525000000Fe 0.6250005265000000 0.8750005264999999 0.7500010525000000 0.3105529344999999 0.310553348000000 0.0000000000000000 As 0.8105529345000000 0.3105533480000000 0.0000000000000000 As As 0.3105529345000000 0.8105533479999998 0.0000000000000000

! ibrav = 0, nat = 40, ntyp = 3

CELL_PARAMETERS bohr

Eu 151.96400 Eu.pbe-spdn-kjpaw_psl.1.0.0.UPF

Fe 55.84500 Fe.pbe-spn-kjpaw_psl.1.0.0.UPF

As 74.92160 As.pbe-n-kjpaw_psl.1.0.0.UPF

ATOMIC_POSITIONS crystal

| Eu | 0.0010140826397086 | 0.0000000000000000 | 0.0000000000000000 |
|----|---|-----------------------|---------------------|
| Eu | 0.5000000000000000000000000000000000000 | 0.0000000000000000 | 0.00000000000000000 |
| Eu | 0.0000000000000000000000000000000000000 | 0.5000000000000000 | 0.00000000000000000 |
| Eu | 0.500000000000000000 | 0.4999999999999999999 | 0.0000000000000000 |
| Eu | 0.0000000000000000000000000000000000000 | 0.0000000000000000 | 0.50000000000000000 |
| Eu | 0.500000000000000000 | 0.0000000000000000 | 0.50000000000000000 |
| Eu | 0.0000000000000000000000000000000000000 | 0.4999999999999999999 | 0.50000000000000000 |
| Eu | 0.5000000000000000000 | 0.4999999999999999999 | 0.50000000000000000 |
| Fe | 0.3749994735000000 | 0.1249994735000000 | 0.2499989475000000 |
| Fe | 0.8749994735000000 | 0.1249994735000000 | 0.2499989475000000 |
| Fe | 0.3749994735000001 | 0.6249994735000000 | 0.2499989475000000 |
| Fe | 0.8749994734999997 | 0.6249994735000000 | 0.2499989475000000 |
| Fe | 0.3749994735000001 | 0.1249994735000000 | 0.7499989475000001 |
| Fe | 0.8749994735000002 | 0.1249994735000001 | 0.7499989475000001 |
| Fe | 0.3749994735000002 | 0.6249994735000000 | 0.7499989475000001 |
| Fe | 0.8749994735000000 | 0.6249994735000000 | 0.7499989475000001 |
| Fe | 0.1250005265000000 | 0.3750005265000000 | 0.2500010525000000 |
| Fe | 0.6250005265000002 | 0.3750005265000000 | 0.2500010525000000 |
| Fe | 0.1250005265000000 | 0.8750005265000000 | 0.2500010525000000 |
| Fe | 0.6250005265000000 | 0.8750005264999999 | 0.2500010525000000 |
| Fe | 0.1250005265000000 | 0.3750005264999999 | 0.7500010525000000 |
| Fe | 0.6250005265000000 | 0.3750005265000000 | 0.7500010525000000 |

0.1250005265000000 0.8750005264999999 0.7500010525000000 Fe Fe 0.6250005265000000 0.8750005264999999 0.7500010525000000 As 0.3105529344999999 0.310553348000000 0.0000000000000000 As 0.8105529345000000 0.3105533480000000 0.0000000000000000 As 0.3105529345000000 0.8105533479999998 0.0000000000000000 As 0.8105529345000000 0.8105533480000000 0.0000000000000000 As 0.3105529345000000 0.3105533480000000 0.5000000000000000 As 0.8105529345000000 0.3105533480000000 0.5000000000000000 As 0.3105529345000001 0.8105533479999999 0.5000000000000000 As 0.8105529345000000 0.8105533479999999 0.5000000000000000 As 0.1894470655000000 0.1894466520000000 0.0000000000000000 As 0.6894470655000000 0.1894466520000000 0.0000000000000000 As 0.1894470655000000 0.6894466520000000 0.000000000000000 As 0.6894470655000000 0.6894466519999999 0.0000000000000000 As 0.1894470655000000 0.1894466520000000 0.500000000000000 As 0.6894470655000000 0.1894466519999999 0.500000000000000 As 0.1894470655000001 0.689446652000000 0.5000000000000000 As 0.6894470655000000 0.6894466520000000 0.5000000000000000 Super cell 003

! ibrav = 0, nat = 40, ntyp = 3

CELL_PARAMETERS bohr

 $-15.4189123256459197 \quad -8.0498961940121188 \quad 9.2968100231471915$

ATOMIC_SPECIES

Eu 151.96400 Eu.pbe-spdn-kjpaw_psl.1.0.0.UPF

Fe 55.84500 Fe.pbe-spn-kjpaw_psl.1.0.0.UPF

As 74.92160 As.pbe-n-kjpaw_psl.1.0.0.UPF

ATOMIC_POSITIONS crystal

Eu Eu Eu Eu Eu Eu 0.5000000000000 0.49999999999999 0.500000000000000 Eu 0.3749994735000000 0.1249994735000000 0.2510130211703417 Fe 0.8749994735000000 0.1249994735000000 0.2499989475000000 Fe Fe 0.3749994735000001 0.6249994735000000 0.2499989475000000 0.8749994734999997 0.6249994735000000 0.2499989475000000 Fe 0.3749994735000001 0.1249994735000000 0.7499989475000001 Fe Fe 0.8749994735000002 0.1249994735000001 0.7499989475000001 0.3749994735000002 0.6249994735000000 0.7499989475000001 Fe 0.8749994735000000 0.6249994735000000 0.7499989475000001 Fe 0.1250005265000000 0.3750005265000000 0.2500010525000000 Fe
Fe 0.6250005265000002 0.3750005265000000 0.25000105250000000.1250005265000000 0.8750005265000000 0.2500010525000000 Fe 0.6250005265000000 0.8750005264999999 0.2500010525000000 Fe 0.1250005265000000 0.3750005264999999 0.7500010525000000 Fe 0.6250005265000000 0.3750005265000000 0.7500010525000000 Fe 0.1250005265000000 0.8750005264999999 0.7500010525000000 Fe 0.6250005265000000 0.8750005264999999 0.7500010525000000 Fe 0.3105529344999999 0.310553348000000 0.0000000000000000 As As 0.8105529345000000 0.3105533480000000 0.0000000000000000 0.3105529345000000 0.8105533479999998 0.0000000000000000 As As 0.8105529345000000 0.8105533480000000 0.0000000000000000 As 0.3105529345000000 0.3105533480000000 0.5000000000000000 0.8105529345000000 0.3105533480000000 0.5000000000000000 As 0.3105529345000001 0.8105533479999999 0.5000000000000000 As 0.8105529345000000 0.8105533479999999 0.5000000000000000 As As 0.1894470655000000 0.1894466520000000 0.0000000000000000 As 0.1894470655000000 0.6894466520000000 0.0000000000000000 As As As 0.1894470655000000 0.1894466520000000 0.500000000000000 As 0.6894470655000000 0.1894466519999999 0.5000000000000000 As 0.1894470655000001 0.689446652000000 0.5000000000000000 As 0.6894470655000000 0.6894466520000000 0.5000000000000000

The output file for super cell 001 is as below

Program PWSCF v.6.4.1 starts on 28Apr2020 at 20:27:55

This program is part of the open-source Quantum ESPRESSO suite for quantum simulation of materials; please cite

"P. Giannozzi et al., J. Phys.:Condens. Matter 21 395502 (2009);

"P. Giannozzi et al., J. Phys.:Condens. Matter 29 465901 (2017);

URL http://www.quantum-espresso.org",

in publications or presentations arising from this work. More details at http://www.quantum-espresso.org/quote

Parallel version (MPI), running on 48 processors

MPI processes distributed on 2 nodes R & G space division: proc/nbgrp/npool/nimage =

Reading input from supercell-001.in

Current dimensions of program PWSCF are:

Max number of different atomic species (ntypx) = 10

Max number of k-points (npk) = 40000

Max angular momentum in pseudopotentials (lmaxx) = 3

file Eu.pbe-spdn-kjpaw_psl.1.0.0.UPF: wavefunction(s) 5P renormalized file Fe.pbe-spn-kjpaw_psl.1.0.0.UPF: wavefunction(s) 3P 3D renormalized

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Subspace diagonalization in iterative solution of the eigenvalue problem: one sub-group per band group will be used scalapack distributed-memory algorithm (size of sub-group: 4* 4 procs)

Parallelization info

| |
|------|

| sticks: | dense s | smooth | PW | G-vecs: | dense | smooth | PW |
|---------|---------|--------|------|---------|--------|----------|-----|
| Min | 171 | 85 | 26 | 6054 | 2140 | 365 | |
| Max | 172 | 86 | 27 | 6057 | 2142 | 366 | |
| Sum | 8227 | 4111 | 1263 | 290 | 659 10 | 02771 17 | 539 |

bravais-lattice index 0 = lattice parameter (alat) = 19.7223 a.u. unit-cell volume 3006.5198 (a.u.)^3 = number of atoms/cell 40 = number of atomic types = 3 number of electrons 424.00 = number of Kohn-Sham states= 254 kinetic-energy cutoff 40.0000 Ry =charge density cutoff 320.0000 Ry =convergence threshold 1.0E-09 = mixing beta 0.4000 = number of iterations used = 8 plain mixing = SLA PW PBX PBC (1 4 3 4 0 0) Exchange-correlation

celldm(1)= 19.722259 celldm(2)= 0.000000 celldm(3)= 0.000000 celldm(4)= 0.000000 celldm(5)= 0.000000 celldm(6)= 0.000000

crystal axes: (cart. coord. in units of alat)

a(1) = (0.999953 - 0.009673 0.000000)a(2) = (0.563652 0.825999 0.000000)a(3) = (-0.781803 - 0.408163 0.471387)

reciprocal axes: (cart. coord. in units 2 pi/alat)

b(1) = (0.993489 -0.677945 1.060700) b(2) = (0.011635 1.202715 1.060700) b(3) = (0.000000 0.000000 2.121401)

PseudoPot. # 1 for Eu read from file:

./Eu.pbe-spdn-kjpaw_psl.1.0.0.UPF

MD5 check sum: 02c18b8c493c24051d280dd8a22a9cee

Pseudo is Projector augmented-wave + core cor, Zval = 11.0

Generated using "atomic" code by A. Dal Corso v.6.2.2

Shape of augmentation charge: PSQ

Using radial grid of 1261 points, 6 beta functions with:

l(1) = 0 l(2) = 0 l(3) = 1 l(4) = 1 l(5) = 2l(6) = 2

Q(r) pseudized with 0 coefficients

PseudoPot. # 2 for Fe read from file:

./Fe.pbe-spn-kjpaw_psl.1.0.0.UPF

MD5 check sum: fc81f059e5c5069939230b1155715ae8

Pseudo is Projector augmented-wave + core cor, Zval = 16.0

Generated using "atomic" code by A. Dal Corso v.6.3

Shape of augmentation charge: PSQ

Using radial grid of 1191 points, 6 beta functions with:

l(1) = 0l(2) = 0l(3) = 1 l(4) = 1l(5) = 2l(6) = 2

Q(r) pseudized with 0 coefficients

PseudoPot. # 3 for As read from file: ./As.pbe-n-kjpaw_psl.1.0.0.UPF MD5 check sum: 21b474db91924651be503153fb2dbf55 Pseudo is Projector augmented-wave + core cor, Zval = 5.0 Generated using "atomic" code by A. Dal Corso v.6.3 Shape of augmentation charge: PSQ Using radial grid of 1209 points, 4 beta functions with:

> l(1) = 0l(2) = 0l(3) = 1l(4) = 1

Q(r) pseudized with 0 coefficients

atomic species valence mass pseudopotential

| Eu | 11.00 | 151.96400 | Eu(1.00) |
|----|-------|-----------|-----------|
| Fe | 16.00 | 55.84500 | Fe(1.00) |
| As | 5.00 | 74.92160 | As(1.00) |

No symmetry found

s frac. trans.

isym = 1 identity

cryst. s(1) = (1 0 0)(0 1 0) (0 0 1)

cart. s(1) = (1.0000000 0.0000000 0.0000000) (-0.0000000 1.0000000 0.0000000) (0.0000000 0.0000000 1.0000000)

Cartesian axes

| site n. | atom | positions (alat units) | |
|---------|---------|------------------------------------|---------|
| 1 | Eu tau(| 1) = (-0.0007928 -0.0004139 0.00 | 04780) |
| 2 | Eu tau(| 2) = (0.4999766 -0.0048366 0.00 | (00000 |
| 3 | Eu tau(| 3) = (0.2818260 0.4129996 0.000 |)0000) |
| 4 | Eu tau(| 4) = (0.7818026 0.4081630 0.000 |)0000) |
| 5 | Eu tau(| 5) = (-0.3909013 -0.2040815 0.23 | 56933) |
| 6 | Eu tau(| 6) = (0.1090753 -0.2089181 0.23 | 56933) |
| 7 | Eu tau(| 7) = (-0.1090753 0.2089181 0.23 | 56933) |
| 8 | Eu tau(| 8) = (0.3909013 0.2040815 0.235 | 56933) |
| 9 | Fe tau(| 9) = (0.2499883 -0.0024183 0.117 | 78462) |
| 10 | Fe tau(| 10) = (0.7499649-0.0072550 0.12 | 178462) |
| 11 | Fe tau(| 11) = (0.53181430.4105813 0.11 | 78462) |
| 12 | Fe tau(| 12) = (1.03179090.4057447 0.11 | 78462) |
| 13 | Fe tau(| 13) = (-0.1409130-0.2064998 0.35 | 35395) |
| 14 | Fe tau(| 14) = (0.3590636 -0.2113365 0.35 | 35395) |
| 15 | Fe tau(| 15) = (0.1409130 0.2064998 0.35 | 35395) |
| 16 | Fe tau(| 16) = (0.6408896 0.2016632 0.35 | 35395) |
| 17 | Fe tau(| 17) = (0.1409130 0.2064998 0.11 | 78472) |
| 18 | Fe tau(| 18) = (0.6408896 0.2016632 0.11 | 78472) |

| 19 | Fe | tau(19) = (0.4) | 227389 | 0.6194995 | 0.1178472 |) |
|----|----|-------------------------|----------|------------|-----------|---|
| 20 | Fe | tau(20) = (0.9) | 0227155 | 0.6146628 | 0.1178472 |) |
| 21 | Fe | tau(21) = (-0.2) | 2499883 | 0.0024183 | 0.3535405 |) |
| 22 | Fe | tau(22) = (0.2 | 2499883 | -0.0024183 | 0.3535405 |) |
| 23 | Fe | tau(23) = (0.0) |)318377 | 0.4154180 | 0.3535405 |) |
| 24 | Fe | tau $(24) = (0.5)$ | 5318143 | 0.4105813 | 0.3535405 |) |
| 25 | As | tau(25) = (0.4) | 4855824 | 0.2535128 | 0.0000000 |) |
| 26 | As | tau(26) = (0.9) | 9855590 | 0.2486761 | 0.0000000 |) |
| 27 | As | tau(27) = (0.7) | 7674084 | 0.6665124 | 0.0000000 |) |
| 28 | As | tau(28) = (1.1) | 2673850 | 0.6616758 | 0.0000000 |) |
| 29 | As | tau(29) = (0.4) | 0946811 | 0.0494313 | 0.2356933 |) |
| 30 | As | tau(30) = (0.1) | 5946577 | 0.0445946 | 0.2356933 |) |
| 31 | As | tau(31) = (0.1) | 3765071 | 0.4624309 | 0.2356933 |) |
| 32 | As | tau(32) = (0.3) | 8764837 | 0.4575943 | 0.2356933 |) |
| 33 | As | tau(33) = (0.1) | 2962202 | 0.1546502 | 0.0000000 |) |
| 34 | As | tau(34) = (0.7) | 7961968 | 0.1498136 | 0.0000000 |) |
| 35 | As | tau(35) = (0.1) | 5780461 | 0.5676499 | 0.0000000 |) |
| 36 | As | tau(36) = (1.6) | 0780227 | 0.5628132 | 0.0000000 |) |
| 37 | As | $tau(37) = (-0.1)^{-1}$ | .0946811 | -0.0494313 | 0.2356933 |) |
| 38 | As | tau(38) = (0.4) | 4052955 | -0.0542679 | 0.2356933 |) |
| 39 | As | tau(39) = (0. | 1871448 | 0.3635684 | 0.2356933 |) |
| 40 | As | tau(40) = (0.4) | 6871215 | 0.3587317 | 0.2356933 |) |

Crystallographic axes

| site n. | atom | | po | ositions (cry | /st. coord.) | | |
|---------|------|------|--------|---------------|--------------|-----------|---|
| 1 | Eu | tau(| 1) = (| 0.0000000 | 0.0000000 | 0.0010141 |) |
| 2 | Eu | tau(| 2) = (| 0.5000000 | 0.0000000 | 0.0000000 |) |
| 3 | Eu | tau(| 3) = (| 0.0000000 | 0.5000000 | 0.0000000 |) |
| 4 | Eu | tau(| 4) = (| 0.5000000 | 0.5000000 | 0.0000000 |) |
| 5 | Eu | tau(| 5) = (| 0.0000000 | 0.0000000 | 0.5000000 |) |

| 6 | Eu | tau(| 6) = (0.5000000 | 0.0000000 | 0.5000000 |) |
|----|----|------|------------------|-----------|-----------|---|
| 7 | Eu | tau(| 7) = (0.0000000 | 0.5000000 | 0.5000000 |) |
| 8 | Eu | tau(| 8) = (0.5000000 | 0.5000000 | 0.5000000 |) |
| 9 | Fe | tau(| 9) = (0.3749995 | 0.1249995 | 0.2499989 |) |
| 10 | Fe | tau(| 10) = (0.8749995 | 0.1249995 | 0.2499989 |) |
| 11 | Fe | tau(| 11) = (0.3749995 | 0.6249995 | 0.2499989 |) |
| 12 | Fe | tau(| 12) = (0.8749995 | 0.6249995 | 0.2499989 |) |
| 13 | Fe | tau(| 13) = (0.3749995 | 0.1249995 | 0.7499989 |) |
| 14 | Fe | tau(| 14) = (0.8749995 | 0.1249995 | 0.7499989 |) |
| 15 | Fe | tau(| 15) = (0.3749995 | 0.6249995 | 0.7499989 |) |
| 16 | Fe | tau(| 16) = (0.8749995 | 0.6249995 | 0.7499989 |) |
| 17 | Fe | tau(| 17) = (0.1250005 | 0.3750005 | 0.2500011 |) |
| 18 | Fe | tau(| 18) = (0.6250005 | 0.3750005 | 0.2500011 |) |
| 19 | Fe | tau(| 19) = (0.1250005 | 0.8750005 | 0.2500011 |) |
| 20 | Fe | tau(| 20) = (0.6250005 | 0.8750005 | 0.2500011 |) |
| 21 | Fe | tau(| 21) = (0.1250005 | 0.3750005 | 0.7500011 |) |
| 22 | Fe | tau(| 22) = (0.6250005 | 0.3750005 | 0.7500011 |) |
| 23 | Fe | tau(| 23) = (0.1250005 | 0.8750005 | 0.7500011 |) |
| 24 | Fe | tau(| 24) = (0.6250005 | 0.8750005 | 0.7500011 |) |
| 25 | As | tau(| 25) = (0.3105529 | 0.3105533 | 0.0000000 |) |
| 26 | As | tau(| 26) = (0.8105529 | 0.3105533 | 0.0000000 |) |
| 27 | As | tau(| 27) = (0.3105529 | 0.8105533 | 0.0000000 |) |
| 28 | As | tau(| 28) = (0.8105529 | 0.8105533 | 0.0000000 |) |
| 29 | As | tau(| 29) = (0.3105529 | 0.3105533 | 0.5000000 |) |
| 30 | As | tau(| 30) = (0.8105529 | 0.3105533 | 0.5000000 |) |
| 31 | As | tau(| 31) = (0.3105529 | 0.8105533 | 0.5000000 |) |
| 32 | As | tau(| 32) = (0.8105529 | 0.8105533 | 0.5000000 |) |
| 33 | As | tau(| 33) = (0.1894471 | 0.1894467 | 0.0000000 |) |
| 34 | As | tau(| 34) = (0.6894471 | 0.1894467 | 0.0000000 |) |
| 35 | As | tau(| 35) = (0.1894471 | 0.6894467 | 0.0000000 |) |
| 36 | As | tau(| 36) = (0.6894471 | 0.6894467 | 0.0000000 |) |

37 As $tau(37) = (0.1894471 \ 0.1894467 \ 0.5000000)$

38 As $tau(38) = (0.6894471 \ 0.1894467 \ 0.5000000)$

39 As $tau(39) = (0.1894471 \ 0.6894467 \ 0.5000000)$

40 As $tau(40) = (0.6894471 \ 0.6894467 \ 0.5000000)$

| number of k points= 8 | 3 Marzari-Va | nderbilt smearing, w | width (Ry)= 0.0147 |
|-----------------------|----------------|----------------------|--------------------|
| cart. coord. i | n units 2pi/al | at | |
| k(1) = (0.0000000) | 0.0000000 | 0.0000000), wk = | 0.2500000 |
| k(2) = (0.0000000) | 0.0000000 | -1.0607003), wk = | 0.2500000 |
| k(3) = (-0.0058174) | -0.6013577 | -0.5303502), wk = | 0.2500000 |
| k(4) = (-0.4967443 | 0.3389723 | -0.5303502), wk = | 0.2500000 |
| k(5) = (-0.5025616 | 5 -0.2623854 | -1.0607003), wk = | 0.2500000 |
| | | | |

k(6) = (-0.5025616 - 0.2623854 - 2.1214006), wk = 0.2500000

k(7) = ($0.0058174 \ 0.6013577 \ -0.5303502$), wk = 0.2500000

k(8) = (0.4967443 - 0.3389723 - 0.5303502), wk = 0.2500000

cryst. coord.

| k(| 1) = (| 0.0000000 | 0.0000000 | 0.0000000), wk = | 0.2500000 |
|----|--------|------------|------------|------------------|-----------|
| k(| 2) = (| 0.0000000 | 0.0000000 | -0.500000), wk = | 0.2500000 |
| k(| 3) = (| 0.0000000 | -0.5000000 | 0.0000000), wk = | 0.2500000 |
| k(| 4) = (| -0.5000000 | 0.0000000 | 0.0000000), wk = | 0.2500000 |
| k(| 5) = (| -0.5000000 | -0.5000000 | 0.0000000), wk = | 0.2500000 |
| k(| 6) = (| -0.5000000 | -0.5000000 | -0.500000), wk = | 0.2500000 |
| k(| 7) = (| 0.0000000 | 0.5000000 | -0.500000), wk = | 0.2500000 |
| k(| 8) = (| 0.5000000 | 0.0000000 | -0.500000), wk = | 0.2500000 |

Dense grid: 290659 G-vectors FFT dimensions: (120, 120, 120)

Smooth grid: 102771 G-vectors FFT dimensions: (80, 80, 80)

Dynamical RAM for wfc: 1.03 MB

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| Dynamical RAM for | wfc (w. buffer) |): 9.31 MB |
|-------------------|------------------------|------------|
| Dynamical RAM for | str. fact: | 0.28 MB |
| Dynamical RAM for | local pot: | 0.00 MB |
| Dynamical RAM for | nlocal pot: | 2.28 MB |
| Dynamical RAM for | qrad: | 13.50 MB |
| Dynamical RAM for | rho,v,vnew: | 1.27 MB |
| Dynamical RAM for | rhoin: | 0.42 MB |
| Dynamical RAM for | rho*nmix: | 1.48 MB |
| Dynamical RAM for | G-vectors: | 0.36 MB |
| Dynamical RAM for | h,s,v(r/c): | 2.95 MB |
| Dynamical RAM for | <psi beta>:</psi beta> | 2.17 MB |
| Dynamical RAM for | psi: | 4.14 MB |
| Dynamical RAM for | hpsi: | 4.14 MB |
| Dynamical RAM for | spsi: | 4.14 MB |
| Dynamical RAM for | wfcinit/wfcrot: | 5.14 MB |

| Dynamical RAM for | addusdens: | 18.66 MB |
|-------------------|------------|----------|
|-------------------|------------|----------|

Dynamical RAM for addusforce: 28.29 MB

Dynamical RAM for addusstress: 18.57 MB

Estimated static dynamical RAM per process > 30.92 MB

Estimated max dynamical RAM per process > 59.21 MB

Estimated total dynamical RAM > 2.78 GB

Initial potential from superposition of free atoms

starting charge 423.81344, renormalised to 424.00000 Starting wfcs are 328 randomized atomic wfcs Checking if some PAW data can be deallocated... PAW data deallocated on 32 nodes for type: 1 PAW data deallocated on 32 nodes for type: 2 PAW data deallocated on 32 nodes for type: 3

total cpu time spent up to now is 5.7 secs

Self-consistent Calculation

iteration # 1 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.00E-02, avg # of iterations = 2.9

Threshold (ethr) on eigenvalues was too large: Diagonalizing with lowered threshold Davidson diagonalization with overlap ethr = 7.87E-04, avg # of iterations = 1.0

total cpu time spent up to now is 19.4 secs

total energy = -12415.35511877 Ry Harris-Foulkes estimate = -12417.33672552 Ry estimated scf accuracy < 3.34096610 Ry

iteration # 2 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 7.88E-04, avg # of iterations = 6.2

total cpu time spent up to now is 34.7 secs

total energy = -12414.81195502 Ry Harris-Foulkes estimate = -12418.20441481 Ry estimated scf accuracy < 16.60428850 Ry

iteration # 3 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 7.88E-04, avg # of iterations = 4.2

total cpu time spent up to now is 46.3 secs

total energy = -12416.08961670 Ry Harris-Foulkes estimate = -12416.86371319 Ry estimated scf accuracy < 6.33162685 Ry

iteration # 4 ecut= 40.00 Ry beta= 0.40

Davidson diagonalization with overlap ethr = 7.88E-04, avg # of iterations = 2.0

total cpu time spent up to now is 52.5 secs

total energy = -12416.31335946 Ry Harris-Foulkes estimate = -12416.74148722 Ry estimated scf accuracy < 3.90944787 Ry

iteration # 5 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 7.88E-04, avg # of iterations = 2.0

total cpu time spent up to now is 58.8 secs

total energy = -12416.01709394 Ry Harris-Foulkes estimate = -12417.13761176 Ry estimated scf accuracy < 19.84019358 Ry

iteration # 6 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 7.88E-04, avg # of iterations = 1.2

total cpu time spent up to now is 64.5 secs

total energy = -12416.54200270 Ry Harris-Foulkes estimate = -12416.60681356 Ry estimated scf accuracy < 0.60731708 Ry

iteration # 7 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.43E-04, avg # of iterations = 1.9

total cpu time spent up to now is 70.6 secs

total energy = -12416.57481256 Ry Harris-Foulkes estimate = -12416.59654422 Ry estimated scf accuracy < 0.22748752 Ry

iteration # 8 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 5.37E-05, avg # of iterations = 2.0

total cpu time spent up to now is 77.0 secs

total energy = -12416.56968045 Ry Harris-Foulkes estimate = -12416.60394832 Ry estimated scf accuracy < 0.39044666 Ry

iteration # 9 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 5.37E-05, avg # of iterations = 1.0

total cpu time spent up to now is 82.5 secs

total energy = -12416.58628903 Ry Harris-Foulkes estimate = -12416.58851527 Ry estimated scf accuracy < 0.01707445 Ry

iteration # 10 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 4.03E-06, avg # of iterations = 4.9 total cpu time spent up to now is 92.7 secs

total energy = -12416.58426621 Ry Harris-Foulkes estimate = -12416.59223848 Ry estimated scf accuracy < 0.09471521 Ry

iteration # 11 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 4.03E-06, avg # of iterations = 2.4

total cpu time spent up to now is 99.5 secs

total energy = -12416.58763214 Ry Harris-Foulkes estimate = -12416.58865805 Ry estimated scf accuracy < 0.00564409 Ry

iteration # 12 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.33E-06, avg # of iterations = 2.6

total cpu time spent up to now is 106.7 secs

total energy = -12416.58794460 Ry Harris-Foulkes estimate = -12416.58900155 Ry estimated scf accuracy < 0.01227307 Ry

iteration # 13 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.33E-06, avg # of iterations = 1.8 total cpu time spent up to now is 112.7 secs

total energy = -12416.58828668 Ry Harris-Foulkes estimate = -12416.58869401 Ry estimated scf accuracy < 0.00303896 Ry

iteration # 14 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 7.17E-07, avg # of iterations = 1.9

total cpu time spent up to now is 118.8 secs

total energy = -12416.58843249 Ry Harris-Foulkes estimate = -12416.58864477 Ry estimated scf accuracy < 0.00157895 Ry

iteration # 15 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 3.72E-07, avg # of iterations = 2.0

total cpu time spent up to now is 125.6 secs

total energy = -12416.58836997 Ry Harris-Foulkes estimate = -12416.58875814 Ry estimated scf accuracy < 0.00474805 Ry

iteration # 16 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 3.72E-07, avg # of iterations = 1.5

total cpu time spent up to now is 131.6 secs

total energy = -12416.58853212 Ry Harris-Foulkes estimate = -12416.58862197 Ry estimated scf accuracy < 0.00099054 Ry

iteration # 17 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 2.34E-07, avg # of iterations = 1.0

total cpu time spent up to now is 137.1 secs

total energy = -12416.58853623 Ry Harris-Foulkes estimate = -12416.58860594 Ry estimated scf accuracy < 0.00052268 Ry

iteration # 18 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.23E-07, avg # of iterations = 2.0

total cpu time spent up to now is 143.6 secs

total energy = -12416.58848780 Ry Harris-Foulkes estimate = -12416.58866341 Ry estimated scf accuracy < 0.00199064 Ry

iteration # 19 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.23E-07, avg # of iterations = 2.1

total cpu time spent up to now is 150.4 secs

total energy = -12416.58851646 Ry Harris-Foulkes estimate = -12416.58864831 Ry estimated scf accuracy < 0.00162978 Ry

iteration # 20 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.23E-07, avg # of iterations = 1.9

total cpu time spent up to now is 156.5 secs

total energy = -12416.58855930 Ry Harris-Foulkes estimate = -12416.58860279 Ry estimated scf accuracy < 0.00043877 Ry

iteration # 21 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.03E-07, avg # of iterations = 1.0

total cpu time spent up to now is 162.0 secs

total energy = -12416.58857044 Ry Harris-Foulkes estimate = -12416.58859522 Ry estimated scf accuracy < 0.00026970 Ry

iteration # 22 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 6.36E-08, avg # of iterations = 1.0

total cpu time spent up to now is 167.5 secs

total energy = -12416.58857785 Ry

Harris-Foulkes estimate = -12416.58859042 Ry estimated scf accuracy < 0.00013153 Ry

iteration # 23 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 3.10E-08, avg # of iterations = 1.0

total cpu time spent up to now is 173.0 secs

total energy = -12416.58858349 Ry Harris-Foulkes estimate = -12416.58858559 Ry estimated scf accuracy < 0.00001235 Ry

iteration # 24 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 2.91E-09, avg # of iterations = 2.5

total cpu time spent up to now is 180.2 secs

total energy = -12416.58858233 Ry Harris-Foulkes estimate = -12416.58858750 Ry estimated scf accuracy < 0.00005740 Ry

iteration # 25 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 2.91E-09, avg # of iterations = 2.1

total cpu time spent up to now is 186.8 secs

total energy = -12416.58858429 Ry Harris-Foulkes estimate = -12416.58858548 Ry estimated scf accuracy < 0.00000874 Ry

iteration # 26 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 2.06E-09, avg # of iterations = 2.0

total cpu time spent up to now is 193.1 secs

total energy = -12416.58858432 Ry Harris-Foulkes estimate = -12416.58858577 Ry estimated scf accuracy < 0.00001653 Ry

iteration # 27 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 2.06E-09, avg # of iterations = 1.2

total cpu time spent up to now is 198.8 secs

total energy = -12416.58858479 Ry Harris-Foulkes estimate = -12416.58858546 Ry estimated scf accuracy < 0.00000742 Ry

iteration # 28 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.75E-09, avg # of iterations = 1.0

total cpu time spent up to now is 204.4 secs

total energy = -12416.58858488 Ry Harris-Foulkes estimate = -12416.58858539 Ry estimated scf accuracy < 0.00000504 Ry iteration # 29 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.19E-09, avg # of iterations = 1.0

total cpu time spent up to now is 209.9 secs

total energy = -12416.58858503 Ry Harris-Foulkes estimate = -12416.58858530 Ry estimated scf accuracy < 0.00000225 Ry

iteration # 30 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 5.31E-10, avg # of iterations = 1.9

total cpu time spent up to now is 216.0 secs

total energy = -12416.58858495 Ry Harris-Foulkes estimate = -12416.58858541 Ry estimated scf accuracy < 0.00000459 Ry

iteration # 31 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 5.31E-10, avg # of iterations = 2.0

total cpu time spent up to now is 222.5 secs

total energy = -12416.58858486 Ry Harris-Foulkes estimate = -12416.58858554 Ry estimated scf accuracy < 0.00000874 Ry iteration # 32 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 5.31E-10, avg # of iterations = 2.0

total cpu time spent up to now is 228.9 secs

total energy = -12416.58858507 Ry Harris-Foulkes estimate = -12416.58858530 Ry estimated scf accuracy < 0.00000235 Ry

iteration # 33 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 5.31E-10, avg # of iterations = 1.0

total cpu time spent up to now is 234.4 secs

total energy = -12416.58858514 Ry Harris-Foulkes estimate = -12416.58858526 Ry estimated scf accuracy < 0.00000105 Ry

iteration # 34 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 2.47E-10, avg # of iterations = 1.0

total cpu time spent up to now is 239.9 secs

total energy = -12416.58858517 Ry Harris-Foulkes estimate = -12416.58858525 Ry estimated scf accuracy < 0.00000090 Ry

iteration # 35 ecut= 40.00 Ry beta= 0.40

Davidson diagonalization with overlap ethr = 2.12E-10, avg # of iterations = 1.0

total cpu time spent up to now is 245.4 secs

total energy = -12416.58858519 Ry Harris-Foulkes estimate = -12416.58858524 Ry estimated scf accuracy < 0.00000051 Ry

iteration # 36 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.21E-10, avg # of iterations = 1.0

total cpu time spent up to now is 250.9 secs

total energy = -12416.58858520 Ry Harris-Foulkes estimate = -12416.58858523 Ry estimated scf accuracy < 0.00000035 Ry

iteration # 37 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 8.33E-11, avg # of iterations = 1.0

total cpu time spent up to now is 256.5 secs

total energy = -12416.58858521 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000015 Ry

iteration # 38 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 3.44E-11, avg # of iterations = 1.0

total cpu time spent up to now is 262.1 secs

total energy = -12416.58858521 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000007 Ry

iteration # 39 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.54E-11, avg # of iterations = 1.0

total cpu time spent up to now is 267.6 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000007 Ry

iteration # 40 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 1.54E-11, avg # of iterations = 1.0

total cpu time spent up to now is 273.1 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000004 Ry

iteration # 41 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 9.72E-12, avg # of iterations = 1.0 total cpu time spent up to now is 278.6 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000005 Ry

iteration # 42 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 9.72E-12, avg # of iterations = 1.0

total cpu time spent up to now is 284.2 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000005 Ry

iteration # 43 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 9.72E-12, avg # of iterations = 1.4

total cpu time spent up to now is 290.0 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000007 Ry

iteration # 44 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 9.72E-12, avg # of iterations = 1.2 total cpu time spent up to now is 295.7 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000004 Ry

iteration # 45 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 9.63E-12, avg # of iterations = 1.0

total cpu time spent up to now is 301.2 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000002 Ry

iteration # 46 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 3.74E-12, avg # of iterations = 1.0

total cpu time spent up to now is 306.7 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000001 Ry

iteration # 47 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 2.52E-12, avg # of iterations = 1.0

total cpu time spent up to now is 312.2 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 0.00000001 Ry

iteration # 48 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 2.52E-12, avg # of iterations = 1.0

total cpu time spent up to now is 317.7 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 2.7E-09 Ry

iteration # 49 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 6.32E-13, avg # of iterations = 1.0

total cpu time spent up to now is 323.3 secs

total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry estimated scf accuracy < 2.0E-09 Ry

iteration # 50 ecut= 40.00 Ry beta= 0.40 Davidson diagonalization with overlap ethr = 4.81E-13, avg # of iterations = 1.0

total cpu time spent up to now is 328.8 secs

k = 0.0000 0.0000 0.0000 (12843 PWs) bands (ev):

-65.6686 -65.6672 -65.6270 -65.6270 -65.6269 -65.6269 -65.6268 -65.6268 -65.6266 -65.6266 -65.6266 -65.6266 -65.6255 -65.6245 -65.5883 -65.5872 -31.8741 -31.8735 -31.8597 -31.8286 -31.8258 -31.8251 -31.8057 -31.8050 -31.7229 -31.6959 -31.6959 -31.6958 -31.6958 -31.6888 -31.6888 -31.6887 -31.6887 -31.6852 -31.6823 -31.6823 -31.6822 -31.6822 -31.6820 -31.6819 -31.6818 -31.6818 -31.6725 -31.6724 -31.6582 -31.6582 -31.6582 -31.6581 -31.6571 -31.6509 -31.6508 -31.6508 -31.6507 -31.6507 -31.6190 -31.6178 -31.5778 -31.5773 -31.5613 -31.5609 -31.5053 -31.5048 -31.4952 -31.4929 -20.0084 -20.0017 -19.9364 -19.9364 -19.9364 -19.9364 -19.8750 -19.8749 -0.3241 -0.3240 -0.3240 -0.3240 0.2770 0.2772 0.3262 0.32640.8698 1.0262 1.0262 1.0262 1.0262 1.1184 1.1188 0.6132 1.1296 1.2024 1.2025 1.2997 1.2997 1.2997 1.2997 1.1292 5.3604 6.2782 6.5207 6.5215 8.1974 8.1974 8.1974 8.1974 8.5672 9.0157 9.0157 9.0158 9.0158 10.1629 10.1635 10.2527 12.1320 13.779413.7794 13.7794 13.7794 13.8377 13.8407 14.2162 14.6074 14.607414.6075 14.6075 14.9865 14.9869 15.2605 15.2633 15.6839 15.683915.6839 15.6839 16.1338 16.1339 16.5245 16.5251 17.0926 17.0926 17.0926 17.2252 17.2253 16.5973 16.598117.0921 17.2253 17.225517.3112 17.3903 17.3904 17.3904 17.3904 17.5208 17.5217 17.624417.6526 17.6848 17.8144 17.8271 17.8477 17.8522 17.8527 17.968617.9691 18.7404 18.7463 18.8371 18.8379 19.0104 19.0689 19.2356 19.2365 19.4351 19.5843 19.0104 19.0104 19.0104 19.5843 19.5843 19.5843 19.6245 19.6245 19.6246 19.6246 19.6925 19.7769 19.7769 19.7769 19.7770 20.0253 20.0253 20.0253 20.0253 20.0731 20.1179 20.1179 20.1179 20.1179 20.2239 20.2391 20.7821 20.7828 20.840920.8410 21.0058 21.0090 21.0324 21.0325 21.0726 21.0726 21.0727 21.0727 21.5663 21.6129 21.6130 21.6507 22.8055

22.832722.882322.971422.971623.066923.067323.067323.067423.130823.154123.154123.154223.154623.222823.476723.477123.518523.519424.549924.836424.896625.025125.026225.026425.026525.047725.047825.047925.049425.154325.155026.489326.489426.489526.489526.601127.180327.1819

occupation numbers

| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |

| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0006 |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.0007 | 1.0024 | 1.0024 | 1.0360 | 1.0373 | 1.0477 | 1.0477 | 1.0663 |
| 1.0663 | 1.0664 | 1.0664 | 0.0693 | 0.0323 | 0.0323 | 0.0162 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | | |

k = 0.0000 0.0000-1.0607 (12866 PWs) bands (ev):

-65.6472 -65.6469 -65.6468 -65.6466 -65.6464 -65.6464 -65.6463 -65.6462 -65.6082 -65.6080 -65.6074 -65.6072 -65.6072 -65.6070 -65.6070 -65.6070 -31.8472 -31.8471 -31.8471 -31.8470 -31.8465 -31.8463 -31.8453 -31.8451 -31.7046 -31.7045 -31.7045 -31.7044 -31.6992 -31.6992 -31.6991 -31.6990 -31.6884 -31.6880 -31.6843 -31.6842 -31.6816 -31.6811 -31.6754 -31.6754 -31.6750 -31.6750 -31.6674 -31.6673 -31.6673 -31.6672 -31.6647 -31.6645 -31.6603 -31.6598 -31.6424 -31.6420 -31.6342 -31.6342 -31.6338 -31.6338 -31.5420 -31.5418 -31.5332 -31.5331 -31.5330 -31.5330 -31.5330 -31.5328 -19.9404 -19.9400 -19.9386 -19.9386 -19.9386 -19.9385 -19.9371 -19.9367 0.3373 0.3379 0.3643 0.3646 0.3647 0.3650 0.3979 0.3984 0.6852 0.6873 0.6966 0.6967 0.6967 0.6968 0.7055 0.7076 0.9356 0.9367 0.9952 0.9956 0.9958 0.9961 1.0493 1.0500 7.0442 7.0447 7.2492 7.2498 7.2499 7.2505 7.5079 7.5082 8.9025 8.9042 9.3814 9.3821 9.3837 9.3843 9.9628 9.9636 13.0786 13.0787 14.1229 14.1236 14.1238 14.1245 14.8434 14.8438 14.8839 14.8854 14.9682 14.9686 14.9692 14.9696 15.3954 15.3972 15.5906 15.5907 15.5929 15.5930 15.7251 15.7281 15.8749 15.8771 16.0486 16.0491 16.3955 16.3963 16.6894 16.6904 16.6915 16.6925 16.8568 16.859017.2598 17.2617 17.2625 17.2644 17.6406 17.6434 17.6436 17.646217.6735 17.6753 18.0912 18.0927 18.2812 18.2813

18.395918.396218.447318.448118.525318.525718.544718.544918.545718.546019.048919.049019.050419.050519.065219.067719.294019.295119.462219.463019.463719.464519.765219.766320.327520.327920.340120.340620.770820.771020.772820.773820.774320.775220.802120.802920.805220.805220.806020.806120.833020.833520.928920.929920.931420.932421.016821.017021.340021.341321.344521.345821.425621.426221.901521.904522.116022.118722.213122.214822.216422.218322.881722.882323.713423.713824.440424.442824.552024.558724.833724.834624.836124.837025.452825.454525.455525.457125.885325.892826.229626.232626.232726.235826.506726.510826.5108

occupation numbers

| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
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| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
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| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0005 | 1.0005 | 1.0005 | 1.0005 |
| 1.0005 | 1.0005 | 1.0010 | 1.0011 | 1.0011 | 1.0011 | 1.0011 | 1.0011 |
| 1.0021 | 1.0021 | 1.0124 | 1.0126 | 1.0129 | 1.0131 | 1.0407 | 1.0407 |
| 0.6882 | 0.6834 | 0.6715 | 0.6666 | 0.3752 | 0.3735 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | | |

k =-0.0058-0.6014-0.5304 (12838 PWs) bands (ev):

-65.6558 -65.6556 -65.6555 -65.6553 -65.6264 -65.6264 -65.6263 -65.6262 -65.6262 -65.6262 -65.6261 -65.6260 -65.5994 -65.5992 -65.5990 -65.5989 -31.8065 -31.8064 -31.8059 -31.8057 -31.8009 -31.8008 -31.8003 -31.8001 -31.7853 -31.7850 -31.7838 -31.7835 -31.7772 -31.7772 -31.7761 -31.7760 -31.6963 -31.6962 -31.6877 -31.6876 -31.6594 -31.6593 -31.6592 -31.6591 -31.6566 -31.6565 -31.6565 -31.6564 -31.6389 -31.6388 -31.6270 -31.6269 -31.6061 -31.6061 -31.5989 -31.5989 -31.5942 -31.5940 -31.5939 -31.5936 -31.5633 -31.5632 -31.5628 -31.5627 -31.5544 -31.5543 -31.5539 -31.5537 -19.9727 -19.9725 -19.9694 -19.9692 -19.9060 -19.9058 -19.9058 -19.9056 -0.0383 -0.0371 -0.0371 -0.0359 0.2892 0.2917 0.3137 0.3158 0.7691 0.7710 0.7710 0.7729 0.8197 0.8198 0.9403 0.9412 1.1121 1.1125 1.1126 1.1129 1.2076 1.2080 1.2128 1.2132 6.6834 6.6840 7.2124 7.2127 7.3647 7.3654 7.3655 7.3662

121

| 8.8402 | 8.8417 | 9.5225 | 9.5235 | 9.5237 | 9.5248 | 9.68 | 867 9.6 | 887 |
|---------|---------|---------|---------|--------|---------|------|---------|---------|
| 13.2938 | 13.2949 | 13.9837 | 13.9845 | 13.984 | 7 13.9 | 854 | 14.1793 | 14.1795 |
| 14.8827 | 14.8838 | 14.8846 | 14.8856 | 15.243 | 4 15.2 | 446 | 15.5810 | 15.5816 |
| 15.7232 | 15.7234 | 15.7255 | 15.7257 | 16.019 | 5 16.0 | 211 | 16.3144 | 16.3179 |
| 16.3245 | 16.3262 | 16.6005 | 16.6026 | 16.602 | 8 16.6 | 051 | 16.8665 | 16.8687 |
| 17.0006 | 17.0030 | 17.0199 | 17.0229 | 17.023 | 8 17.0 | 267 | 17.7166 | 17.7208 |
| 17.7536 | 17.7567 | 17.9053 | 17.9071 | 17.907 | 1 17.9 | 089 | 17.9682 | 17.9705 |
| 18.0637 | 18.0641 | 18.2276 | 18.2277 | 18.667 | 2 18.6 | 677 | 18.6679 | 18.6684 |
| 18.9901 | 18.9901 | 18.9912 | 18.9914 | 19.109 | 9 19.1 | 110 | 19.2072 | 19.2075 |
| 19.2078 | 19.2079 | 19.4527 | 19.4543 | 19.548 | 3 19.5 | 503 | 19.9194 | 19.9204 |
| 20.2274 | 20.2298 | 20.2298 | 20.2302 | 20.230 | 9 20.2 | 324 | 20.3897 | 20.3913 |
| 20.5502 | 20.5507 | 20.5512 | 20.5514 | 20.762 | 9 20.7 | 633 | 20.7634 | 20.7637 |
| 20.8494 | 20.8507 | 20.9706 | 20.9710 | 21.018 | 31 21.0 | 185 | 21.2725 | 21.2737 |
| 21.3312 | 21.3315 | 21.3325 | 21.3328 | 21.515 | 9 21.5 | 189 | 21.6655 | 21.6678 |
| 21.9601 | 21.9611 | 22.2820 | 22.2856 | 22.550 | 4 22.5 | 511 | 22.5526 | 22.5535 |
| 23.0600 | 23.0614 | 23.1889 | 23.1903 | 23.190 | 8 23.1 | 921 | 23.4700 | 23.4732 |
| 23.8273 | 23.8305 | 24.0252 | 24.0267 | 24.029 | 1 24.0 | 305 | 24.1582 | 24.1637 |
| 24.5349 | 24.5395 | 26.0152 | 26.0196 | 26.261 | 6 26.2 | 645 | 26.3507 | 26.3546 |
| 26.3552 | 26.3591 | 26.5737 | 26.5802 | 26.581 | 4 26.5 | 824 | | |

occupation numbers

| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |

| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
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| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0004 | 1.0004 | 1.0004 | 1.0004 |
| 1.0029 | 1.0030 | 1.0231 | 1.0232 | 1.0412 | 1.0414 | 0.9107 | 0.9072 |
| 0.7203 | 0.7192 | 0.7155 | 0.7145 | 0.1409 | 0.1354 | 0.0121 | 0.0115 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | | |

k =-0.4967 0.3390-0.5304 (12836 PWs) bands (ev):

-65.6557 -65.6556 -65.6554 -65.6552 -65.6264 -65.6264 -65.6263 -65.6262 -65.6262 -65.6262 -65.6261 -65.6260 -65.5994 -65.5992 -65.5990 -65.5989 -31.8065 -31.8064 -31.8059 -31.8057 -31.8009 -31.8008 -31.8003 -31.8001 -31.7853 -31.7850 -31.7838 -31.7835 -31.7772 -31.7772 -31.7761 -31.7760 -31.6963 -31.6962 -31.6873 -31.6872 -31.6594 -31.6593 -31.6592 -31.6591 -31.6566 -31.6565 -31.6565 -31.6564 -31.6389 -31.6388 -31.6270 -31.6269 -31.6061 -31.6061 -31.5961 -31.5960 -31.5940 -31.5940 -31.5938 -31.5936 -31.5633 -31.5632 -31.5628 -31.5627 -31.5544 -31.5543 -31.5539 -31.5537 -19.9727 -19.9725 -19.9694 -19.9692 -19.9060 -19.9058 -19.9058 -19.9056 -0.0383 -0.0371 -0.0371 -0.0359 0.2892 0.2917 0.3137 0.31580.7691 0.7710 0.7710 0.7729 0.8197 0.8198 0.9403 0.9413 1.1121 1.1125 1.1126 1.1129 1.2076 1.2080 1.2128 1.2132 6.6834 6.6840 7.2124 7.2127 7.3647 7.3654 7.3655 7.3662 8.8402 8.8417 9.5225 9.5236 9.5237 9.5248 9.6868 9.6887 13.2941 13.2953 13.9837 13.9845 13.9847 13.9854 14.1793 14.1795 14.8827 14.8838 14.8846 14.8856 15.2435 15.2446 15.5810 15.5816 15.7232 15.7234 15.7255 15.7257 16.0195 16.0211 16.3145 16.3179 16.3245 16.3262 16.6005 16.6026 16.6028 16.6051 16.8664 16.8687 17.0006 17.003017.0199 17.0229 17.0238 17.0267 17.7166 17.7208 17.7539 17.7570 17.9053 17.9071 17.9071 17.9088 17.9684 17.9706 18.0637 18.0642 18.2297 18.2297 18.6672 18.6677 18.6679 18.6684 18.9901 18.9902 18.9912 18.9914 19.1098 19.1110 19.2072 19.2074 19.2079 19.2079 19.4532 19.4548 19.5482 19.5503 19.9200 19.9209 20.2274 20.2298 20.2298 20.2303 20.2309 20.2324 20.3917 20.3933 20.5502 20.5507 20.5512 20.5514 20.7629 20.7633 20.7634 20.7637 20.9733 21.0181 21.0185 21.2749 21.2761 20.8494 20.8507 20.9730 21.3328 21.5158 21.5188 21.6656 21.6679 21.3313 21.3315 21.3326 21.9601 21.9610 22.2820 22.2856 22.5504 22.5511 22.5526 22.5535 23.0600 23.0615 23.1890 23.1903 23.1909 23.1921 23.4704 23.4736 24.0267 24.0291 24.0305 24.1584 24.1639 23.8273 23.830624.0251 24.5349 24.5396 26.0152 26.0195 26.2613 26.2643 26.3507 26.3546 26.3552 26.3590 26.5738 26.5807 26.5834 26.5892

occupation numbers

| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |

| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
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| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
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| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
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| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0004 | 1.0004 | 1.0004 | 1.0004 |
| 1.0029 | 1.0030 | 1.0239 | 1.0240 | 1.0412 | 1.0414 | 0.9039 | 0.9005 |
| 0.7201 | 0.7191 | 0.7154 | 0.7143 | 0.1410 | 0.1356 | 0.0121 | 0.0115 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | | |

k =-0.5026-0.2624-1.0607 (12866 PWs) bands (ev):
-65.6470 -65.6470 -65.6467 -65.6467 -65.6465 -65.6464 -65.6463 -65.6462 -65.6081 -65.6081 -65.6073 -65.6073 -65.6072 -65.6071 -65.6070 -65.6069 -31.8479 -31.8478 -31.8477 -31.8476 -31.8458 -31.8458 -31.8446 -31.8446 -31.7051 -31.7051 -31.7050 -31.7050 -31.6987 -31.6986 -31.6986 -31.6985 -31.6882 -31.6882 -31.6848 -31.6848 -31.6813 -31.6813 -31.6756 -31.6752 -31.6752 -31.6748 -31.6669 -31.6668 -31.6667 -31.6666 -31.6652 -31.6651 -31.6601 -31.6600 -31.6422 -31.6422 -31.6344 -31.6340 -31.6339 -31.6335 -31.5415 -31.5414 -31.5336 -31.5335 -31.5334 -31.5333 -31.5326 -31.5325 -19.9402 -19.9402 -19.9389 -19.9386 -19.9386 -19.9382 -19.9370 -19.9369 0.3370 0.3373 0.3645 0.3651 0.3652 0.3657 0.3976 0.3978 0.6865 0.6867 0.6944 0.6964 0.6965 0.6984 0.7067 0.7069 0.9361 0.9362 0.9947 0.9956 0.9957 0.9967 1.0497 1.0497 7.0450 7.0450 7.2486 7.2493 7.2494 7.2501 7.5086 7.5086 8.9032 8.9032 9.3811 9.3825 9.3836 9.3850 9.9629 9.9630 13.0788 13.0789 14.1227 14.1235 14.1236 14.1244 14.8435 14.8435 14.8849 14.8849 14.9672 14.9688 14.9689 14.9705 15.3964 15.3965 15.5898 15.5915 15.5921 15.5938 15.7268 15.7268 15.8755 15.8755 16.3959 16.6892 16.6912 16.6918 16.6938 16.0492 16.0492 16.3959 16.8571 16.8571 17.2591 17.2617 17.2619 17.2643 17.6405 17.6433 17.6436 17.6463 17.6744 17.6745 18.0921 18.0921 18.2817 18.2817 18.3959 18.3963 18.4479 18.4481 18.5261 18.5261 18.5441 18.5443 19.0491 19.0503 19.0508 19.0668 19.0668 18.5451 18.5454 19.0485 19.2942 19.2942 19.4624 19.4637 19.4639 19.4652 19.7652 19.7652 20.3402 20.7704 20.7704 20.7730 20.7741 20.3273 20.3273 20.3402 20.8023 20.8054 20.8057 20.8063 20.8065 20.7745 20.7755 20.8023 20.8331 20.8331 20.9282 20.9300 20.9314 20.9331 21.0165 21.0165 21.3400 21.3416 21.3446 21.3462 21.4255 21.4256 21.9031 21.9031 22.1174 22.1174 22.2132 22.2150 22.2167 22.2187 22.8819 22.8819 22.9924 22.9931 22.9934 22.9942 23.0132 23.0132 23.5824 23.5826 23.7144 23.7144 24.4413 24.4414 24.5557 24.5557 24.8327 24.8340

24.8353 24.8366 25.4469 25.4540 25.4548 25.4620 25.8895 25.8896 26.2297 26.2328 26.2332 26.2364 26.5096 26.5096

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| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0005 | 1.0005 | 1.0005 | 1.0005 |
| 1.0005 | 1.0006 | 1.0010 | 1.0010 | 1.0011 | 1.0011 | 1.0011 | 1.0011 |
| 1.0021 | 1.0021 | 1.0123 | 1.0126 | 1.0129 | 1.0133 | 1.0405 | 1.0405 |
| 0.6883 | 0.6823 | 0.6711 | 0.6652 | 0.3756 | 0.3755 | 0.0000 | 0.0000 |

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k =-0.5026-0.2624-2.1214 (12848 PWs) bands (ev):

-65.6669 -65.6668 -65.6276 -65.6276 -65.6273 -65.6273 -65.6270 -65.6270 -65.6267 -65.6267 -65.6264 -65.6263 -65.6262 -65.6262 -65.5869 -65.5868 -31.8730 -31.8729 -31.8723 -31.8722 -31.8080 -31.8079 -31.8073 -31.8072 -31.6981 -31.6981 -31.6981 -31.6981 -31.6963 -31.6959 -31.6929 -31.6929 -31.6929 -31.6929 -31.6914 -31.6914 -31.6913 -31.6913 -31.6819 -31.6819 -31.6818 -31.6818 -31.6623 -31.6623 -31.6619 -31.6619 -31.6618 -31.6618 -31.6615 -31.6614 -31.6586 -31.6585 -31.6581 -31.6581 -31.6044 -31.6040 -31.5520 -31.5519 -31.5516 -31.5515 -31.5047 -31.5046 -31.5040 -31.5040 -20.0051 -20.0051 -19.9364 -19.9364 -19.9364 -19.9364 -19.8750 -19.8750 -0.3229 -0.3229 -0.3229 -0.3228 0.3014 0.3016 0.3016 0.3018 0.7352 0.7360 1.0240 1.0241 1.0241 1.0243 1.1239 1.1239 1.1242 1.1243 1.2026 1.2026 1.2996 1.2997 1.2997 1.2997 5.7818 5.7818 6.5207 6.5207 8.1695 8.1697 8.1697 8.1698 9.0868 9.0872 9.0874 9.0878 9.2522 9.2552 10.1548 10.1548 13.3732 13.373413.3743 13.3745 13.4556 13.4568 14.2968 14.2970 14.2973 14.297515.0006 15.0011 15.0013 15.0018 15.3242 15.3242 15.6748 15.674915.6750 15.6751 16.3184 16.3186 16.3192 16.3195 16.8900 16.890016.8901 16.8902 17.1900 17.1905 17.1928 17.1934 17.2860 17.291217.3876 17.3877 17.3877 17.3878 17.6849 17.6863 17.7085 17.708517.7481 17.7485 17.7496 17.7502 17.9316 17.9317 17.9321 17.932218.1243 18.1280 18.7792 18.7799 18.7801 18.7809 18,7869 18,787318,7878 18.7881 19.0230 19.0231 19.0231 19.0231 19.2633 19.2633 19.4948 19.4950 19.4951 19.4953 19.6351 19.6354

20.023020.023120.023220.023320.096820.096920.096920.097020.466320.466420.467020.467121.004221.004321.022421.022421.080821.082321.082521.083921.193121.193821.193921.194621.210021.210121.211821.211821.263921.264621.265521.266221.544721.547221.730121.732422.901522.901723.068323.068523.069323.069523.330023.330023.991223.993623.993723.996124.256324.256724.259024.259424.571724.573524.573624.575324.720024.721426.228726.228826.230826.231026.481626.485226.485226.488726.572726.583027.000527.001527.0015

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| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0353 | 1.0354 | 1.0431 | 1.0431 |
| 1.0698 | 1.0705 | 1.0706 | 1.0711 | 1.0577 | 1.0571 | 1.0570 | 1.0562 |
| 1.0383 | 1.0383 | 1.0359 | 1.0358 | 0.9332 | 0.9315 | 0.9292 | 0.9274 |
| 0.0953 | 0.0919 | 0.0030 | 0.0029 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
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| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | | |

k = 0.0058 0.6014-0.5304 (12838 PWs) bands (ev):

-65.6557 -65.6557 -65.6554 -65.6554 -65.6264 -65.6264 -65.6263 -65.6262 -65.6262 -65.6262 -65.6261 -65.6260 -65.5993 -65.5993 -65.5990 -65.5989 -31.8065 -31.8064 -31.8058 -31.8058 -31.8009 -31.8008 -31.8002 -31.8002 -31.7852 -31.7851 -31.7837 -31.7836 -31.7772 -31.7772 -31.7761 -31.7760 -31.6964 -31.6962 -31.6878 -31.6876 -31.6594 -31.6593 -31.6592 -31.6591 -31.6566 -31.6565 -31.6565 -31.6564 -31.6390 -31.6388 -31.6271 -31.6269 -31.6061 -31.6061 -31.5989 -31.5989 -31.5942 -31.5941 -31.5938 -31.5937 -31.5633 -31.5632 -31.5627 -31.5627 -31.5543 -31.5543 -31.5538 -31.5538 -19.9727 -19.9725 -19.9694 -19.9692 -19.9060 -19.9058 -19.9058 -19.9056 -0.0383 -0.0371 -0.0371 -0.0359 0.2894 0.2915 0.3135 0.3160 0.7691 0.7710 0.7710 0.7729 0.8192 0.8203 0.9407 0.9408 1.1121 1.1125 1.1126 1.1129 1.2076 1.2080 1.2128 1.2132 6.6836 6.6838 7.2120 7.2131 7.3647 7.3654 7.3655 7.3662 8.8398 8.8421 9.5224 9.5235 9.5237 9.5249 9.6864 9.6889 13.2932 13.2955 13.9834 13.9844 13.9849 13.9857 14.1793 14.1795 14.8834 14.8839 14.8845 14.8849 15.2435 15.2445 15.5801 15.5824

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| 15.7222 | 15.7239 | 15.7250 | 15.7268 | 16.0202 | 16.0204 | 16.3154 | 16.3169 |
|---------|---------|---------|---------|---------|---------|---------|---------|
| 16.3243 | 16.3264 | 16.5987 | 16.6023 | 16.6032 | 16.6067 | 16.8657 | 16.8695 |
| 17.0005 | 17.0030 | 17.0215 | 17.0232 | 17.0234 | 17.0252 | 17.7165 | 17.7209 |
| 17.7551 | 17.7552 | 17.9061 | 17.9066 | 17.9076 | 17.9080 | 17.9682 | 17.9706 |
| 18.0637 | 18.0641 | 18.2276 | 18.2277 | 18.6674 | 18.6675 | 18.6680 | 18.6681 |
| 18.9895 | 18.9904 | 18.9911 | 18.9918 | 19.1093 | 19.1116 | 19.2073 | 19.2074 |
| 19.2076 | 19.2081 | 19.4526 | 19.4544 | 19.5485 | 19.5501 | 19.9193 | 19.9205 |
| 20.2287 | 20.2295 | 20.2300 | 20.2304 | 20.2306 | 20.2312 | 20.3898 | 20.3912 |
| 20.5505 | 20.5508 | 20.5509 | 20.5513 | 20.7626 | 20.7634 | 20.7634 | 20.7641 |
| 20.8494 | 20.8507 | 20.9708 | 20.9708 | 21.0182 | 21.0184 | 21.2722 | 21.2739 |
| 21.3308 | 21.3318 | 21.3322 | 21.3332 | 21.5148 | 21.5199 | 21.6655 | 21.6679 |
| 21.9601 | 21.9611 | 22.2821 | 22.2855 | 22.5505 | 22.5516 | 22.5522 | 22.5533 |
| 23.0594 | 23.0619 | 23.1900 | 23.1904 | 23.1906 | 23.1911 | 23.4699 | 23.4733 |
| 23.8282 | 23.8295 | 24.0246 | 24.0278 | 24.0279 | 24.0312 | 24.1588 | 24.1632 |
| 24.5354 | 24.5391 | 26.0159 | 26.0189 | 26.2606 | 26.2654 | 26.3519 | 26.3541 |
| 26.3558 | 26.3579 | 26.5763 | 26.5802 | 26.5835 | 26.5846 | | |

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| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0004 | 1.0004 | 1.0004 | 1.0004 |
| 1.0029 | 1.0030 | 1.0232 | 1.0232 | 1.0413 | 1.0414 | 0.9113 | 0.9066 |
| 0.7219 | 0.7180 | 0.7166 | 0.7130 | 0.1427 | 0.1336 | 0.0121 | 0.0115 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
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k = 0.4967-0.3390-0.5304 (12836 PWs) bands (ev):

-65.6557 -65.6557 -65.6553 -65.6553 -65.6264 -65.6264 -65.6263 -65.6262 -65.6262 -65.6262 -65.6261 -65.6260 -65.5993 -65.5993 -65.5990 -65.5989 -31.8065 -31.8064 -31.8058 -31.8058 -31.8009 -31.8008 -31.8002 -31.8002 -31.7852 -31.7851 -31.7836 -31.7836 -31.7772 -31.7772 -31.7761 -31.7760 -31.6964 -31.6962 -31.6873 -31.6872 -31.6594 -31.6593 -31.6592 -31.6591 -31.6566 -31.6565 -31.6565 -31.6563 -31.6389 -31.6388 -31.6271 -31.6269 -31.6061 -31.6061 -31.5961 -31.5960 -31.5940 -31.5940 -31.5938 -31.5937 -31.5633 -31.5632 -31.5628 -31.5627 -31.5544 -31.5543 -31.5538 -31.5538 -19.9727 -19.9725 -19.9694 -19.9692 -19.9060 -19.9058 -19.9058 -19.9056

| -0.0383 | -0.0371 | -0.0371 | -0.0359 | 0.2894 | 0.2915 | 0.3 | 135 0.3 | 160 |
|---------|---------|---------|---------|----------|----------|-------|---------|---------|
| 0.7691 | 0.7710 | 0.7710 | 0.7729 | 0.8191 | 0.8203 | 0.94 | 08 0.9 | 408 |
| 1.1121 | 1.1125 | 1.1126 | 1.1129 | 1.2076 | 1.2080 | 1.21 | 28 1.2 | 132 |
| 6.6836 | 6.6838 | 7.2120 | 7.2131 | 7.3647 | 7.3654 | 7.36 | 55 7.3 | 662 |
| 8.8398 | 8.8421 | 9.5224 | 9.5235 | 9.5237 | 9.5249 | 9.68 | 65 9.6 | 890 |
| 13.2935 | 13.2959 | 13.9834 | 13.984 | 4 13.984 | 49 13.98 | 857 1 | 4.1793 | 14.1795 |
| 14.8834 | 14.8839 | 14.8845 | 14.884 | 9 15.243 | 35 15.24 | 445 1 | 5.5801 | 15.5824 |
| 15.7222 | 15.7239 | 15.7250 | 15.726 | 7 16.020 | 02 16.02 | 204 1 | 6.3155 | 16.3170 |
| 16.3243 | 16.3263 | 16.5987 | 16.602 | 3 16.603 | 32 16.60 |)67 1 | 6.8657 | 16.8695 |
| 17.0005 | 17.0030 | 17.0215 | 17.023 | 3 17.023 | 34 17.02 | 252 1 | 7.7165 | 17.7209 |
| 17.7554 | 17.7555 | 17.9061 | 17.906 | 5 17.90 | 76 17.90 | 080 1 | 7.9683 | 17.9707 |
| 18.0638 | 18.0641 | 18.2297 | 18.229 | 8 18.66 | 75 18.60 | 575 1 | 8.6680 | 18.6681 |
| 18.9895 | 18.9904 | 18.9912 | 18.991 | 8 19.10 | 92 19.1 | 115 1 | 9.2073 | 19.2074 |
| 19.2077 | 19.2081 | 19.4531 | 19.454 | 9 19.548 | 85 19.55 | 501 1 | 9.9199 | 19.9210 |
| 20.2287 | 20.2296 | 20.2300 | 20.230 | 4 20.230 | 07 20.23 | 312 2 | 0.3918 | 20.3932 |
| 20.5505 | 20.5507 | 20.5508 | 20.551 | 3 20.762 | 26 20.76 | 533 2 | 0.7633 | 20.7641 |
| 20.8494 | 20.8507 | 20.9731 | 20.973 | 1 21.018 | 82 21.02 | 184 2 | 1.2747 | 21.2764 |
| 21.3308 | 21.3319 | 21.3323 | 21.333 | 3 21.514 | 48 21.5 | 199 2 | 1.6655 | 21.6680 |
| 21.9601 | 21.9611 | 22.2821 | 22.285 | 5 22.550 | 05 22.55 | 515 2 | 2.5522 | 22.5533 |
| 23.0595 | 23.0620 | 23.1900 | 23.190 | 4 23.19 | 06 23.19 | 911 2 | 3.4703 | 23.4737 |
| 23.8283 | 23.8296 | 24.0246 | 24.027 | 7 24.02 | 79 24.03 | 312 2 | 4.1589 | 24.1633 |
| 24.5354 | 24.5391 | 26.0158 | 26.018 | 9 26.26 | 04 26.26 | 552 2 | 6.3518 | 26.3542 |
| 26.3559 | 26.3578 | 26.5775 | 26.580 | 3 26.58 | 11 26.58 | 864 | | |

| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |

| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0004 | 1.0004 | 1.0004 | 1.0004 |
| 1.0029 | 1.0030 | 1.0239 | 1.0239 | 1.0413 | 1.0414 | 0.9046 | 0.8999 |
| 0.7217 | 0.7179 | 0.7165 | 0.7128 | 0.1429 | 0.1337 | 0.0121 | 0.0115 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | | |

the Fermi energy is 21.4181 ev

! total energy = -12416.58858522 Ry Harris-Foulkes estimate = -12416.58858522 Ry

134

estimated scf accuracy < 8.2E-10 Ry

total all-electron energy = -286580.605066 Ry

The total energy is the sum of the following terms:

| one-electron contribution = -2345.90180039 | Ry |
|--|------|
| hartree contribution $=$ 1525.02901527 | Ry |
| xc contribution = -1156.46991273 | Ry |
| ewald contribution $= -3259.17105260$ | Ry |
| one-center paw contrib. = -7180.07686909 R | у |
| \rightarrow PAW hartree energy AE = 46.38132384 | 4 Ry |
| \rightarrow PAW hartree energy PS = -46.31023689 | Ry |
| -> PAW xc energy AE = -483.05709339 | Ry |
| \rightarrow PAW xc energy PS = 63.16021088 H | Rу |
| \rightarrow total E_H with PAW = 1525.10010221 | Ry |
| -> total E_XC with PAW = -1576.36679523 | Ry |
| smearing contrib. $(-TS) = 0.00203433 \text{ Ry}$ | 7 |

convergence has been achieved in 50 iterations

Forces acting on atoms (cartesian axes, Ry/au):

| atom | 1 type | 1 | force = | 0.00561713 | 0.00293390 | -0.00509014 |
|------|--------|---|---------|-------------|-------------|-------------|
| atom | 2 type | 1 | force = | 0.00011904 | -0.00003720 | -0.00002775 |
| atom | 3 type | 1 | force = | 0.00003822 | 0.00011738 | -0.00003084 |
| atom | 4 type | 1 | force = | -0.00019394 | -0.00010005 | 0.00033869 |
| atom | 5 type | 1 | force = | 0.00011621 | 0.00006377 | -0.00003894 |
| atom | 6 type | 1 | force = | 0.00022485 | -0.00016069 | 0.00018784 |
| atom | 7 type | 1 | force = | -0.00000642 | 0.00027250 | 0.00018777 |
| atom | 8 type | 1 | force = | 0.00003820 | 0.00001949 | 0.00013537 |

| atom | 9 type | 2 force $=$ | -0.00045996 | 0.00016075 -0.00036639 |
|------|---------|-------------|-------------|---------------------------|
| atom | 10 type | 2 force = | -0.00074551 | 0.00028266 0.00058733 |
| atom | 11 type | 2 force = | -0.00009640 | -0.00000656 0.00005108 |
| atom | 12 type | 2 force = | -0.00008104 | 0.00003130 -0.00005408 |
| atom | 13 type | 2 force = | -0.00001605 | -0.00008853 -0.00005695 |
| atom | 14 type | 2 force = | -0.00018591 | -0.00075441 0.00057281 |
| atom | 15 type | 2 force = | -0.00005611 | -0.00007123 0.00005126 |
| atom | 16 type | 2 force = | -0.00012873 | -0.00047367 -0.00036933 |
| atom | 17 type | 2 force = | -0.00013140 | -0.00046639 -0.00039050 |
| atom | 18 type | 2 force = | -0.00005883 | $-0.00007442\ 0.00002927$ |
| atom | 19 type | 2 force = | -0.00019207 | -0.00077454 0.00056710 |
| atom | 20 type | 2 force = | -0.00001838 | -0.00008440 -0.00007483 |
| atom | 21 type | 2 force = | -0.00008248 | 0.00003483 -0.00007648 |
| atom | 22 type | 2 force = | -0.00009323 | -0.00000605 0.00002891 |
| atom | 23 type | 2 force = | -0.00072379 | 0.00028218 0.00054768 |
| atom | 24 type | 2 force = | -0.00045936 | 0.00016387 -0.00039268 |
| atom | 25 type | 3 force = | 0.00006548 | 0.00002004 -0.00000714 |
| atom | 26 type | 3 force = | 0.00024475 | -0.00096148 -0.00006940 |
| atom | 27 type | 3 force = | -0.00063575 | 0.00072787 -0.00006644 |
| atom | 28 type | 3 force = | -0.00005395 | -0.00004075 0.00001595 |
| atom | 29 type | 3 force = | 0.00028143 | 0.00013068 0.00000295 |
| atom | 30 type | 3 force = | -0.00009885 | -0.00004060 0.00002075 |
| atom | 31 type | 3 force = | -0.00007659 | -0.00008345 0.00002219 |
| atom | 32 type | 3 force = | -0.00066179 | -0.00035850 0.00188929 |
| atom | 33 type | 3 force = | -0.00011812 | -0.00004772 0.00001829 |
| atom | 34 type | 3 force = | -0.00070573 | 0.00073135 -0.00007341 |
| atom | 35 type | 3 force = | 0.00018680 | -0.00097530 -0.00007355 |
| atom | 36 type | 3 force = | -0.00000416 | 0.00001359 -0.00000676 |
| atom | 37 type | 3 force = | -0.00074581 | -0.00037295 0.00195618 |
| atom | 38 type | 3 force = | -0.00014782 | -0.00008881 0.00001990 |
| atom | 39 type | 3 force = | -0.00016754 | -0.00004633 0.00002144 |

atom 40 type 3 force = 0.00021358 0.00012787 0.00001360 The non-local contrib. to forces

| atom | 1 type | 1 | force = | 0.00381747 | 0.00199422 | -0.00201584 |
|------|---------|---|---------|-------------|-------------|-------------|
| atom | 2 type | 1 | force = | 0.00006207 | -0.00005769 | 0.00003585 |
| atom | 3 type | 1 | force = | -0.00001106 | 0.00008281 | 0.00003304 |
| atom | 4 type | 1 | force = | -0.00001219 | -0.00000560 | 0.00010174 |
| atom | 5 type | 1 | force = | 0.00002566 | 0.00001577 | -0.00012227 |
| atom | 6 type | 1 | force = | -0.00008778 | -0.00009074 | 0.00008717 |
| atom | 7 type | 1 | force = | -0.00012691 | -0.00002311 | 0.00008694 |
| atom | 8 type | 1 | force = | 0.00002431 | 0.00001197 | 0.00003632 |
| atom | 9 type | 2 | force = | 0.00067706 | -0.00013069 | 0.00065977 |
| atom | 10 type | 2 | force = | 0.00135003 | -0.00025563 | -0.00061869 |
| atom | 11 type | 2 | force = | 0.00015202 | -0.00007367 | 0.00002098 |
| atom | 12 type | 2 | force = | 0.00013602 | -0.00002848 | 0.00024182 |
| atom | 13 type | 2 | force = | 0.00005673 | 0.00012404 | 0.00024046 |
| atom | 14 type | 2 | force = | 0.00054085 | 0.00120951 | -0.00059687 |
| atom | 15 type | 2 | force = | 0.00002134 | 0.00016927 | 0.00001523 |
| atom | 16 type | 2 | force = | 0.00028537 | 0.00064248 | 0.00067262 |
| atom | 17 type | 2 | force = | 0.00027901 | 0.00063180 | 0.00063431 |
| atom | 18 type | 2 | force = | 0.00002595 | 0.00016811 | -0.00000545 |
| atom | 19 type | 2 | force = | 0.00056220 | 0.00125309 | -0.00064595 |
| atom | 20 type | 2 | force = | 0.00005517 | 0.00012618 | 0.00021514 |
| atom | 21 type | 2 | force = | 0.00013411 | -0.00002407 | 0.00021394 |
| atom | 22 type | 2 | force = | 0.00015037 | -0.00007855 | -0.00000921 |
| atom | 23 type | 2 | force = | 0.00130156 | -0.00024883 | -0.00062422 |
| atom | 24 type | 2 | force = | 0.00069048 | -0.00013276 | 0.00064521 |
| atom | 25 type | 3 | force = | -0.08667313 | -0.04526362 | 0.00001207 |
| atom | 26 type | 3 | force = | -0.08669552 | -0.04578959 | 0.00002848 |
| atom | 27 type | 3 | force = | -0.08711625 | -0.04498164 | 0.00003061 |
| atom | 28 type | 3 | force = | -0.08650628 | -0.04517524 | 0.00003893 |
| atom | 29 type | 3 | force = | -0.08664979 | -0.04525286 | 0.00007803 |

| atom | 30 type | 3 | force = | -0.08667528 | -0.04525854 | 0.00003269 |
|--------|-----------|-----|-----------|-------------|-------------|-------------|
| atom | 31 type | 3 | force = | -0.08666899 | -0.04527043 | 0.00003377 |
| atom | 32 type | 3 | force = | -0.08715577 | -0.04551458 | 0.00097734 |
| atom | 33 type | 3 | force = | 0.08678052 | 0.04531950 | 0.00003779 |
| atom | 34 type | 3 | force = | 0.08616953 | 0.04551979 | 0.00002750 |
| atom | 35 type | 3 | force = | 0.08659682 | 0.04470333 | 0.00002744 |
| atom | 36 type | 3 | force = | 0.08661378 | 0.04523376 | 0.00001227 |
| atom | 37 type | 3 | force = | 0.08611761 | 0.04497499 | 0.00101636 |
| atom | 38 type | 3 | force = | 0.08661519 | 0.04522717 | 0.00003209 |
| atom | 39 type | 3 | force = | 0.08661130 | 0.04523799 | 0.00003333 |
| atom | 40 type | 3 | force = | 0.08664073 | 0.04524804 | 0.00008388 |
| The id | onic cont | rit | oution to | forces | | |
| atom | 1 type | 1 | force = | 0.34125760 | 0.17816868 | -0.07613463 |
| atom | 2 type | 1 | force = | -0.01857216 | -0.00237680 | -0.00055253 |
| atom | 3 type | 1 | force = | -0.01256656 | -0.01388080 | -0.00055272 |
| atom | 4 type | 1 | force = | 0.01155184 | 0.00603140 | 0.00824885 |
| atom | 5 type | 1 | force = | -0.01864304 | -0.00973328 | 0.00718930 |
| atom | 6 type | 1 | force = | 0.03341203 | -0.00772887 | 0.01172786 |
| atom | 7 type | 1 | force = | 0.01275646 | 0.03183390 | 0.01172897 |
| atom | 8 type | 1 | force = | -0.01249461 | -0.00652342 | -0.00578698 |
| atom | 9 type | 2 | force = | -0.03047389 | 0.01094674 | -0.03958320 |
| atom | 10 type | 2 | force = | -0.07628440 | 0.01519472 | 0.03269252 |
| atom | 11 type | 2 | force = | 0.00363563 | -0.01056684 | 0.00031358 |
| atom | 12 type | 2 | force = | -0.00679536 | -0.00429859 | 0.01187954 |
| atom | 13 type | 2 | force = | -0.00727755 | -0.00313463 | 0.01198312 |
| atom | 14 type | 2 | force = | -0.03110001 | -0.07053710 | 0.03244318 |
| atom | 15 type | 2 | force = | -0.00668329 | 0.00890771 | 0.00026347 |
| atom | 16 type | 2 | force = | -0.00810129 | -0.03112432 | -0.03984527 |
| atom | 17 type | 2 | force = | -0.00843675 | -0.03126183 | -0.04052472 |
| atom | 18 type | 2 | force = | -0.00659169 | 0.00902303 | -0.00062673 |
| atom | 19 type | 2 | force = | -0.03113847 | -0.07127954 | 0.03175338 |

| atom | 20 type | 2 force = | -0.00741143 | -0.00311873 | 0.01093960 |
|--------|-----------|---------------|--------------|-------------|-------------|
| atom | 21 type | 2 force = | -0.00673154 | -0.00417946 | 0.01104225 |
| atom | 22 type | 2 force = | 0.00348900 | -0.01057591 | -0.00067701 |
| atom | 23 type | 2 force = | -0.07565290 | 0.01480208 | 0.03150154 |
| atom | 24 type | 2 force = | -0.03016898 | 0.01114356 | -0.04078455 |
| atom | 25 type | 3 force = | -10.44666878 | -5.45436944 | 0.00071033 |
| atom | 26 type | 3 force = | -10.42834038 | -5.46244710 | -0.00462258 |
| atom | 27 type | 3 force = | -10.44282055 | -5.43471334 | -0.00462235 |
| atom | 28 type | 3 force = | -10.45660145 | -5.45955505 | -0.00230439 |
| atom | 29 type | 3 force = | -10.42814557 | -5.44469872 | -0.00291098 |
| atom | 30 type | 3 force = | -10.44797348 | -5.45361008 | 0.00049312 |
| atom | 31 type | 3 force = | -10.44679153 | -5.45587414 | 0.00049323 |
| atom | 32 type | 3 force = | -10.44295190 | -5.45242879 | 0.02827738 |
| atom | 33 type | 3 force = | 10.42711787 | 5.44416217 | -0.00224985 |
| atom | 34 type | 3 force = | 10.44099173 | 5.46898600 | -0.00467857 |
| atom | 35 type | 3 force = | 10.45541741 | 5.44135663 | -0.00467880 |
| atom | 36 type | 3 force = | 10.43694947 | 5.44929501 | 0.00069378 |
| atom | 37 type | 3 force = | 10.44078353 | 5.45129684 | 0.02852350 |
| atom | 38 type | 3 force = | 10.43682534 | 5.44781977 | 0.00048442 |
| atom | 39 type | 3 force = | 10.43566815 | 5.45003639 | 0.00048431 |
| atom | 40 type | 3 force = | 10.45556152 | 5.45901212 | -0.00273137 |
| The lo | ocal cont | ribution to f | orces | | |
| atom | 1 type | 1 force = | -0.33900676 | -0.17698927 | 0.07269618 |
| atom | 2 type | 1 force = | 0.01864842 | 0.00237377 | 0.00050453 |
| atom | 3 type | 1 force = | 0.01261117 | 0.01393843 | 0.00049095 |
| atom | 4 type | 1 force = | -0.01172385 | -0.00611675 | -0.00800494 |
| atom | 5 type | 1 force = | 0.01873207 | 0.00979198 | -0.00714286 |
| atom | 6 type | 1 force = | -0.03309401 | 0.00764501 | -0.01160938 |
| atom | 7 type | 1 force = | -0.01265522 | -0.03153998 | -0.01161035 |
| atom | 8 type | 1 force = | 0.01251804 | 0.00653224 | 0.00590145 |
| atom | 9 type | 2 force = | 0.02932022 | -0.01068189 | 0.03855586 |

| atom | 10 type | 2 | force = | 0.07414192 | -0.01463843 | -0.03147111 |
|------|---------|---|---------|--------------|-------------|-------------|
| atom | 11 type | 2 | force = | -0.00385567 | 0.01062782 | -0.00027419 |
| atom | 12 type | 2 | force = | 0.00655897 | 0.00438055 | -0.01217552 |
| atom | 13 type | 2 | force = | 0.00721812 | 0.00292709 | -0.01225516 |
| atom | 14 type | 2 | force = | 0.03033325 | 0.06853636 | -0.03128210 |
| atom | 15 type | 2 | force = | 0.00659918 | -0.00915777 | -0.00019641 |
| atom | 16 type | 2 | force = | 0.00768157 | 0.02999766 | 0.03877661 |
| atom | 17 type | 2 | force = | 0.00801056 | 0.03013120 | 0.03947906 |
| atom | 18 type | 2 | force = | 0.00651829 | -0.00925526 | 0.00065383 |
| atom | 19 type | 2 | force = | 0.03036762 | 0.06922051 | -0.03052972 |
| atom | 20 type | 2 | force = | 0.00732734 | 0.00291079 | -0.01122896 |
| atom | 21 type | 2 | force = | 0.00652741 | 0.00424194 | -0.01133510 |
| atom | 22 type | 2 | force = | -0.00373909 | 0.01063660 | 0.00070250 |
| atom | 23 type | 2 | force = | 0.07356955 | -0.01427483 | -0.03030960 |
| atom | 24 type | 2 | force = | 0.02900469 | -0.01083606 | 0.03972675 |
| atom | 25 type | 3 | force = | 10.50291626 | 5.48373174 | -0.00072683 |
| atom | 26 type | 3 | force = | 10.48480792 | 5.49118455 | 0.00450001 |
| atom | 27 type | 3 | force = | 10.49868909 | 5.46461197 | 0.00451455 |
| atom | 28 type | 3 | force = | 10.51255619 | 5.48877294 | 0.00228187 |
| atom | 29 type | 3 | force = | 10.48461817 | 5.47416891 | 0.00285663 |
| atom | 30 type | 3 | force = | 10.50407246 | 5.48290610 | -0.00050532 |
| atom | 31 type | 3 | force = | 10.50290753 | 5.48513962 | -0.00049784 |
| atom | 32 type | 3 | force = | 10.49881992 | 5.48159989 | -0.02703493 |
| atom | 33 type | 3 | force = | -10.48353349 | -5.47361405 | 0.00223082 |
| atom | 34 type | 3 | force = | -10.49750570 | -5.49774170 | 0.00455896 |
| atom | 35 type | 3 | force = | -10.51131045 | -5.47128802 | 0.00455897 |
| atom | 36 type | 3 | force = | -10.49309336 | -5.47859601 | -0.00070944 |
| atom | 37 type | 3 | force = | -10.49729524 | -5.48078854 | -0.02723862 |
| atom | 38 type | 3 | force = | -10.49310103 | -5.47721570 | -0.00049740 |
| atom | 39 type | 3 | force = | -10.49195208 | -5.47939614 | -0.00048946 |
| atom | 40 type | 3 | force = | -10.51147320 | -5.48819067 | 0.00267853 |

The core correction contribution to forces

| atom | 1 type | 1 | force = | -0.00044451 | -0.00023221 | 0.00035690 |
|------|---------|---|---------|-------------|-------------|-------------|
| atom | 2 type | 1 | force = | -0.00002601 | 0.00001446 | -0.00001138 |
| atom | 3 type | 1 | force = | -0.00000301 | -0.00002967 | -0.00001133 |
| atom | 4 type | 1 | force = | -0.0000082 | -0.00000041 | -0.00000475 |
| atom | 5 type | 1 | force = | -0.00001715 | -0.00000896 | 0.00003775 |
| atom | 6 type | 1 | force = | 0.00001517 | 0.00001513 | -0.00001566 |
| atom | 7 type | 1 | force = | 0.00002109 | 0.00000380 | -0.00001560 |
| atom | 8 type | 1 | force = | -0.00001196 | -0.00000621 | -0.00001197 |
| atom | 9 type | 2 | force = | 0.00002427 | -0.00000216 | 0.00001068 |
| atom | 10 type | 2 | force = | 0.00004458 | 0.00000135 | -0.00002158 |
| atom | 11 type | 2 | force = | -0.00000406 | -0.00000010 | -0.00000342 |
| atom | 12 type | 2 | force = | -0.00000158 | -0.00000078 | -0.00000521 |
| atom | 13 type | 2 | force = | -0.00000164 | -0.00000078 | -0.00000520 |
| atom | 14 type | 2 | force = | 0.00002658 | 0.00003534 | -0.00002145 |
| atom | 15 type | 2 | force = | -0.00000250 | -0.00000340 | -0.00000337 |
| atom | 16 type | 2 | force = | 0.00001186 | 0.00002117 | 0.00001092 |
| atom | 17 type | 2 | force = | 0.00001209 | 0.00002112 | 0.00001948 |
| atom | 18 type | 2 | force = | -0.00000244 | -0.00000329 | 0.00000531 |
| atom | 19 type | 2 | force = | 0.00002653 | 0.00003586 | -0.00001292 |
| atom | 20 type | 2 | force = | -0.00000158 | -0.0000085 | 0.00000346 |
| atom | 21 type | 2 | force = | -0.00000158 | -0.00000085 | 0.00000348 |
| atom | 22 type | 2 | force = | -0.00000416 | -0.00000010 | 0.00000537 |
| atom | 23 type | 2 | force = | 0.00004416 | 0.00000156 | -0.00001264 |
| atom | 24 type | 2 | force = | 0.00002409 | -0.00000234 | 0.00001963 |
| atom | 25 type | 3 | force = | 0.03049131 | 0.01592324 | -0.00000265 |
| atom | 26 type | 3 | force = | 0.03047065 | 0.01609273 | 0.00001591 |
| atom | 27 type | 3 | force = | 0.03061855 | 0.01580941 | 0.00001589 |
| atom | 28 type | 3 | force = | 0.03049084 | 0.01592295 | -0.00000514 |
| atom | 29 type | 3 | force = | 0.03046239 | 0.01590815 | -0.00001566 |
| atom | 30 type | 3 | force = | 0.03047744 | 0.01591865 | -0.00000138 |

| atom | 31 type | 3 force = | 0.03047958 | 0.01591456 | -0.00000140 |
|-------|------------|---------------|-------------|-------------|-------------|
| atom | 32 type | 3 force = | 0.03062542 | 0.01599324 | -0.00033263 |
| atom | 33 type | 3 force = | -0.03048482 | -0.01591986 | -0.00000494 |
| atom | 34 type | 3 force = | -0.03035698 | -0.01603362 | 0.00001646 |
| atom | 35 type | 3 force = | -0.03050514 | -0.01574988 | 0.00001650 |
| atom | 36 type | 3 force = | -0.03048380 | -0.01591935 | -0.00000266 |
| atom | 37 type | 3 force = | -0.03034713 | -0.01584803 | -0.00034061 |
| atom | 38 type | 3 force = | -0.03049517 | -0.01592790 | -0.00000139 |
| atom | 39 type | 3 force = | -0.03049736 | -0.01592376 | -0.00000142 |
| atom | 40 type | 3 force = | -0.03051360 | -0.01593489 | -0.00001799 |
| The H | lubbard co | ontrib. to fo | orces | | |
| atom | 1 type | 1 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 2 type | 1 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 3 type | 1 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 4 type | 1 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 5 type | 1 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 6 type | 1 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 7 type | 1 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 8 type | 1 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 9 type 2 | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 10 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 11 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 12 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 13 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 14 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 15 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 16 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 17 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 18 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 19 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 20 type | 2 force = | 0.00000000 | 0.00000000 | 0.00000000 |

| atom | 21 type | 2 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
|-------|----------|------|------------|-------------|-------------|-------------|
| atom | 22 type | 2 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 23 type | 2 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 24 type | 2 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 25 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 26 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 27 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 28 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 29 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 30 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 31 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 32 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 33 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 34 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 35 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 36 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 37 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 38 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 39 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| atom | 40 type | 3 | force = | 0.00000000 | 0.00000000 | 0.00000000 |
| The S | CF corre | ecti | ion term t | o forces | | |
| atom | 1 type | 1 | force = | -0.00000635 | -0.00000742 | 0.00000707 |
| atom | 2 type | 1 | force = | 0.00000705 | 0.00000916 | -0.00000441 |
| atom | 3 type | 1 | force = | 0.00000801 | 0.00000670 | 0.00000905 |
| atom | 4 type | 1 | force = | -0.00000859 | -0.00000861 | -0.00000238 |
| atom | 5 type | 1 | force = | 0.00001899 | -0.00000165 | -0.00000103 |
| atom | 6 type | 1 | force = | -0.00002024 | -0.00000114 | -0.00000232 |
| atom | 7 type | 1 | force = | -0.00000152 | -0.00000202 | -0.00000236 |
| atom | 8 type | 1 | force = | 0.00000274 | 0.00000501 | -0.00000362 |
| atom | 9 type | 2 | force = | -0.00000730 | 0.00002883 | -0.00000967 |
| atom | 10 type | 2 | force = | 0.00000268 | -0.00001928 | 0.00000601 |
| | | | | | | |

| atom | 11 type | 2 | force = | -0.00002400 | 0.00000632 | -0.00000604 |
|------|---------|---|---------|-------------|-------------|-------------|
| atom | 12 type | 2 | force = | 0.00002124 | -0.00002131 | 0.00000513 |
| atom | 13 type | 2 | force = | -0.00001138 | -0.00000416 | -0.00002035 |
| atom | 14 type | 2 | force = | 0.00001375 | 0.00000158 | 0.00002987 |
| atom | 15 type | 2 | force = | 0.00000949 | 0.00001304 | -0.00002784 |
| atom | 16 type | 2 | force = | -0.00000591 | -0.00001057 | 0.00001561 |
| atom | 17 type | 2 | force = | 0.00000400 | 0.00001142 | 0.00000119 |
| atom | 18 type | 2 | force = | -0.00000861 | -0.00000692 | 0.00000215 |
| atom | 19 type | 2 | force = | -0.00000963 | -0.00000437 | 0.00000214 |
| atom | 20 type | 2 | force = | 0.00001244 | -0.00000169 | -0.00000425 |
| atom | 21 type | 2 | force = | -0.00001055 | -0.00000264 | -0.00000123 |
| atom | 22 type | 2 | force = | 0.00001097 | 0.00001200 | 0.00000710 |
| atom | 23 type | 2 | force = | 0.00001417 | 0.00000229 | -0.00000757 |
| atom | 24 type | 2 | force = | -0.00000931 | -0.00000845 | 0.00000010 |
| atom | 25 type | 3 | force = | 0.00000014 | -0.00000180 | -0.0000024 |
| atom | 26 type | 3 | force = | 0.00000240 | -0.00000199 | 0.00000862 |
| atom | 27 type | 3 | force = | -0.00000626 | 0.00000155 | -0.00000531 |
| atom | 28 type | 3 | force = | 0.00000707 | -0.00000628 | 0.00000451 |
| atom | 29 type | 3 | force = | -0.00000345 | 0.00000530 | -0.00000525 |
| atom | 30 type | 3 | force = | 0.00000035 | 0.00000337 | 0.00000146 |
| atom | 31 type | 3 | force = | -0.00000286 | 0.00000703 | -0.00000574 |
| atom | 32 type | 3 | force = | 0.00000087 | -0.00000818 | 0.00000195 |
| atom | 33 type | 3 | force = | 0.00000213 | 0.00000461 | 0.00000430 |
| atom | 34 type | 3 | force = | -0.00000399 | 0.0000097 | 0.00000207 |
| atom | 35 type | 3 | force = | -0.00001152 | 0.00000273 | 0.00000217 |
| atom | 36 type | 3 | force = | 0.00001007 | 0.0000027 | -0.00000088 |
| atom | 37 type | 3 | force = | -0.00000425 | -0.00000813 | -0.00000461 |
| atom | 38 type | 3 | force = | 0.00000818 | 0.00000793 | 0.00000201 |
| atom | 39 type | 3 | force = | 0.00000276 | -0.00000072 | -0.00000549 |
| atom | 40 type | 3 | force = | -0.00000155 | -0.00000665 | 0.0000038 |

Total force = 0.009209 Total SCF correction = 0.000100

Computing stress (Cartesian axis) and pressure

| total stress (Ry/bohr | (kbar) | P= 61.42 | | |
|-------------------------|-------------|----------|--------------|---|
| -0.00002314 -0.00038944 | -0.00000004 | -3.40 | -57.29 -0.01 | |
| -0.00038944 0.00051353 | -0.00000002 | -57.29 | 75.54 -0.00 | |
| -0.00000004 -0.00000002 | 0.00076217 | -0.01 | -0.00 112.12 | 2 |

kinetic stress (kbar) 52416.59 -45.06 -0.01 -45.06 52479.68 -0.00 -0.01 -0.00 52505.87

local stress (kbar) 30493.19 31310.00 0.02 31310.00 -13131.72 0.01 0.02 0.01 -29470.87

nonloc. stress (kbar) -9459.98 -51.58 0.00 -51.58 -9388.92 0.00 0.00 0.00 -9357.10

hartree stress (kbar) 8486.11 -14858.62 0.00 -14858.62 29188.51 0.00

0.00 0.00 36943.04

exc-cor stress (kbar) 17993.88 -1.69 -0.00 -1.69 17996.23 -0.00 -0.00 -0.00 17997.12

corecor stress (kbar) -28674.67 4.95 0.00

4.95 -28681.570.000.000.00 -28684.18

ewald stress (kbar) -71258.52 -16415.28 -0.02 -16415.28 -48386.67 -0.01 -0.02 -0.01 -39821.76

| hubbard stress (kbar) | 0.00 | 0.00 | 0.00 |
|-----------------------|------|------|------|
| 0.00 | 0.00 | 0.00 | |
| 0.00 | 0.00 | 0.00 | |
| | | | |
| london stress (kbar) | 0.00 | 0.00 | 0.00 |
| 0.00 | 0.00 | 0.00 | |
| 0.00 | 0.00 | 0.00 | |
| | | | |
| DFT-D3 stress (kbar) | 0.00 | 0.00 | 0.00 |
| 0.00 | 0.00 | 0.00 | |
| 0.00 | 0.00 | 0.00 | |
| | | | |
| XDM stress (kbar) | 0.00 | 0.00 | 0.00 |
| 0.00 | 0.00 | 0.00 | |
| 0.00 | 0.00 | 0.00 | |
| | | | |
| dft-nl stress (kbar) | 0.00 | 0.00 | 0.00 |
| 0.00 | 0.00 | 0.00 | |
| 0.00 | 0.00 | 0.00 | |
| | | | |
| TS-vdW stress (kbar) | 0.00 | 0.00 | 0.00 |
| 0.00 | 0.00 | 0.00 | |
| 0.00 | 0.00 | 0.00 | |

Writing output data file EuFe2As2.save/

| init_run | : | 3.38s CPU | 3.49s WALL (| 1 calls) |
|-----------|---|-------------|----------------|----------|
| electrons | : | 317.17s CPU | 323.12s WALL (| 1 calls) |
| forces | : | 1.15s CPU | 1.16s WALL (| 1 calls) |
| stress | : | 3.60s CPU | 3.60s WALL (| 1 calls) |

```
Called by init_run:
```

| wfcinit | : | 2.59s CPU | 2.64s WALL (| 1 | calls) |
|------------|-------|-----------|--------------|---|----------|
| wfcinit:at | om : | 0.01s CPU | 0.01s WALL (| | 8 calls) |
| wfcinit:w | fcr : | 2.54s CPU | 2.58s WALL (| | 8 calls) |
| potinit | : | 0.31s CPU | 0.32s WALL (| 1 | calls) |
| hinit0 | : | 0.35s CPU | 0.38s WALL (| 1 | calls) |

Called by electrons:

| c_bands | : | 265.39s CPU | 270.53s WALL | (51 | calls) |
|----------|---|-------------|--------------|-------|--------|
| sum_band | : | 40.45s CPU | 41.09s WALL | (51 | calls) |
| v_of_rho | : | 1.77s CPU | 1.78s WALL (| 51 | calls) |
| v_h : | | 0.13s CPU (| 0.13s WALL (| 51 | calls) |
| v_xc : | | 1.70s CPU | 1.71s WALL (| 53 | calls) |
| newd | : | 2.23s CPU | 2.25s WALL (| 51 | calls) |
| PAW_pot | : | 6.98s CPU | 7.05s WALL (| 51 | calls) |
| mix_rho | : | 0.35s CPU | 0.35s WALL (| 51 ca | lls) |

Called by c_bands:

| init_us_2 | : | 0.95s CPU | 0.98s WALL (| 840 | calls) |
|-----------|---|-------------|----------------|-----|--------|
| cegterg | : | 260.24s CPU | 265.27s WALL (| 408 | calls) |

Called by sum_band:

| sum_band:b | ec : | 0.60s CPU | 0.60s WALL (| 408 calls) |
|------------|------|-----------|--------------|------------|
| addusdens | : | 2.60s CPU | 2.62s WALL (| 51 calls) |

Called by *egterg:

| h_psi | : | 147.41s CPU | 149.67s WALL (| 1103 | calls) |
|------------|------|--------------|----------------|--------|--------|
| s_psi | : | 9.22s CPU | 9.24s WALL (1 | 103 | calls) |
| g_psi | : | 0.22s CPU | 0.22s WALL (| 687 | calls) |
| cdiaghg | : | 78.35s CPU | 80.84s WALL (| 1087 | calls) |
| cegterg:o | ver | : 10.88s CPU | 11.10s WALL (| 687 | calls) |
| cegterg:uj | pda | : 5.96s CPU | 5.98s WALL (| 687 | calls) |
| cegterg:la | st : | 4.47s CPU | 4.48s WALL (| 408 | calls) |
| cdiaghg:c | hol | : 5.30s CPU | 5.69s WALL (| 1087 | calls) |
| cdiaghg:in | nve | : 4.68s CPU | 4.70s WALL (| 1087 | calls) |
| cdiaghg:p | ara | : 8.51s CPU | 9.34s WALL (| 2174 c | alls) |

Called by h_psi:

h_psi:pot : 147.18s CPU 149.43s WALL (1103 calls) h_psi:calbec : 10.77s CPU 10.80s WALL (1103 calls) vloc_psi : 127.03s CPU 129.25s WALL (1103 calls) add_vuspsi : 9.38s CPU 9.39s WALL (1103 calls)

General routines

| calbec | : | 16.50s CPU | 16.54s WALL | (1551 calls) |
|----------|-----|-------------|--------------|-----------------|
| fft | : | 1.65s CPU | 1.69s WALL (| 687 calls) |
| ffts | : | 0.08s CPU | 0.08s WALL (| 102 calls) |
| fftw | : | 150.53s CPU | 153.01s WALL | (536030 calls) |
| interpol | ate | : 0.17s CPU | 0.17s WALL | (51 calls) |

Parallel routines

| fft_scatt_xy : | 7.49s CPU | 8.62s WALL (536819 calls) |
|----------------|-------------|------------------------------|
| fft_scatt_yz : | 102.55s CPU | 102.73s WALL (536819 calls) |

PAW routines

PAW_pot : 6.98s CPU 7.05s WALL (51 calls)

PWSCF : 5m30.45s CPU 5m39.24s WALL

This run was terminated on: 20:33:34 28Apr2020

JOB DONE.

Et cetera

APPENDIX II

Structural and electronic properties of the iron pnictide compound EuFe2As2 from first principles.We report results of the electronic and mechanical structure properties of the iron pnictide compound EuFe₂As₂, at zero pressure. The open source computer code Quantum Espresso, which incorporates the Density Functional Theory (DFT), Pseudo Potentials (PP) and the Plane Wave (PW) were used to perform calculations from first principles. Projector-Augmented Wave (PAW) Pseudo Potentials were used in these calculations. The Density of States exhibits a sizeable superconducting gap and the band structure has no band gap. Calculations were performed from scratch.

APPENDIX III: First principle study of the Mechanical properties and phonon dispersion of the iron pnictide compound EuFe2As2

We present results on the first principle study of the elastic constants and the phonon dispersion of EuFe₂As₂ at zero pressure. The ground-state energy calculations were performed within Density Functional Theory (DFT) and the generalized gradient approximation using the pseudo potential method with plane-wave basis sets. The projector augmented-wave (PAW) pseudo potentials were used in our calculation. The open source code QUANTUM ESPRESSSO was used with its pseudo potential database. The study on the elastic constants at zero pressure was a clear indication that the compound is mechanically stable, and the phonon dispersion study also indicated that the compound is dynamically stable. The elastic constants and mechanical properties also led to the conclusion that the compound is ductile and anisotropic.

APPENDIX IV: Letter of Introduction



APPENDIX V: Research Permit



APPENDIX VI: Plagiarism Report

AB-INITIO STUDY OF ELECTRONIC AND MECHANICAL STRUCTURE PROPERTIES OF THE SUPERCONDUCTING IRON PNICTIDE 0000000

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